

SOLAR CONSTRAINTS FOR PARTICLE PHYSICS

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IFAE – 22/05/2015

PLAN

Part I

- Standard solar models and the abundance problem
 - what is helioseismology and solar νs really tell us
- A generalized approach to solar models (with dark energy channels)
 - revisiting solar limits for axion-photon coupling and hidden photons

Part II

- Asymmetric dark matter in the Sun
 - q and v_{rel} dependent interactions
- A non-standard look at the solar abundance problem
 - evidence for ADM in the Sun

STANDARD SOLAR MODELS

SSM assumes

constant mass evolution – $1 M_{\odot}$

initially homogeneous

solar system age 4.57 Gyr

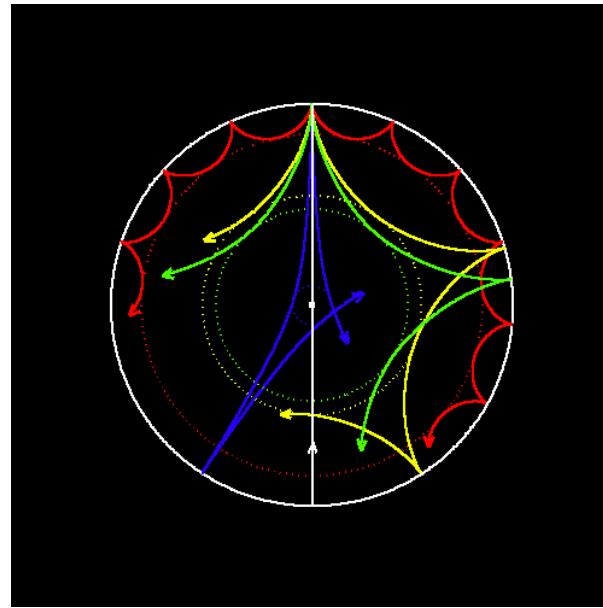
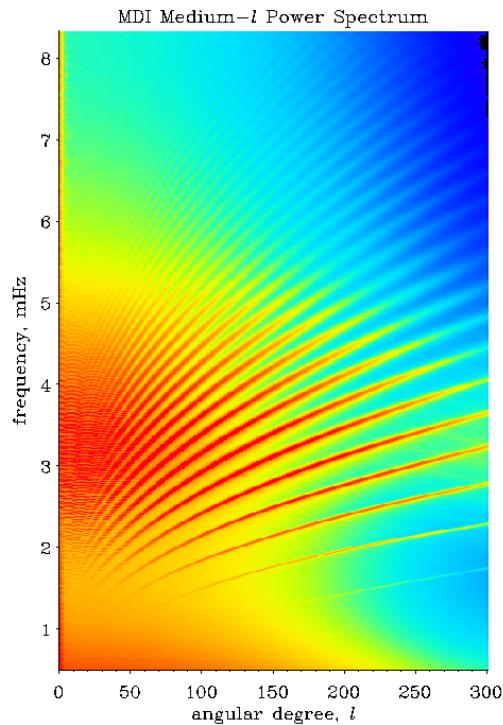
3 present-day constraints \leftrightarrow 3 adjustable quantities

Solar radius -- \rightarrow convection parameter – mixing length

Solar (photon) luminosity -- \rightarrow initial helium

Metal to hydrogen surface abundance (Z/X) -- \rightarrow initial metallicity

HELIOSEISMOLOGY



$\ell = 0$

$\ell = 2$

$\ell = 20$

$\ell = 25$

$\ell = 75$

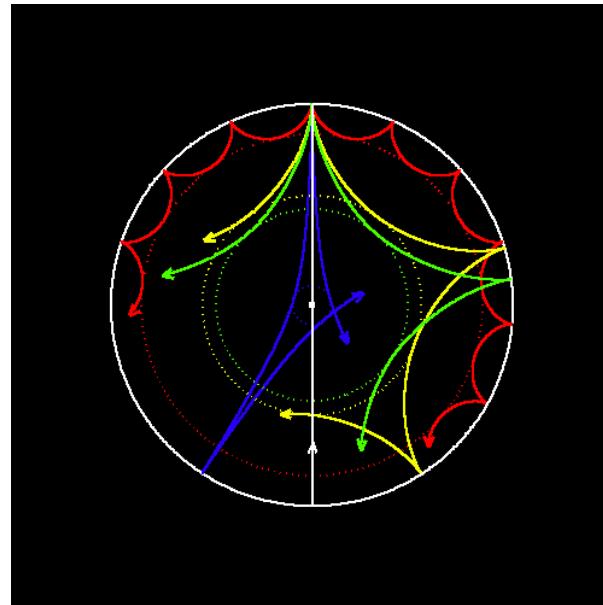
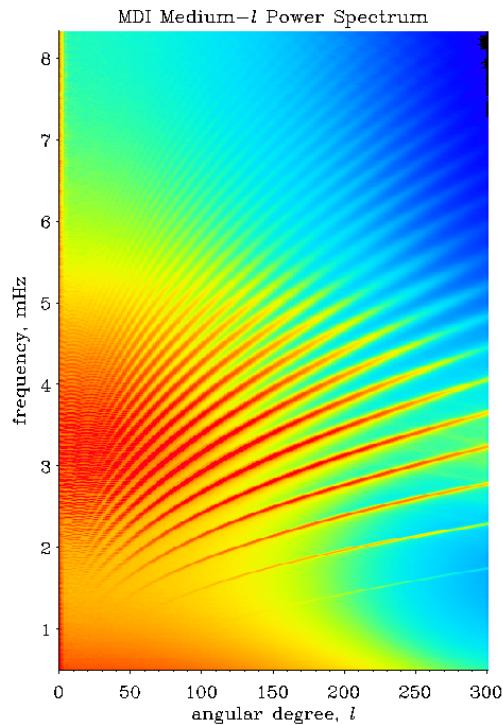
Acoustic p-modes – standing sound waves

$$c^2 = \frac{\Gamma_1 p}{\rho}$$

Low degree modes – probe the solar core

Mid/high degree – outer regions

HELIOSEISMOLOGY



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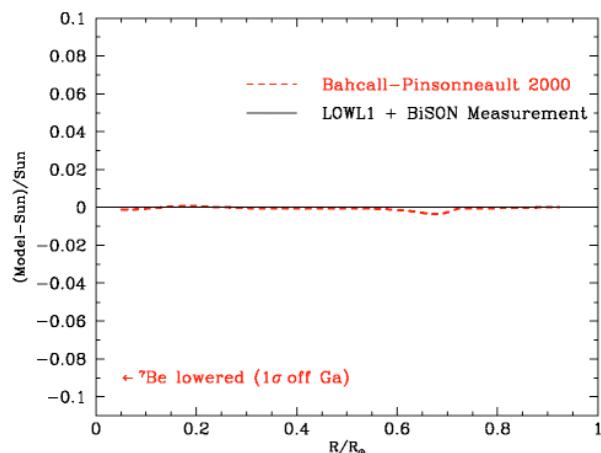
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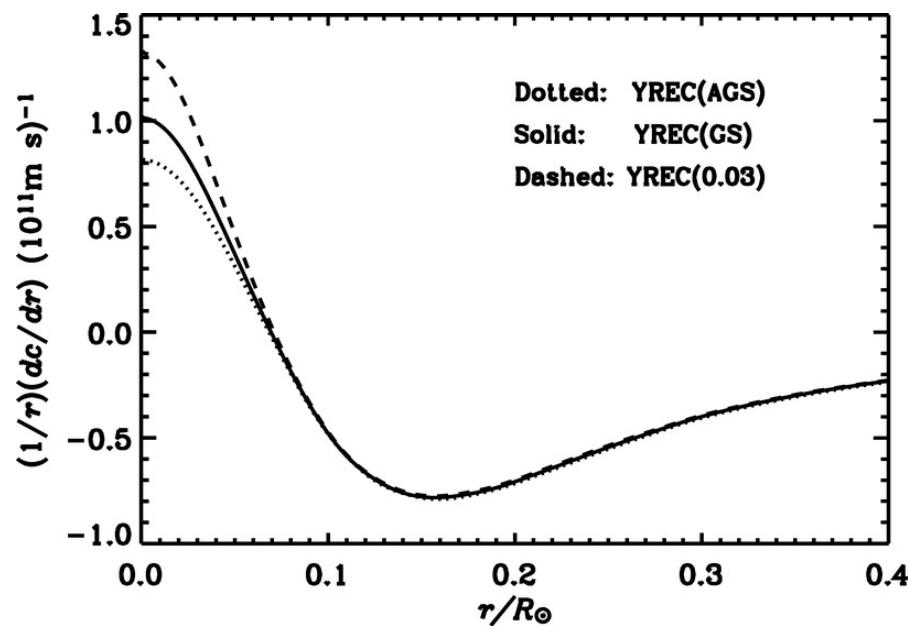
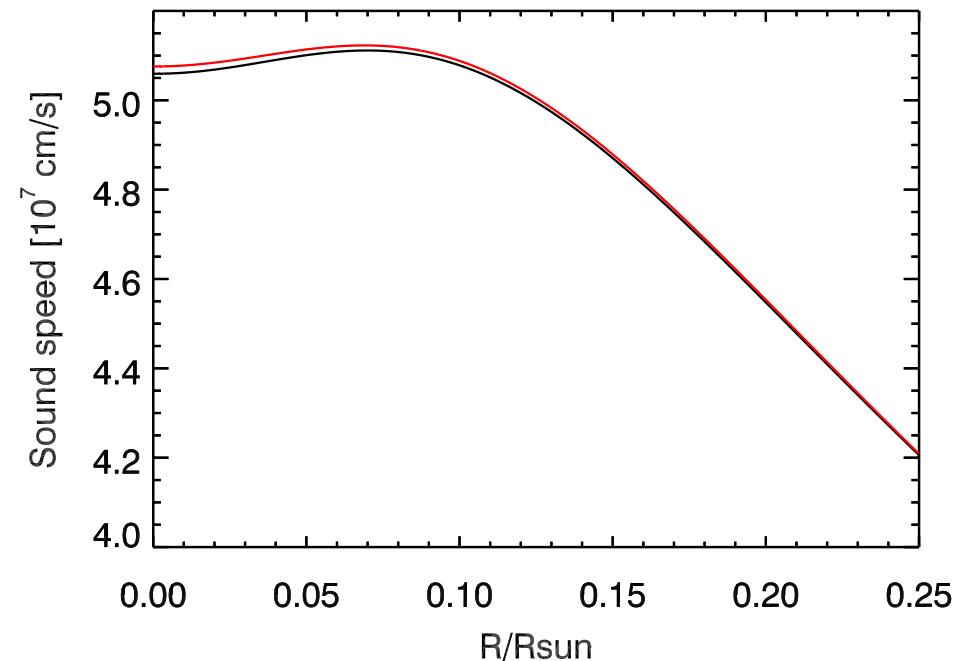
Sound speed profile from inversions -- >



HELIOSEISMOLOGY

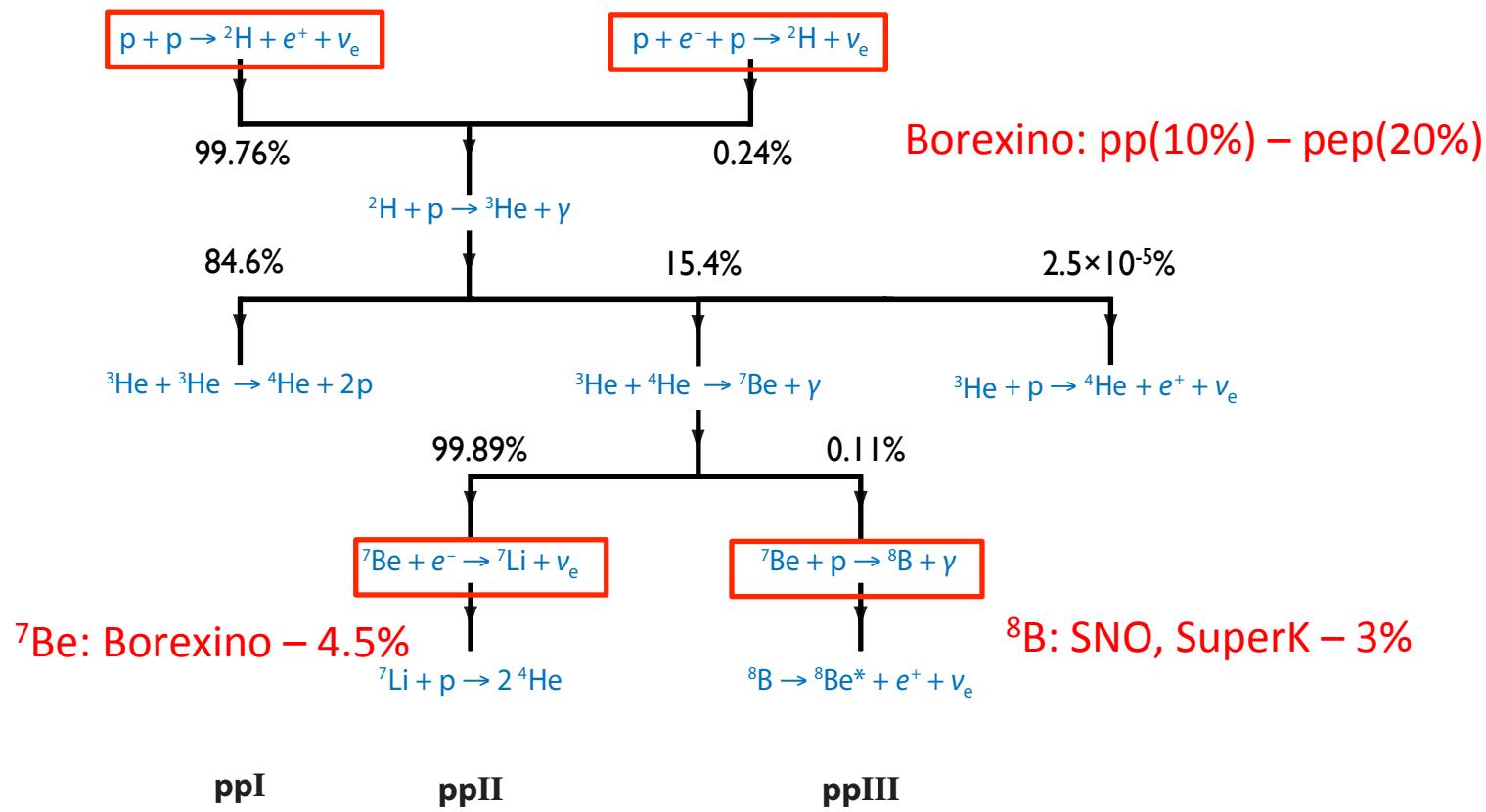
Low degree modes; $l=0, 1, 2, 3$ – frequency separation ratios

$$\left. \begin{aligned} r_{02} &= \frac{\nu_{n,0} - \nu_{n-1,2}}{\nu_{n,1} - \nu_{n-1,1}} \\ r_{13} &= \frac{\nu_{n,1} - \nu_{n-1,3}}{\nu_{n+1,0} - \nu_{n,0}} \end{aligned} \right\} \propto \int_0^R \frac{dc}{dr} \frac{dr}{r}$$



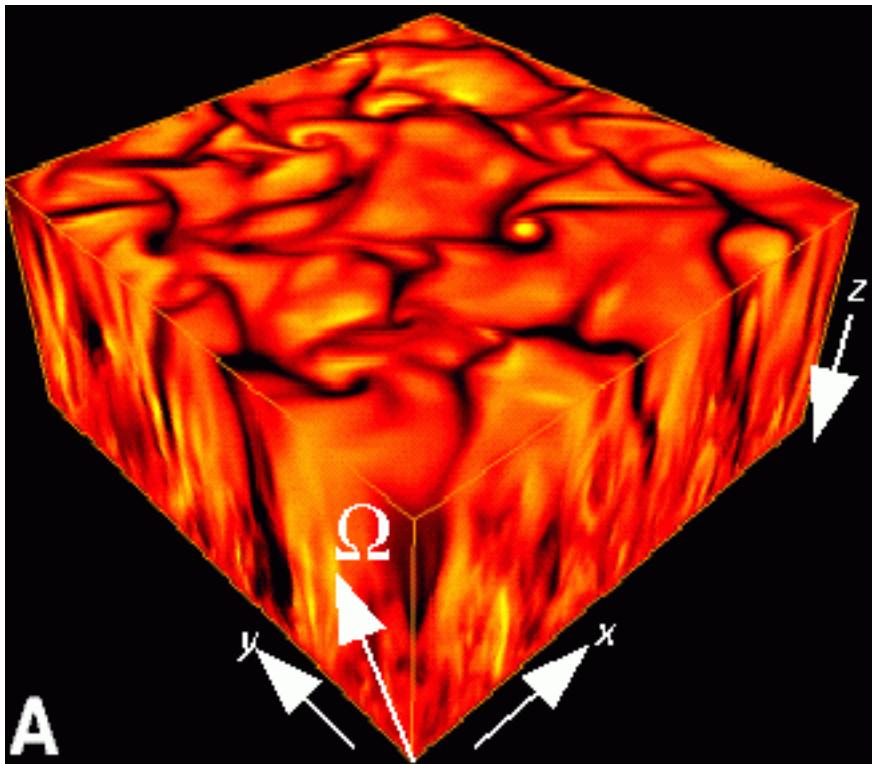
Frequency ratios: probing solar core

SOLAR NEUTRINOS: PP-CHAINS

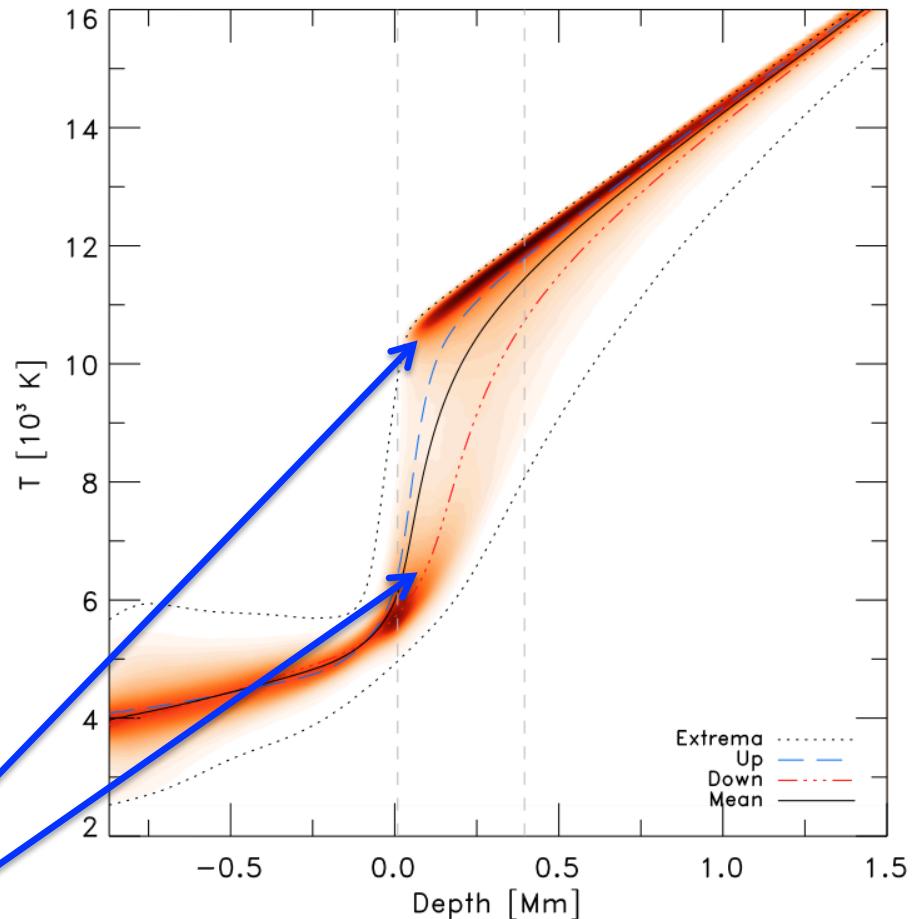


SOLAR ATMOSPHERES & ABUNDANCES

Dealing with convection



Hard to mimic with 1D models



Magic et al. 2014

SOLAR ABUNDANCES: END PRODUCT

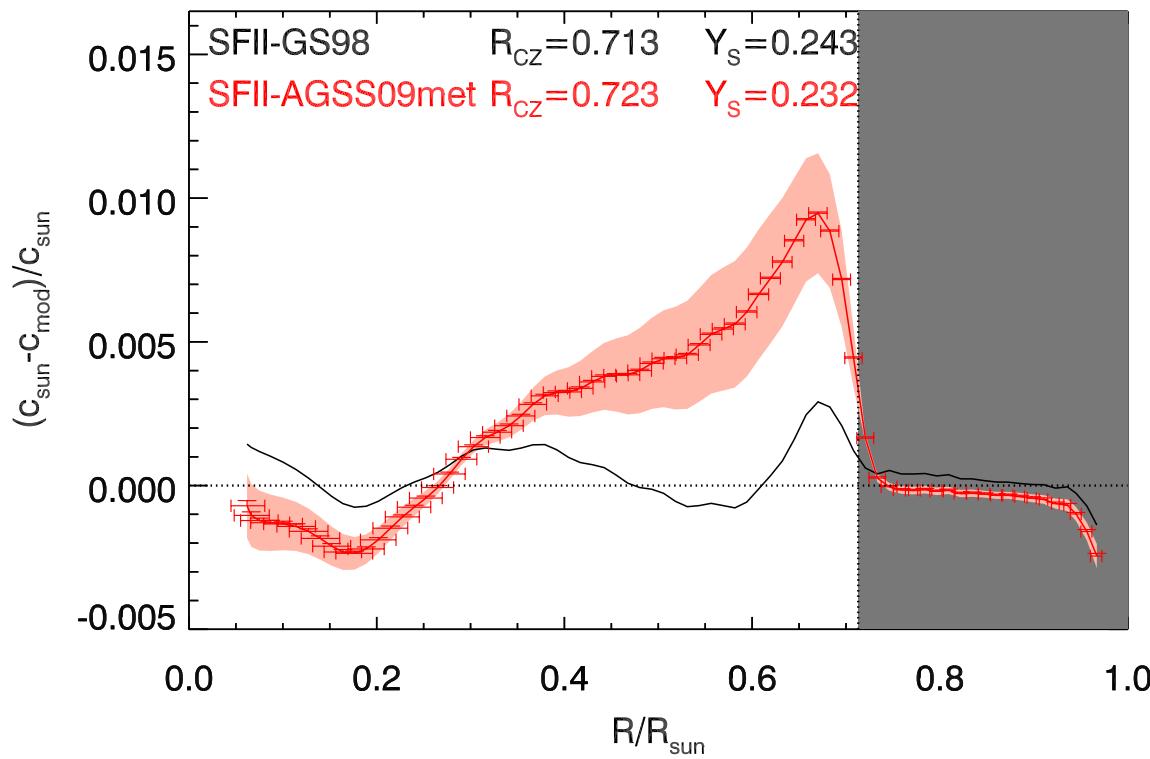
Element	GS98	AGSS09+met
C	8.52	8.43
N	7.92	7.83
O	8.83	8.69
Ne	8.08	7.93
Mg	7.58	7.53
Si	7.56	7.51
Ar	6.40	6.40
Fe	7.50	7.45
Z/X	0.0229	0.0178

Differences of

CNO(Ne)~30-40%

refractories~10%

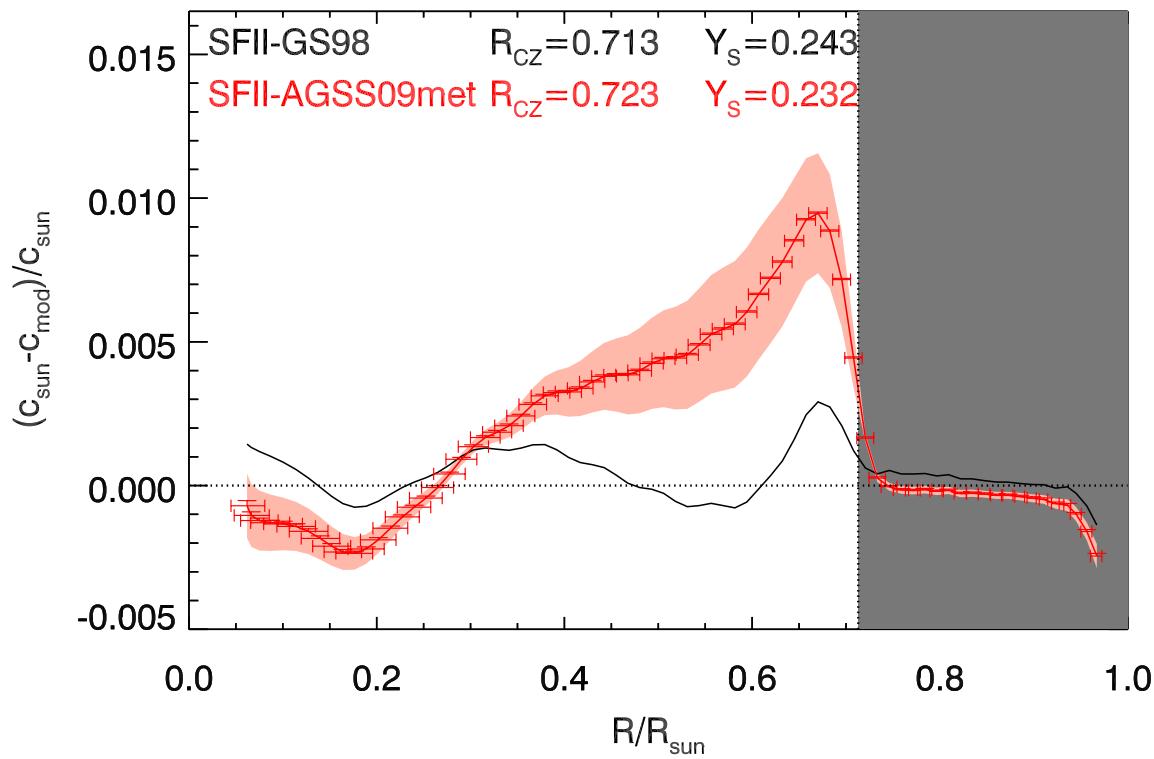
STANDARD SOLAR MODELS: HELIOSEISMOLOGY



	GS98	AGSS09	Helios.
(Z/X_{\odot})	0.0229	0.0178	—
R_{cz}/R_{\odot}	0.712	0.723	0.713 ± 0.001
Y_s	0.2429	0.2319	0.2485 ± 0.0034
$\langle \delta c/c \rangle$	0.0009	0.0037	—
$\langle \delta \rho/\rho \rangle$	0.011	0.040	—

Helioseismology --> high-Z

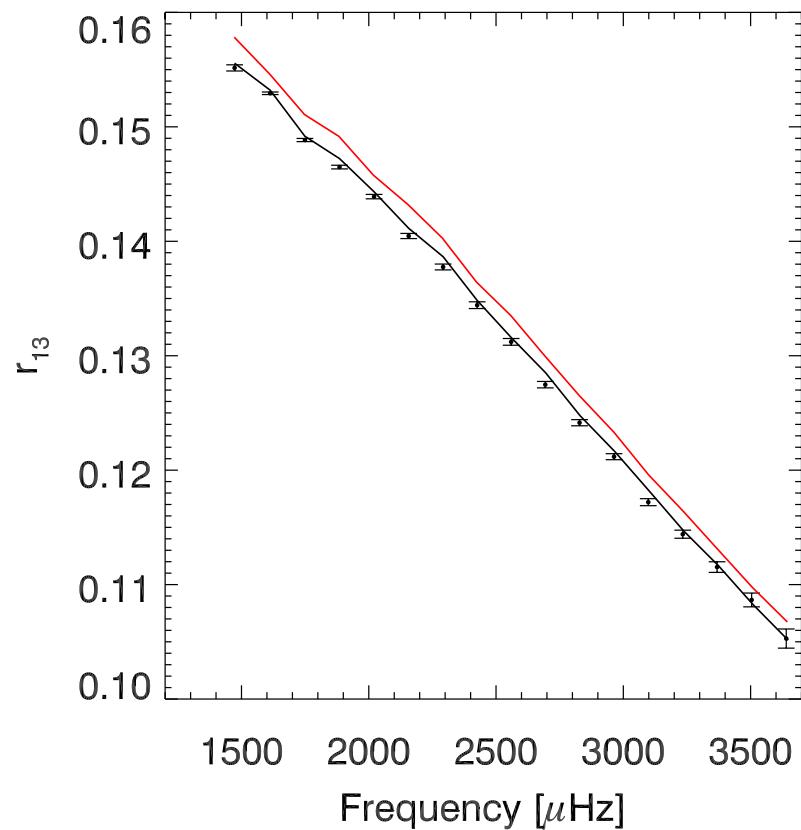
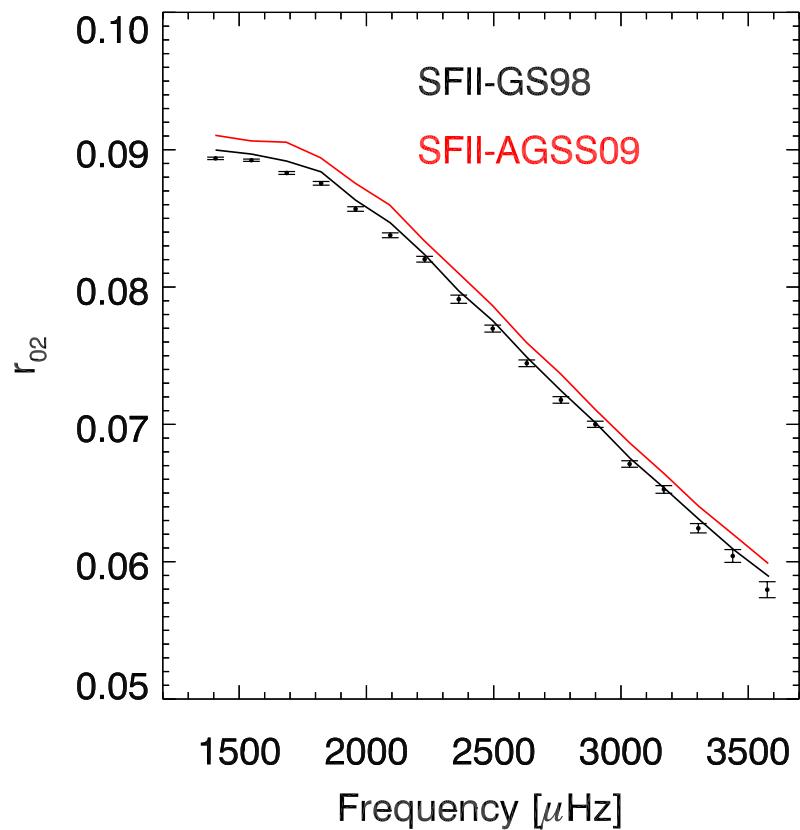
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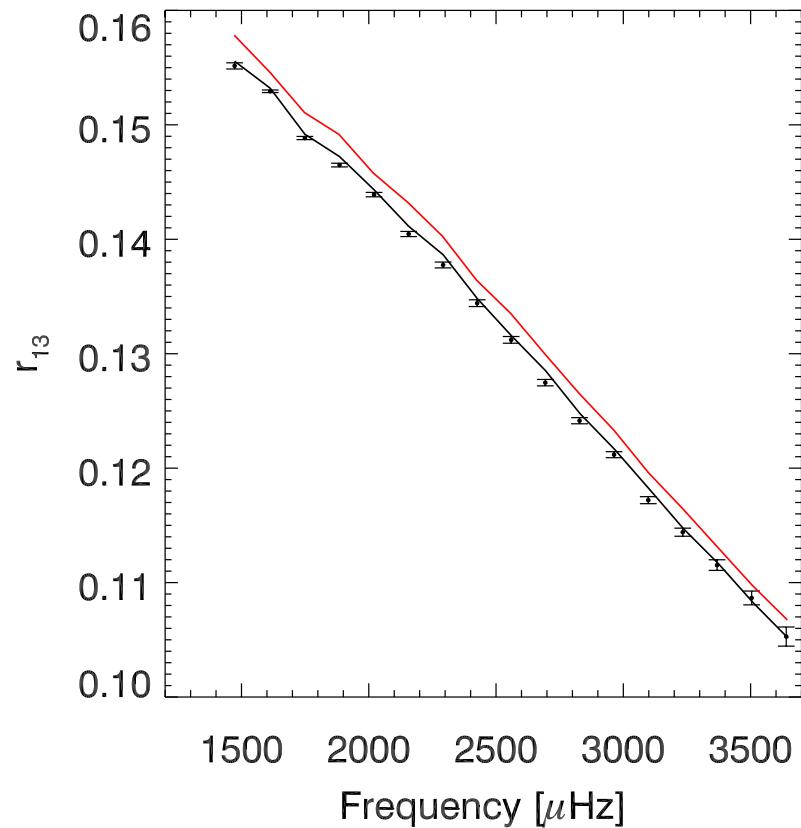
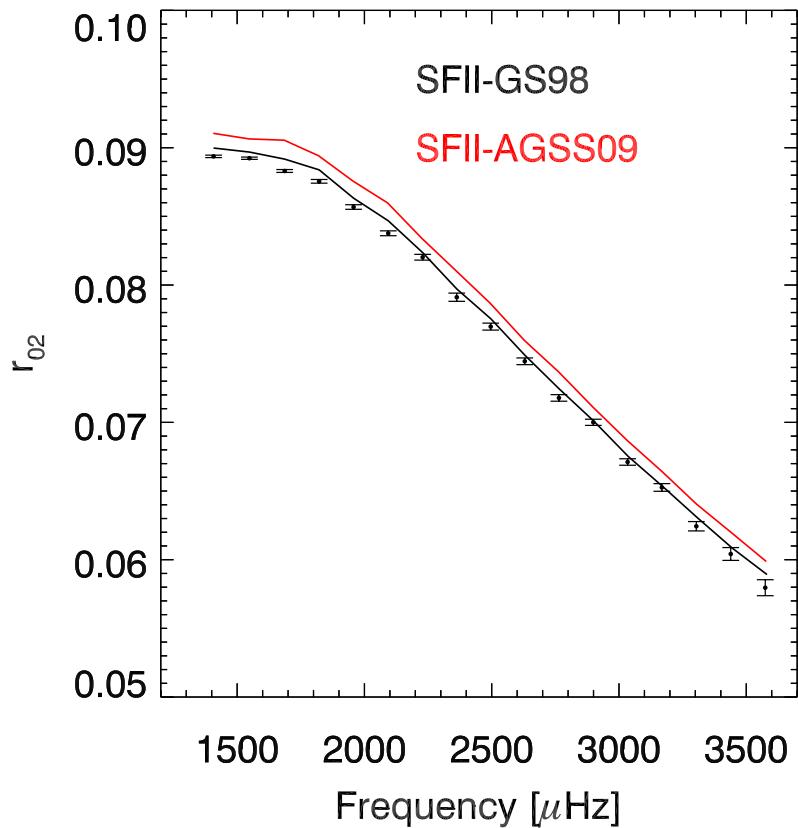
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STANDARD SOLAR MODELS: HELIOSEISMOLOGY



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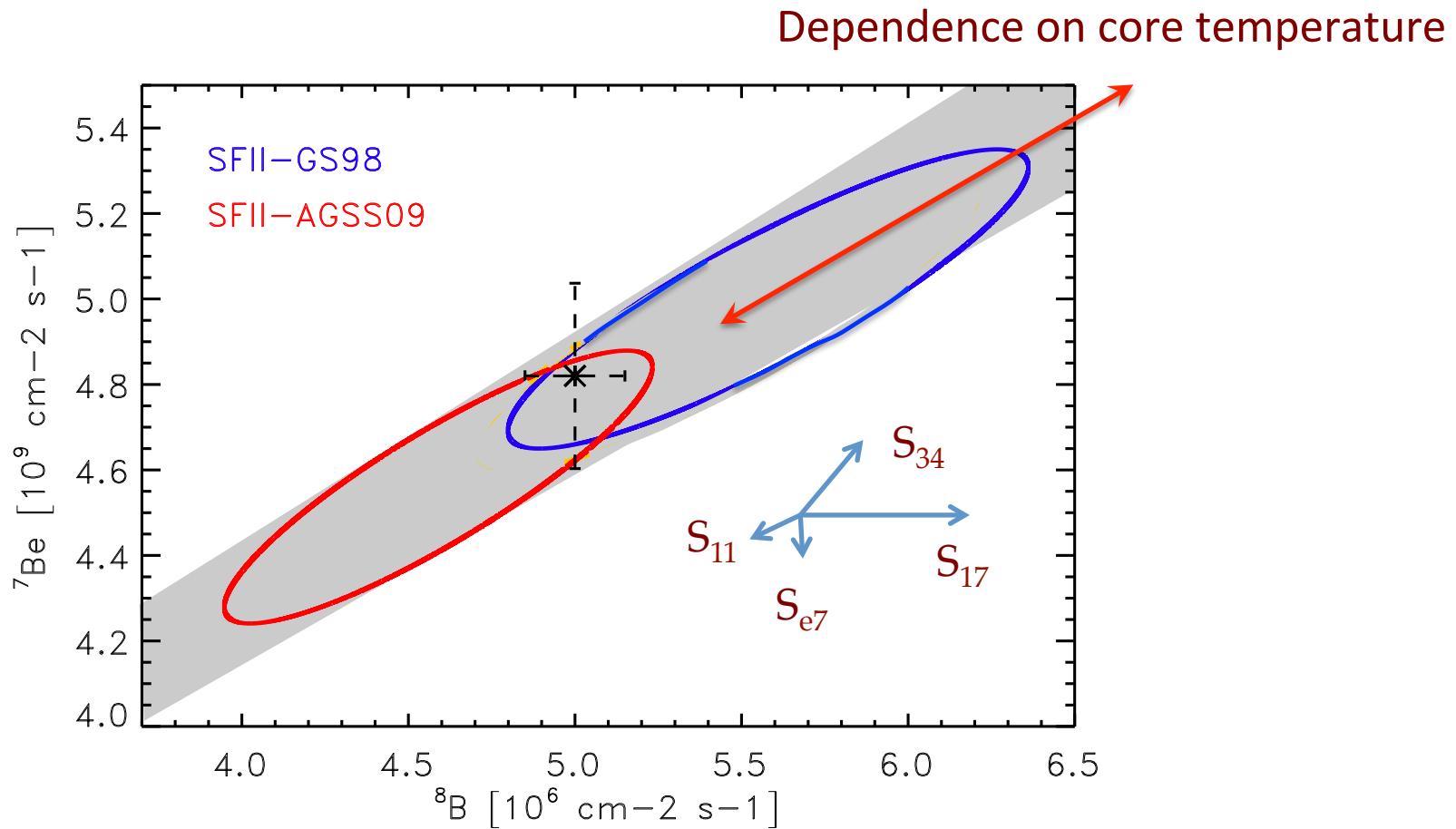


Helioseismic predictions of SSM --> high-Z
Solar atmospheres & spectroscopy --> low-Z

Solar Abundance Problem

STANDARD SOLAR MODELS: NEUTRINOS

Borexino (${}^7\text{Be}$) – SNO & SuperK (${}^8\text{B}$)



ROBUST INFERENCES FROM SSMS?

- * all robust helioseismic probes
- * pp-chain neutrinos depend



depend on T stratification, i.e.
energy transport
not directly on composition

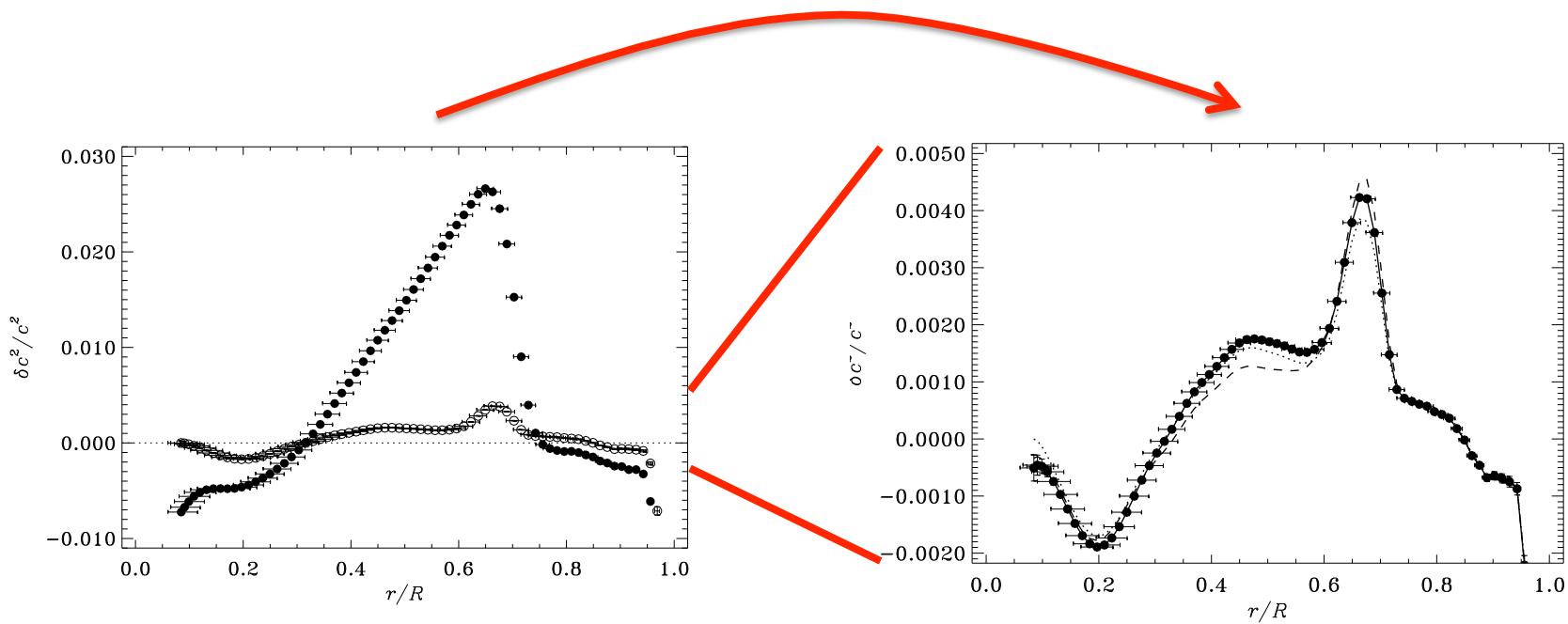
in solar interior T grad. scales with radiative opacity κ

degeneracy between κ and composition

Seismic data and pp-chain neutrinos constraint
radiative gradient / opacity profile

ROBUST INFERENCES FROM SSMS?

1st solution: modify opacity profile to recover good agreement with helioseismology



Christensen Dalsgaard et al 2009

ROBUST INFERENCE FROM SSMs?

- 2nd solution:
- * solar composition (2 parameters) free
 - * SSM input (~10) parameters move around central values
(nucl. x-sect., solar parameters, etc.)

$$\chi^2 = \min_{\{\xi_I\}} \left[\sum_Q \left(\frac{\delta Q_{\text{obs}} - \sum_I \xi_I C_{Q,I}}{U_Q} \right)^2 + \sum_I \xi_I^2 \right]$$

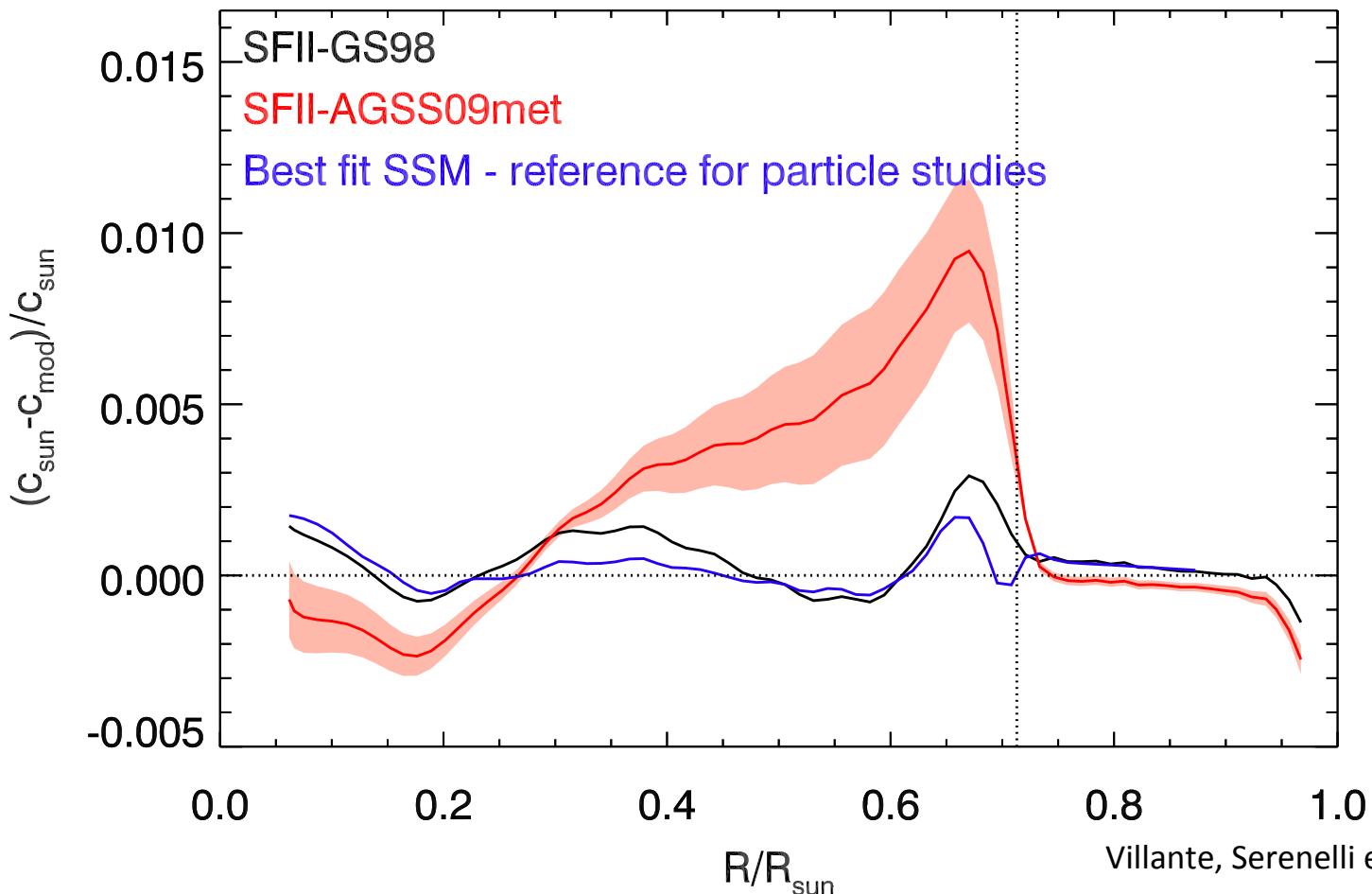
The equation is a sum of two terms. Three blue arrows point downwards from each term to their respective descriptions in red text below.

- An arrow points from the first term $\sum_Q \left(\frac{\delta Q_{\text{obs}} - \sum_I \xi_I C_{Q,I}}{U_Q} \right)^2$ to the text "seismic + neutrino observables".
- An arrow points from the second term $\sum_I \xi_I^2$ to the text "model correlations & pulls ξ_I of input parameters".

ROBUST INFERENCES FROM SSMs?

Even better than the real thing !!

Pulls from systematics of order 1 ($1-\sigma$)



TESTING THE METHOD: AXIONS-PHOTON COUPLING

Solar limits on axion-photon coupling

$$\mathcal{L}_{a\gamma} = g_{a\gamma} \mathbf{B} \cdot \mathbf{E}_a$$
$$g_{a\gamma} = g_{10} 10^{-10} \text{ GeV}^{-1}$$

Schlattl et al. 1999 – $g_{10} < 10$

Sound speed at $R = 0.1 R_\odot$ – equivalent to $L_a < 0.2 L_\odot$

Gondolo & Raffelt 2009 – $g_{10} < 7$

^8B flux $< 1.5 \ ^8\text{B}_{\text{SSM}}$ (3σ) – equivalent to $L_a < 0.1 L_\odot$

Maeda & Shibahashi 2013 – $g_{10} < 2.5$

^8B flux constrained by sound speed (1σ)

seismic (not evolutionary models – neglect basic physics)

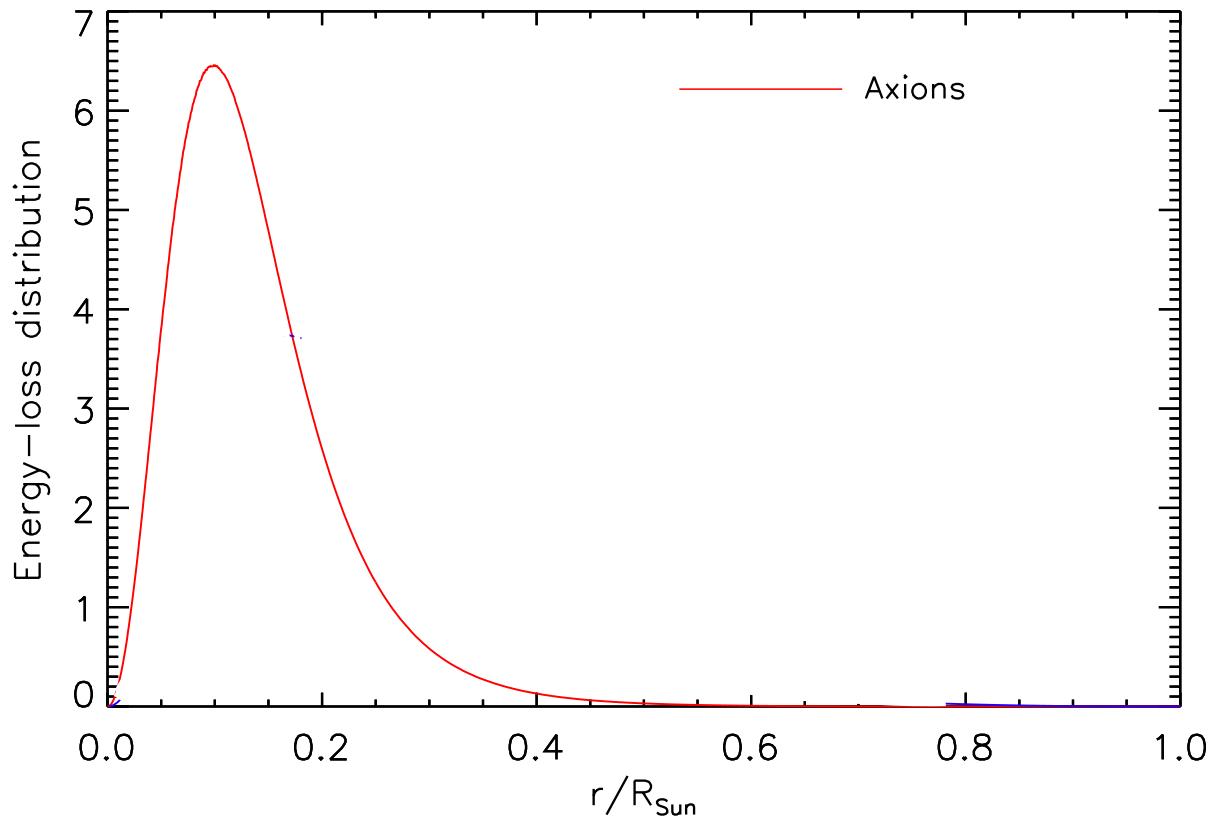
Vinyoles et al. 2015 – $g_{10} < 4$ (3σ)

seismic + neutrino data

extend the method used to construct best-fit SSM

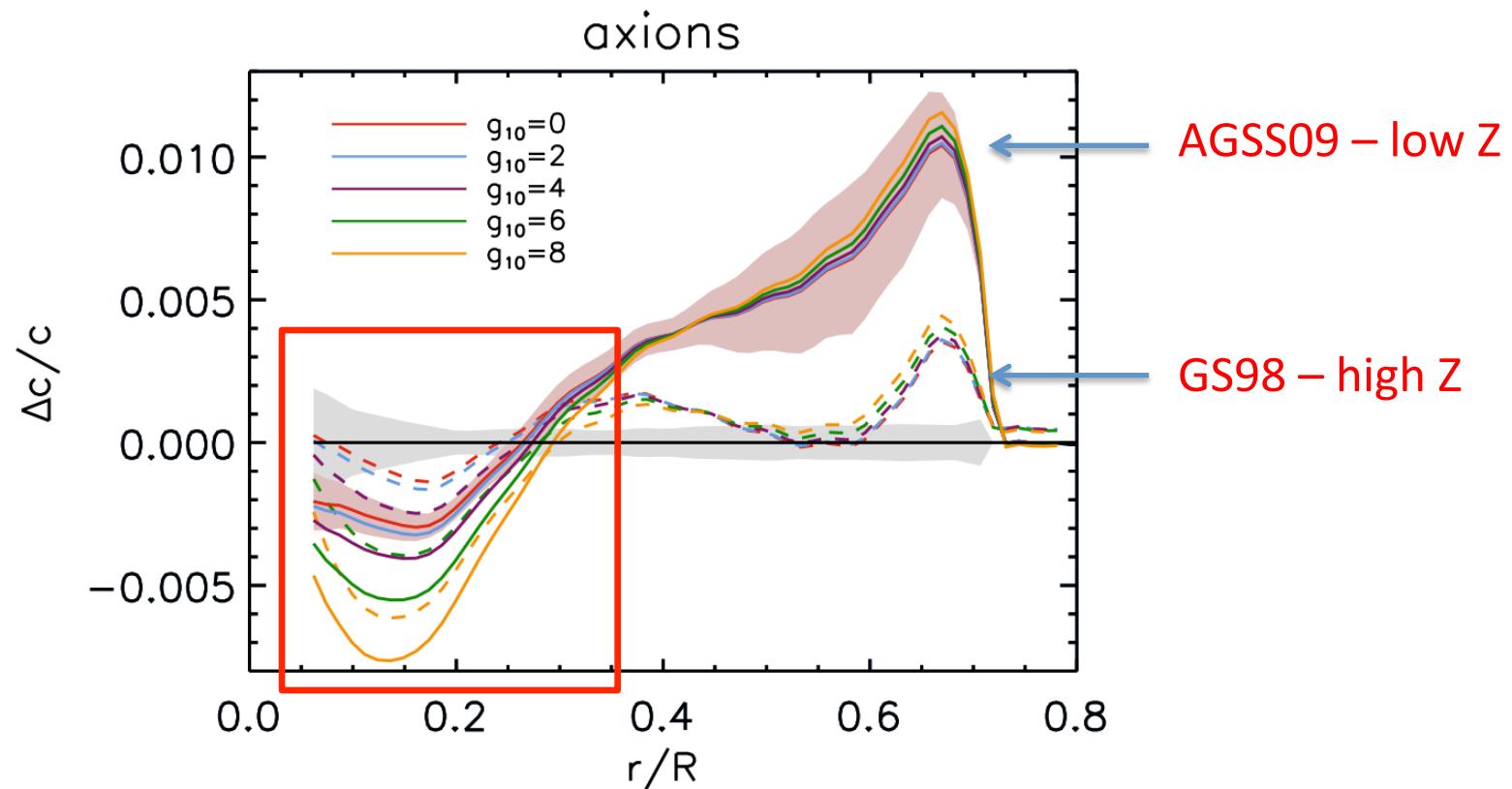
TESTING THE METHOD: AXIONS-PHOTON COUPLING

$$\epsilon_{a\gamma} \propto g_{a\gamma}^2 T^7 F(\kappa^2) \sim g_{a\gamma}^2 T^6 \quad \text{No explicit composition dependence}$$

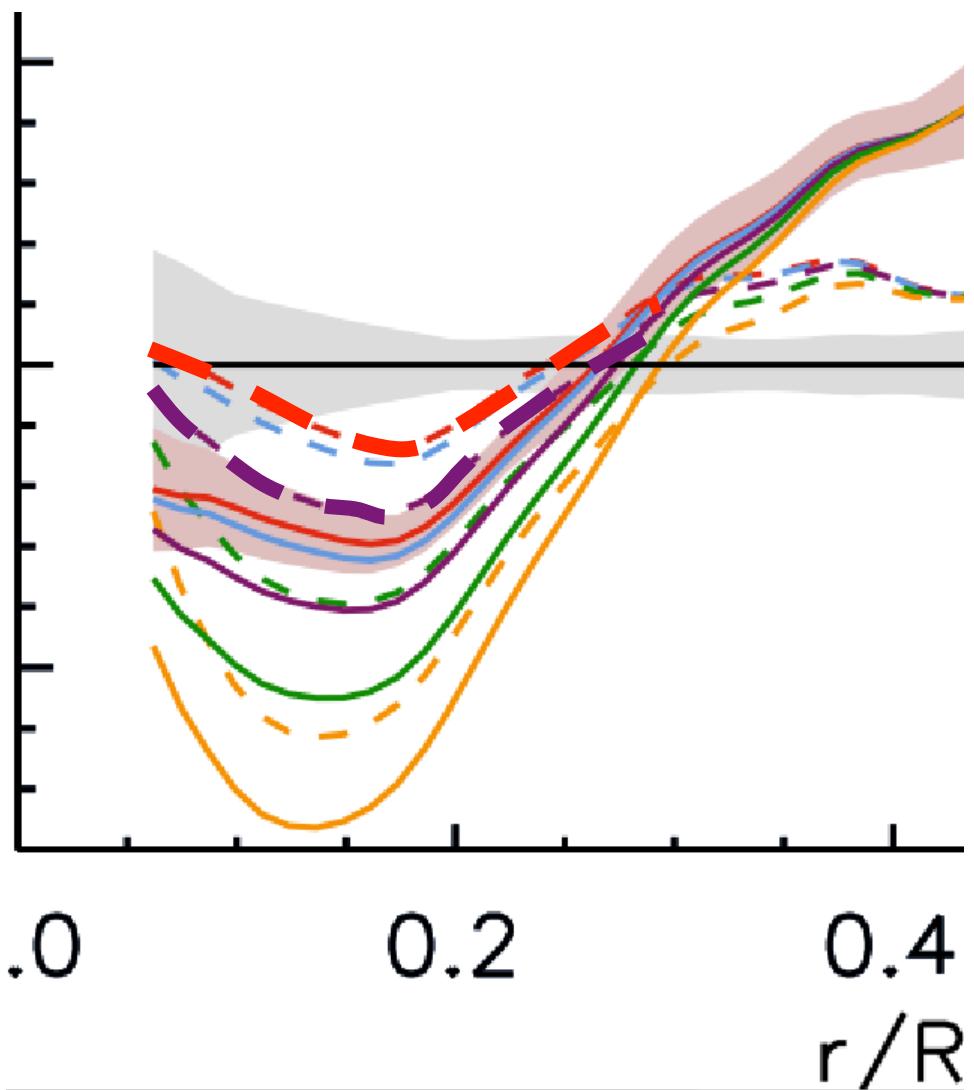


TESTING THE METHOD: AXIONS-PHOTON COUPLING

Variations in sound speed without variations in composition and pulls

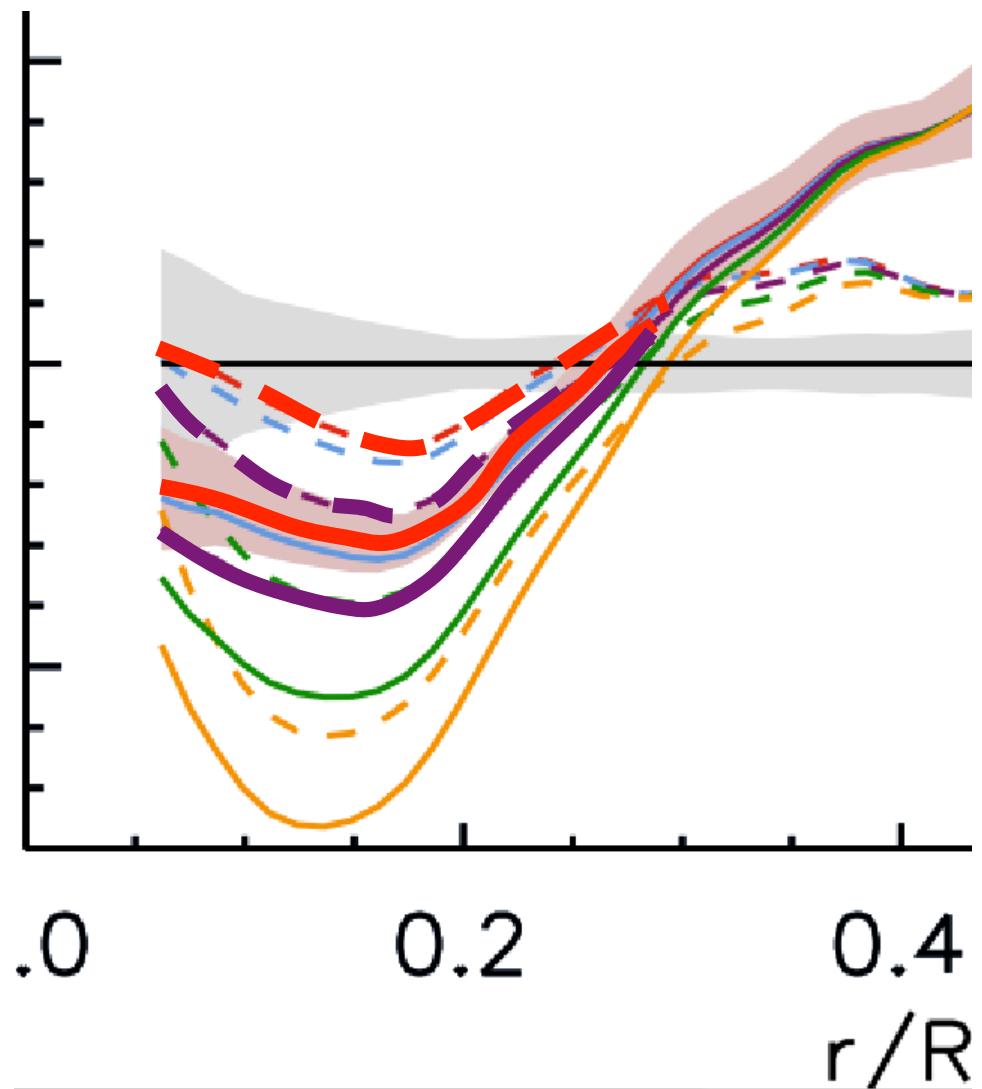


TESTING THE METHOD: AXIONS-PHOTON COUPLING



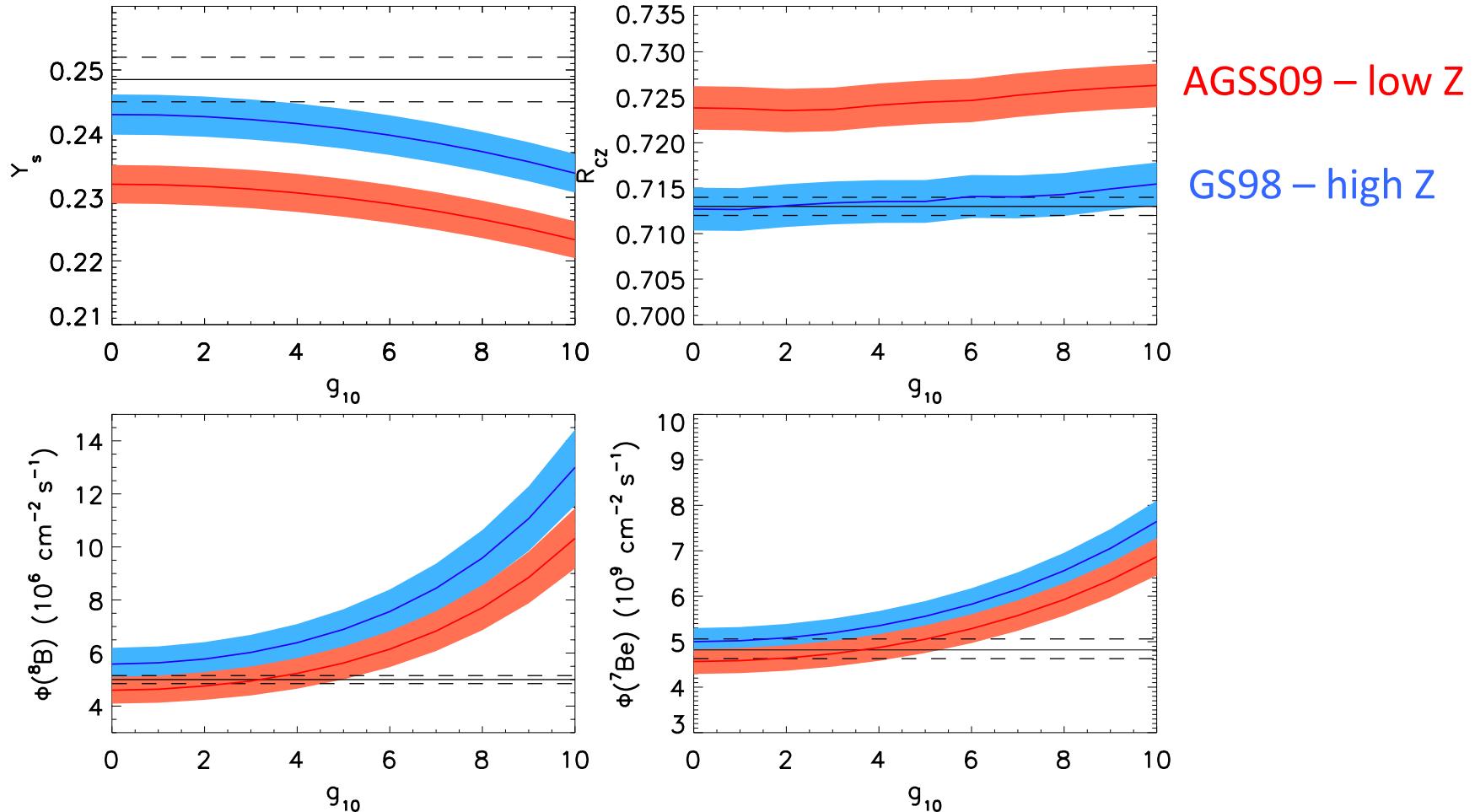
TESTING THE METHOD: AXIONS-PHOTON COUPLING

Relative changes are similar



TESTING THE METHOD: AXIONS-PHOTON COUPLING

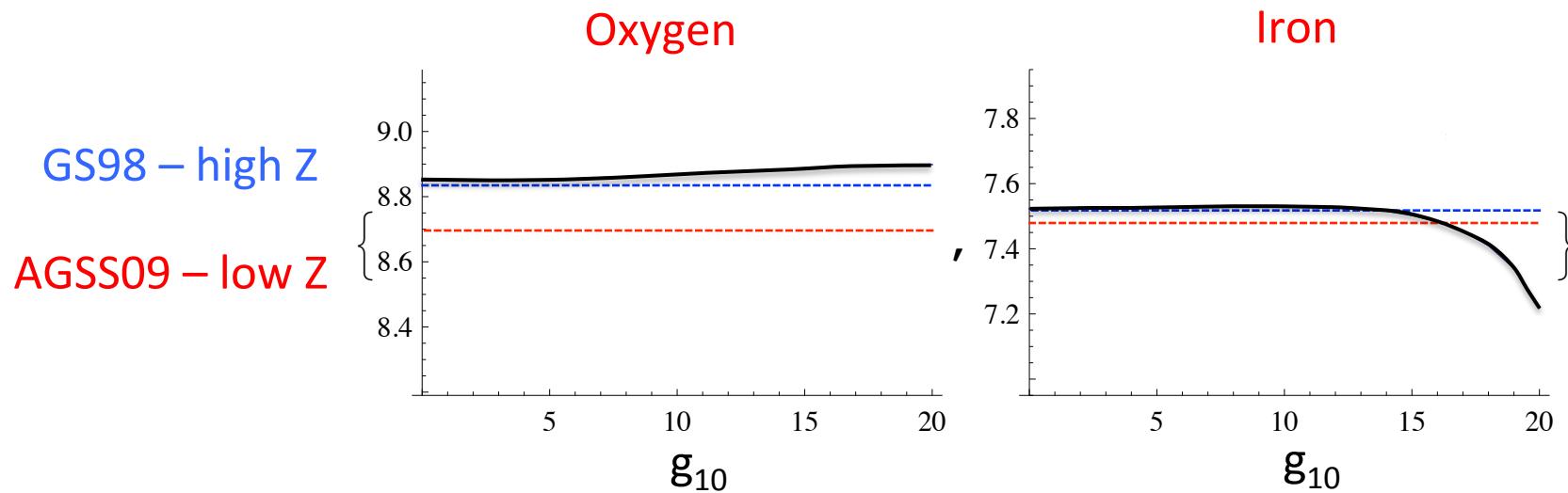
Variations in other quantities without variations in composition and pulls



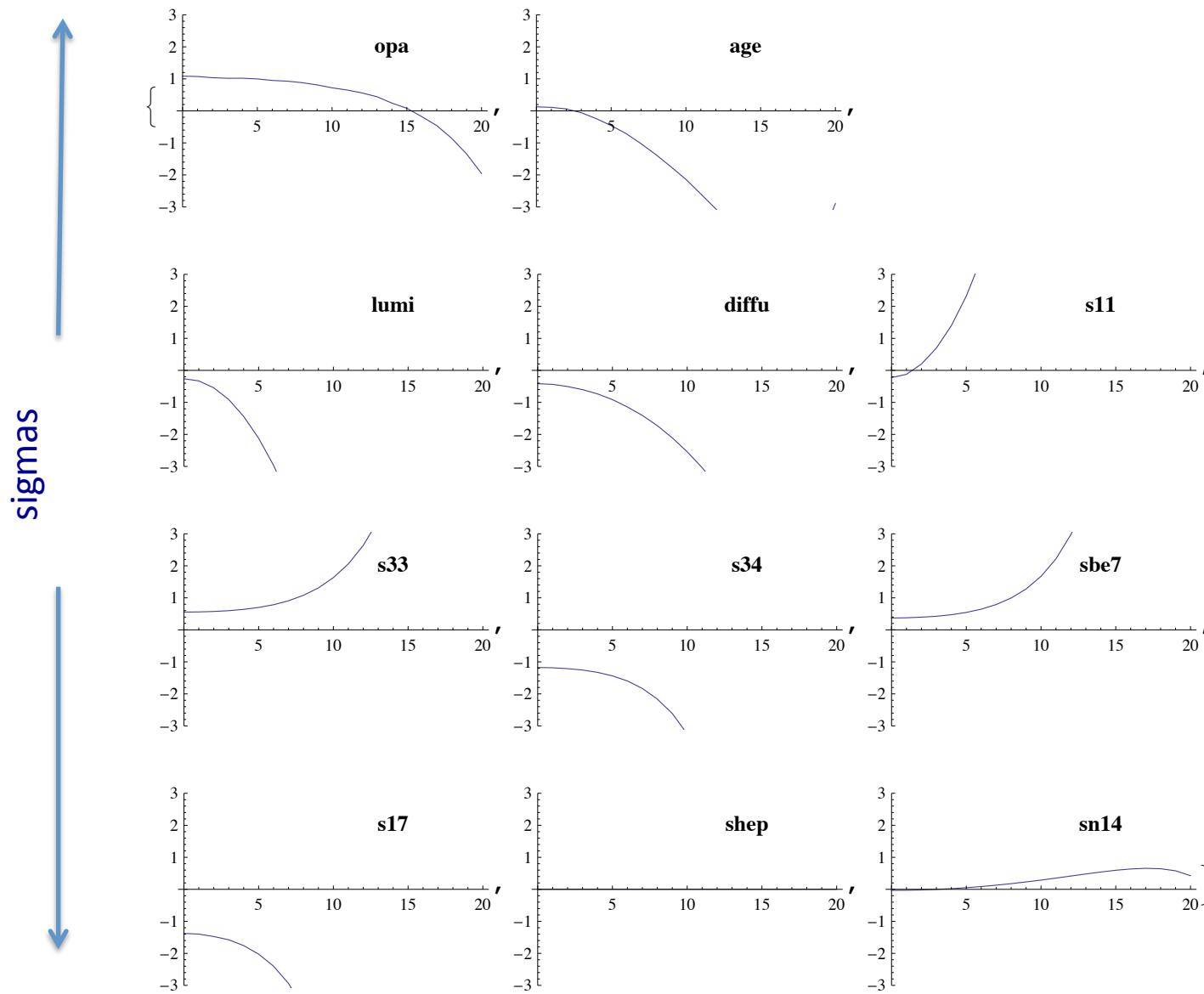
Changes due to axions and “zero point” of SSM to be accounted for by composition and systematics (pulls)

TESTING THE METHOD: AXIONS-PHOTON COUPLING

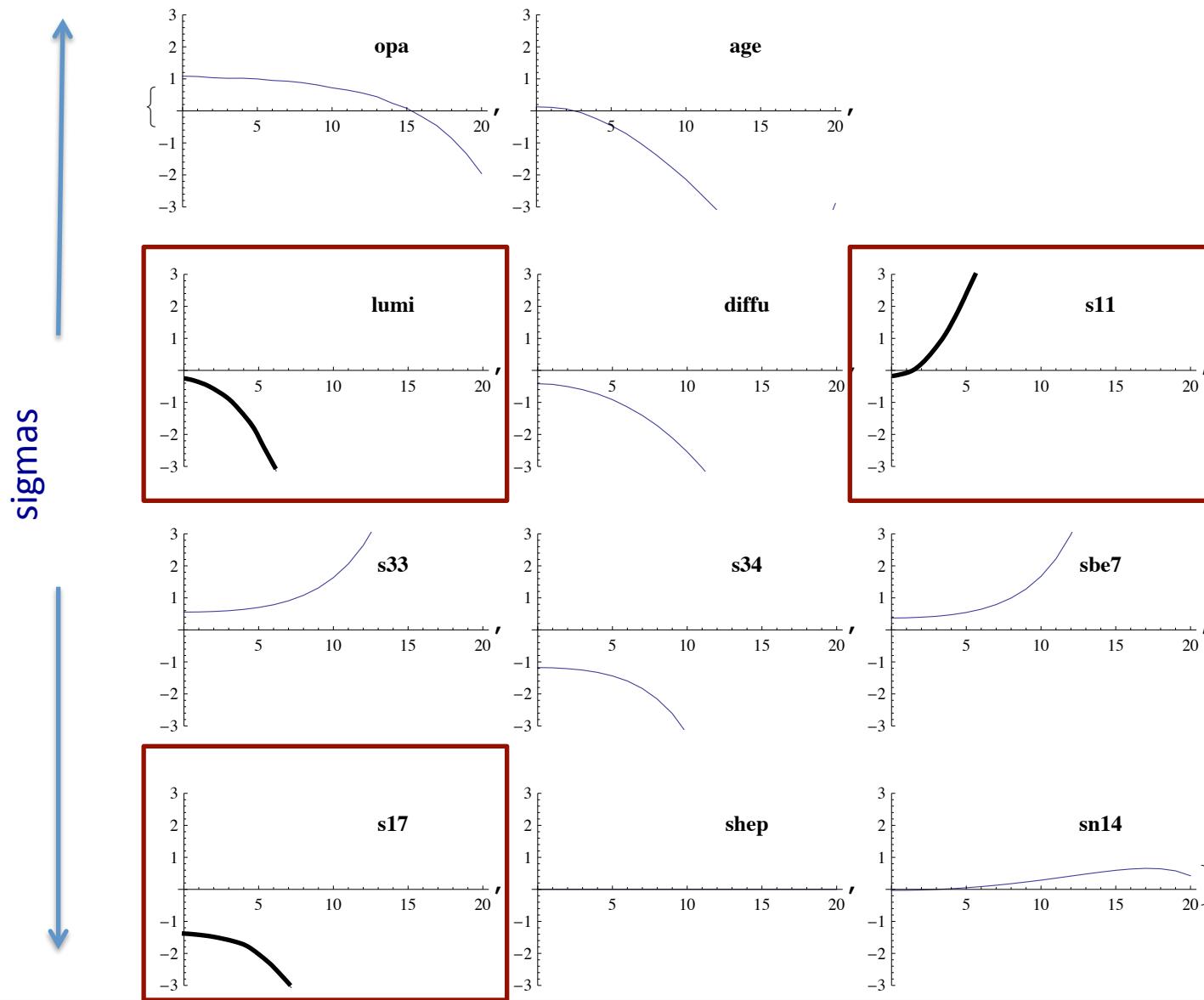
Full solution: composition is free and pulls computed to minimize χ^2 for fixed g_{10}



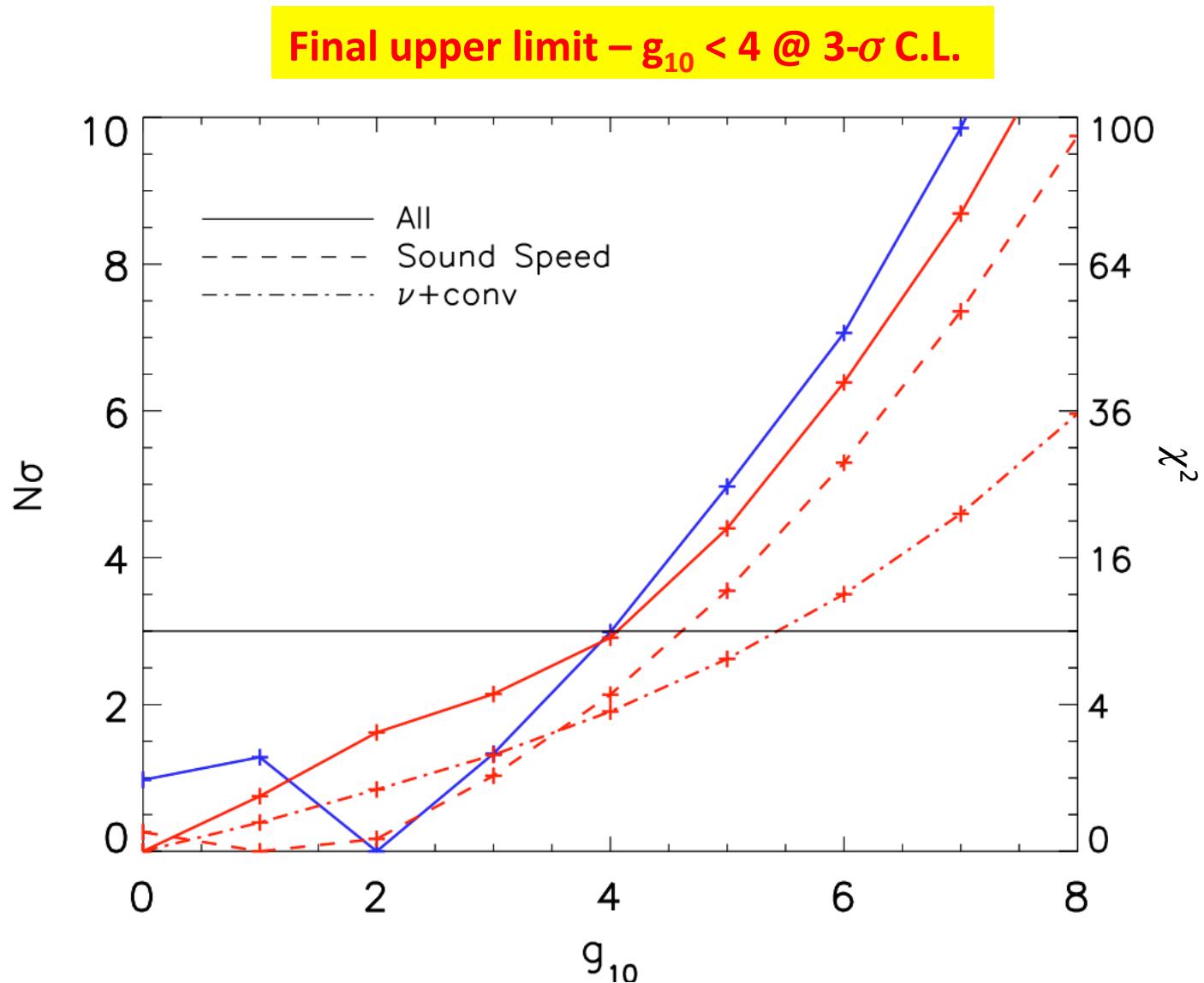
TESTING THE METHOD: AXIONS-PHOTON COUPLING



TESTING THE METHOD: AXIONS-PHOTON COUPLING



TESTING THE METHOD: AXIONS-PHOTON COUPLING



RECENT STELLAR LIMITS FOR g_{α}

Ayala et al. 2014 – $g_{10} < 0.66$

R parameter – HB/RGB stars – no syst. study of stellar uncertainties
He-core burning is a tricky business in stellar evolution

Friedland et al. 2013 – $g_{10} < 0.8$

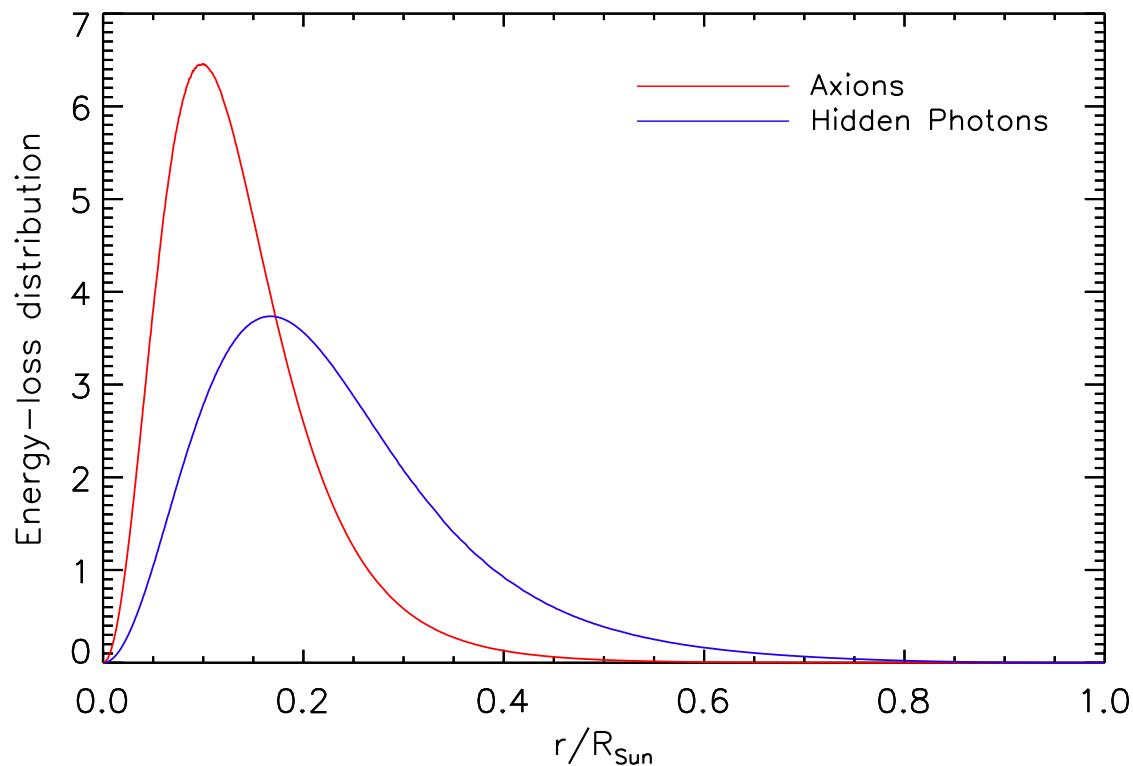
blue loop of Cepheids – stellar calculations are plainly wrong!!

HIDDEN PHOTONS

Energy losses dominated by the L-channel

$$\epsilon_{\text{hp}} = \frac{\chi^2 m^2}{e^{\omega_P/T} - 1} \frac{\omega_P^3}{4\pi} \frac{1}{\rho} \sim \chi^2 m^2 T$$

No explicit composition dependence

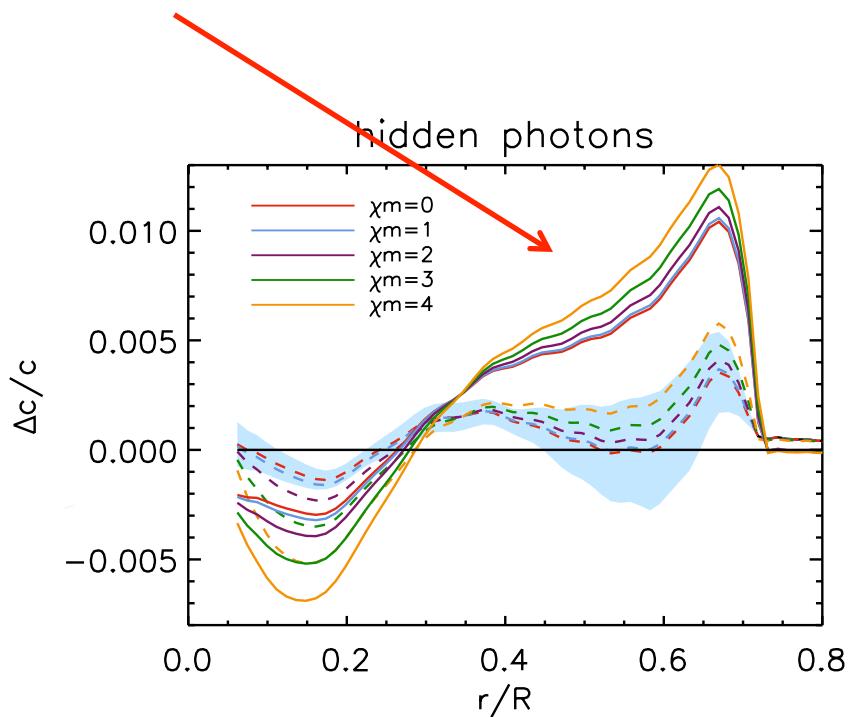
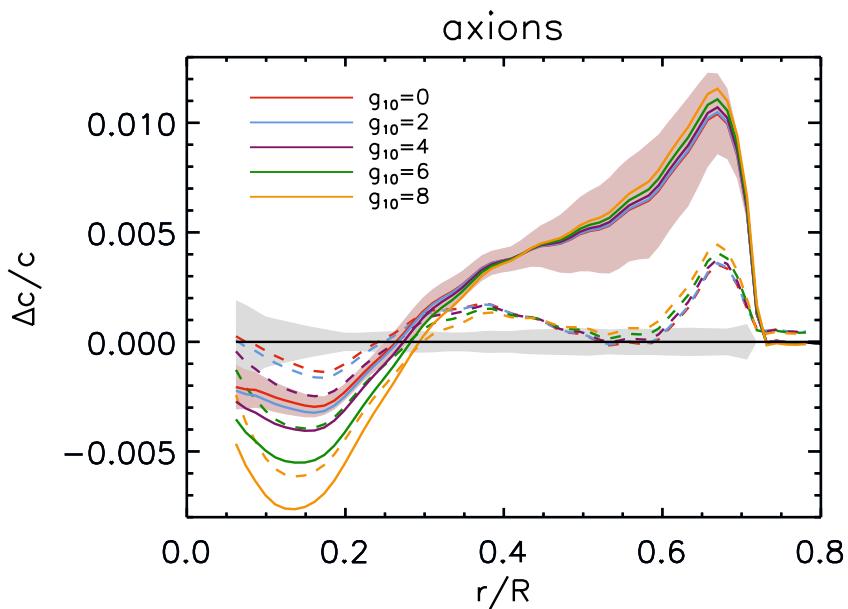


Weak T-dependence -- > broad production region

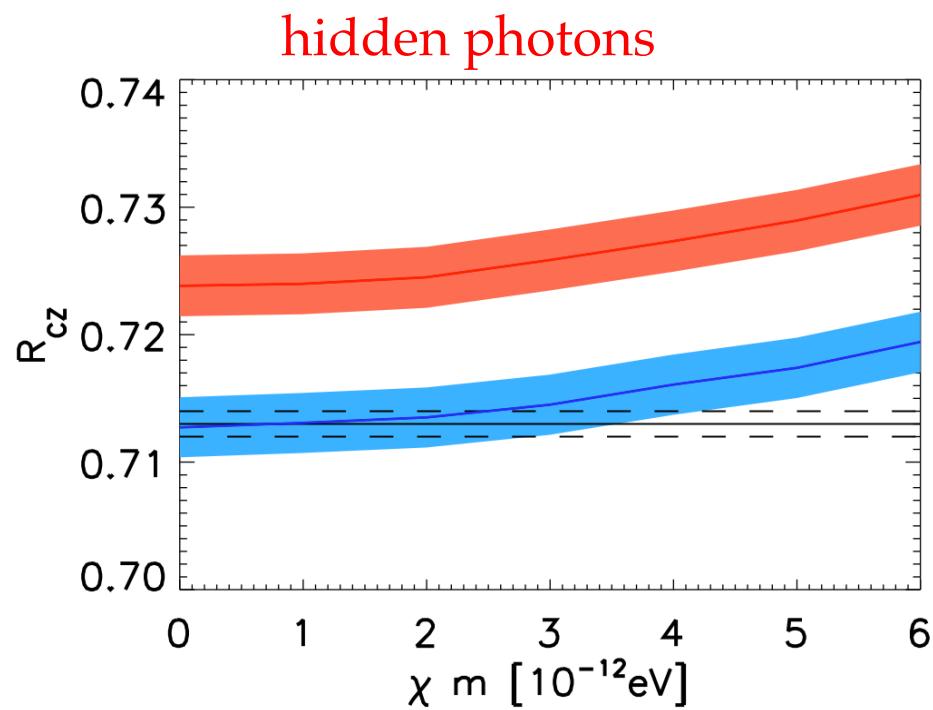
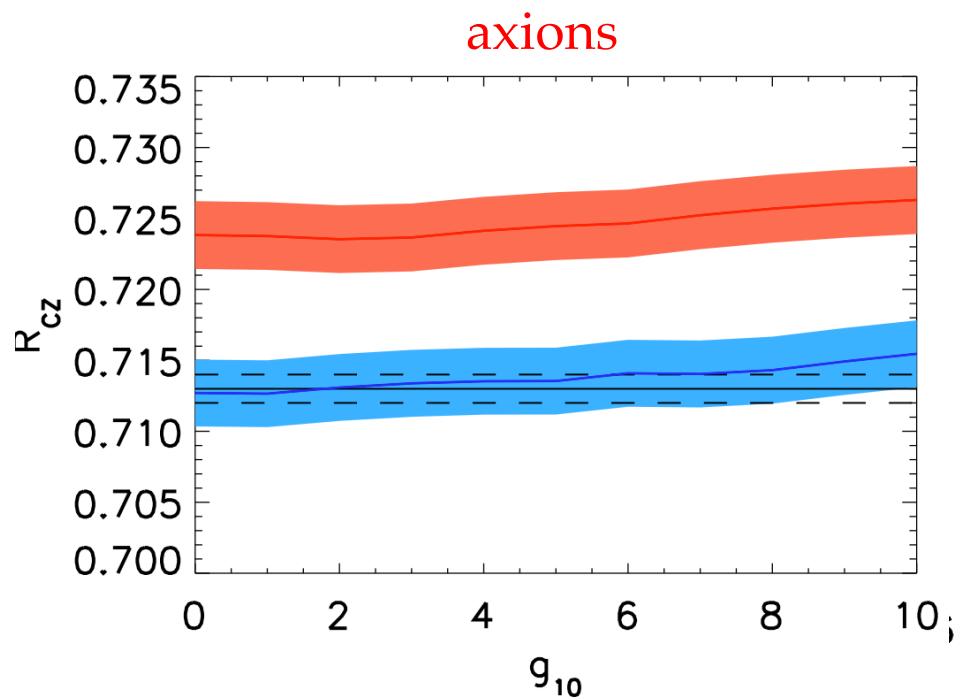
More relevant as T decreases (nucl. energy higher T-dependence)

HIDDEN PHOTONS

Variations in sound speed over whole radiative interior

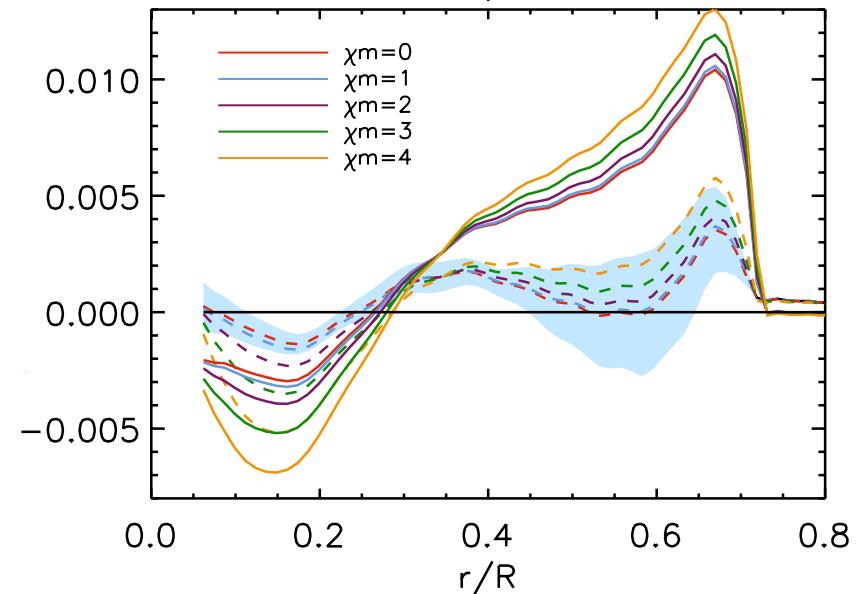
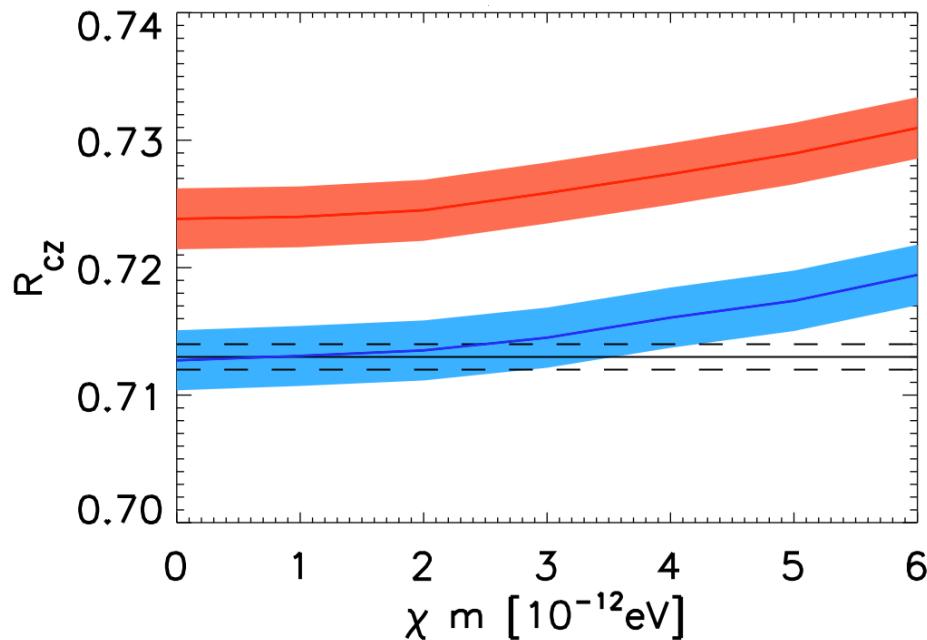


HIDDEN PHOTONS



Depth of convective envelope more sensitive to hidden photons than axions

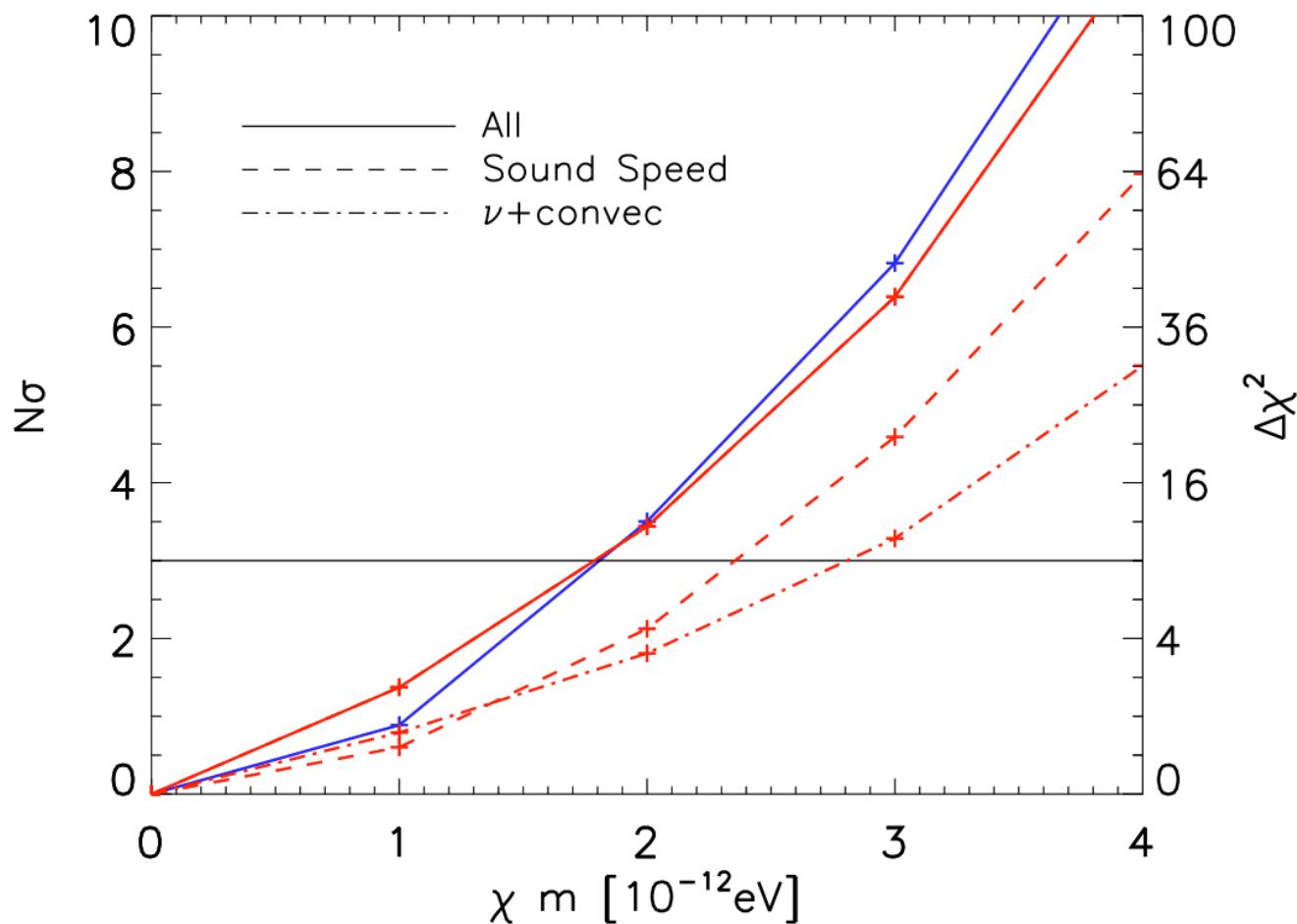
HIDDEN PHOTONS



Our approach: solar model absorbs these variations without influencing boundaries derived for particle properties –
e.g. increase metal abundances: freely or constrained by spectroscopy

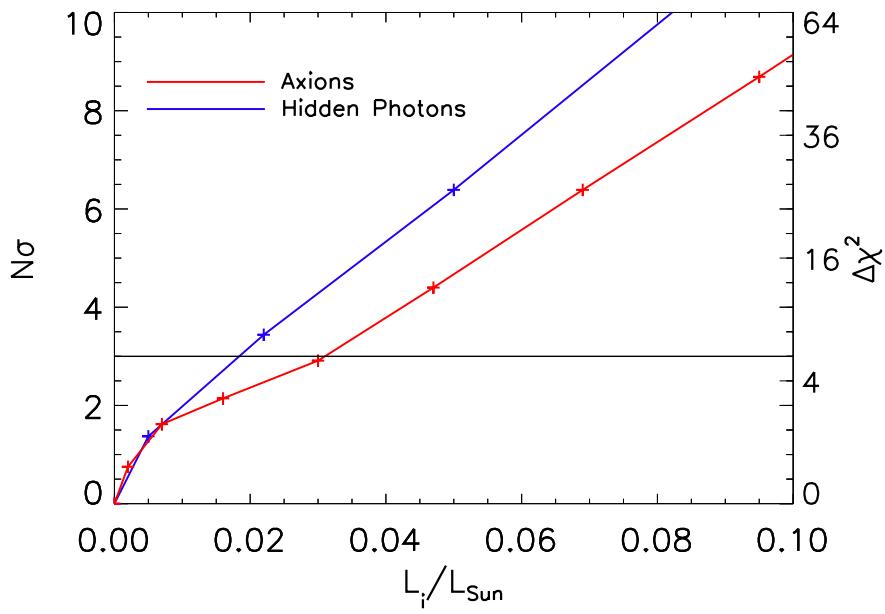
Limits derived are based on forcing solar models (+ dark channel) to fit solar data as best as possible --- > limits then derived from irreducible residuals

HIDDEN PHOTONS



$\chi m < 2$ @ 3- σ C.L. -- improves previous limit by factor 2

COMMENTS ON SOLAR CONSTRAINTS

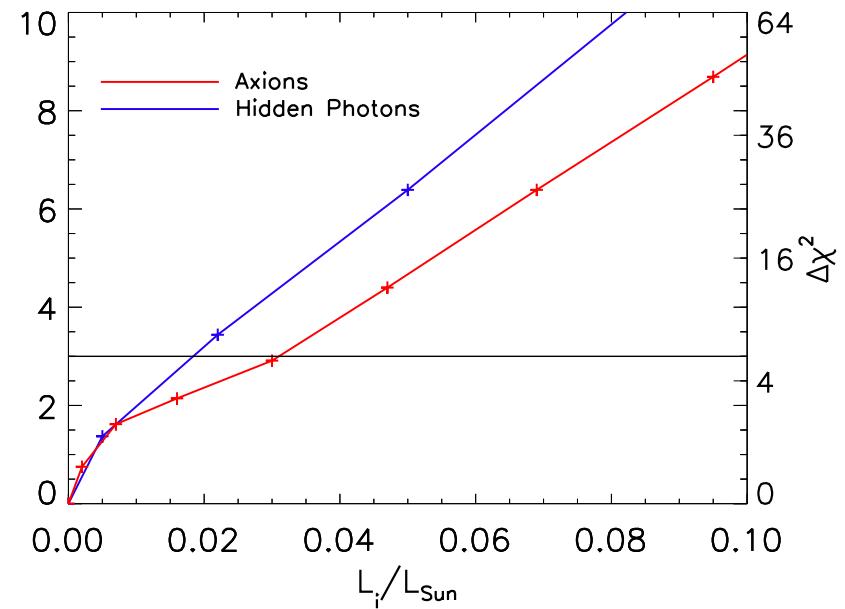


Effective limit in dark channels

$$L_{hp} < 2\% L_{\odot} \quad - \quad L_{\alpha\gamma} < 3\% L_{\odot}$$

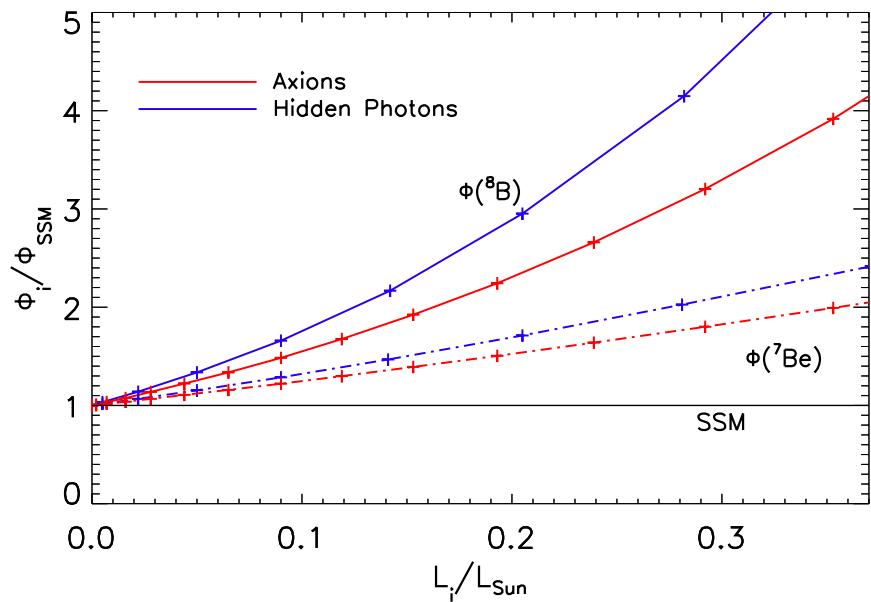
using pp ν flux offers a model independent test – but needs measurement $\sim 1\%$

COMMENTS ON SOLAR CONSTRAINTS



Effective limit in dark channels
 $L_{\text{hp}} < 2\% L_{\odot}$ – $L_{\alpha\gamma} < 3\% L_{\odot}$

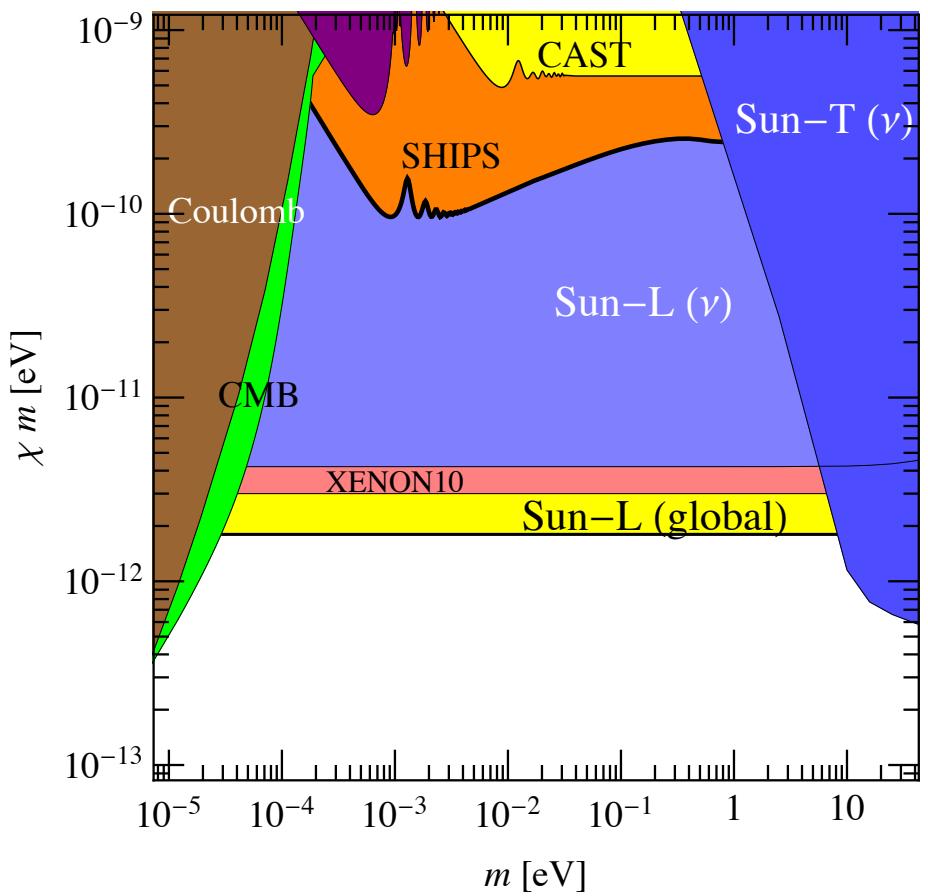
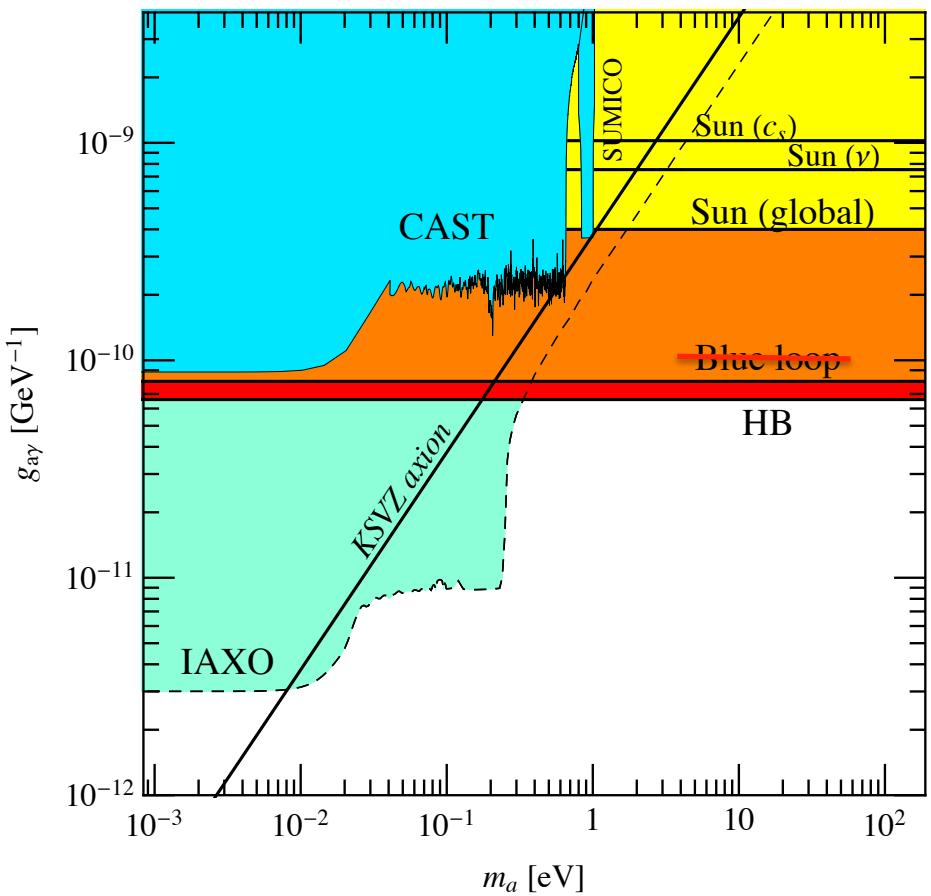
Relations are not universal
 depend on the type of particle



$$\frac{\Phi(^8\text{B})}{\Phi_{\text{SSM}}(^8\text{B})} = \left(\frac{L_x + L_{\odot}}{L_{\odot}} \right)^{\alpha}$$

$$\begin{aligned}\alpha &= 4.4 \text{ (ax)} \\ \alpha &= 5.7 \text{ (hp)}\end{aligned}$$

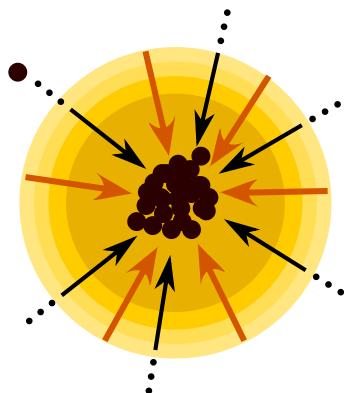
CURRENT LIMITS



SECOND PART --- ADM & SOLAR MODELS

Vincent et al. – arxiv:1411.6626 / 1504.04378

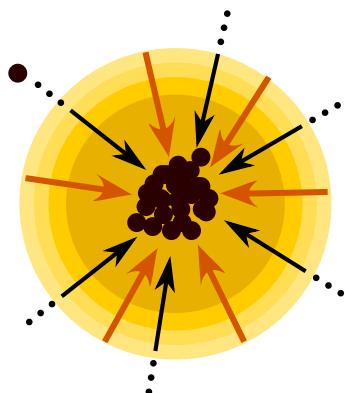
DM-nucleon scattering allows DM collisions with nuclei in the Sun
→ gravitational capture and settling the to solar core



ADM & SOLAR MODELS

Vincent et al. – arxiv:1411.6626 / 1504.04378

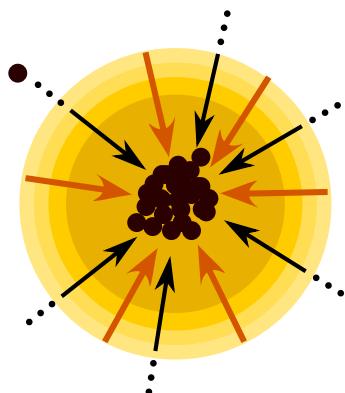
DM-nucleon scattering allows DM collisions with nuclei in the Sun
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→ nuclear scattering inside the Sun



ADM & SOLAR MODELS

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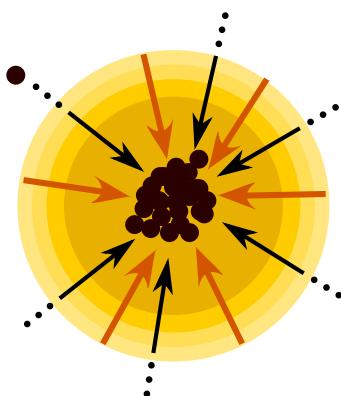
DM-nucleon scattering allows DM collisions with nuclei in the Sun
→ gravitational capture and settling the to solar core
→ nuclear scattering inside the Sun
→ additional energy transport (abundance problem)



ADM & SOLAR MODELS

Vincent et al. – arxiv:1411.6626 / 1504.04378

DM-nucleon scattering allows DM collisions with nuclei in the Sun
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→ additional energy transport
→ modified solar structure



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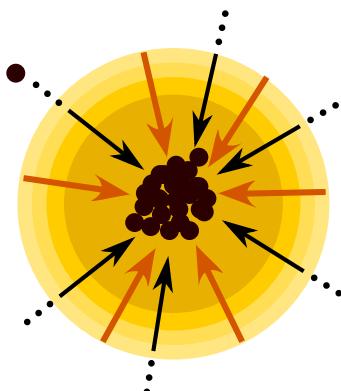
→ 1. observables: (helioseismology)

– sound speed

– oscillation frequencies

– convective zone depth

– surface helium frac.



ADM & SOLAR MODELS

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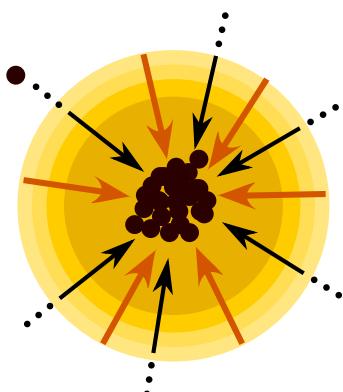
– oscillation frequencies

– convective zone depth

– surface helium frac.

→ 2. different core temperature

– solar neutrino rates



DM-nucleon interaction with q or v_{rel} dependences

$$\sigma = \sigma_0 \left(\frac{q}{q_0} \right)^{2n} \quad \sigma = \sigma_0 \left(\frac{v_{\text{rel}}}{v_0} \right)^{2n}$$

$$\sigma_{N,i} = \frac{m_{\text{nuc}}^2(m_\chi + m_p)^2}{m_p^2(m_\chi + m_{\text{nuc}})^2} \left[\sigma_{\text{SI}} A_i^2 + \sigma_{\text{SD}} \frac{4(J_i + 1)}{3J_i} |\langle S_{p,i} \rangle + \langle S_{n,i} \rangle|^2 \right]$$



SI – A^2 dependence --> enhanced by metals
 sensitive to solar composition
 can be dominant

SD – couples mostly to H

ENERGY TRANSPORT BY ADM

Dark matter number density

$$n_{\chi,\text{LTE}}(r) = n_{\chi,\text{LTE}}(0) \left[\frac{T(r)}{T(0)} \right]^{3/2} \exp \left[- \int_0^r dr' \frac{k_B \alpha(r') \frac{dT(r')}{dr'} + m_\chi \frac{d\phi(r')}{dr'}}{k_B T(r')} \right]$$

Dark matter conductive luminosity

$$L_{\chi,\text{LTE}}(r) = 4\pi r^2 \zeta^{2n}(r) \kappa(r) n_{\chi,\text{LTE}}(r) l_\chi(r) \left[\frac{k_B T(r)}{m_\chi} \right]^{1/2} k_B \frac{dT(r)}{dr}.$$

Energy injection rate

$$\epsilon_{\chi,\text{LTE}}(r) = \frac{1}{4\pi r^2 \rho(r)} \frac{dL_{\chi,\text{LTE}}(r)}{dr}$$

Two limiting behavior: LTE & Isothermal

Intermediate: Knudsen regime $\lambda_\chi \sim r_\chi \rightarrow$ Boltzmann eq.

ENERGY TRANSPORT BY ADM

Dark matter number density

$$n_{\chi,\text{LTE}}(r) = n_{\chi,\text{LTE}}(0) \left[\frac{T(r)}{T(0)} \right]^{3/2} \exp \left[- \int_0^r dr' \frac{k_B \alpha(r') \frac{dT(r')}{dr'} + m_\chi \frac{d\phi(r')}{dr'}}{k_B T(r')} \right]$$

diffusivity

Dark matter conductive luminosity

$$L_{\chi,\text{LTE}}(r) = 4\pi r^2 \zeta^{2n}(r) \kappa(r) n_{\chi,\text{LTE}}(r) l_\chi(r) \left[\frac{k_B T(r)}{m_\chi} \right]^{1/2} k_B \frac{dT(r)}{dr}.$$

Energy injection rate

$$\epsilon_{\chi,\text{LTE}}(r) = \frac{1}{4\pi r^2 \rho(r)} \frac{dL_{\chi,\text{LTE}}(r)}{dr} \quad v_0/v(r) - q_0/q(r)$$

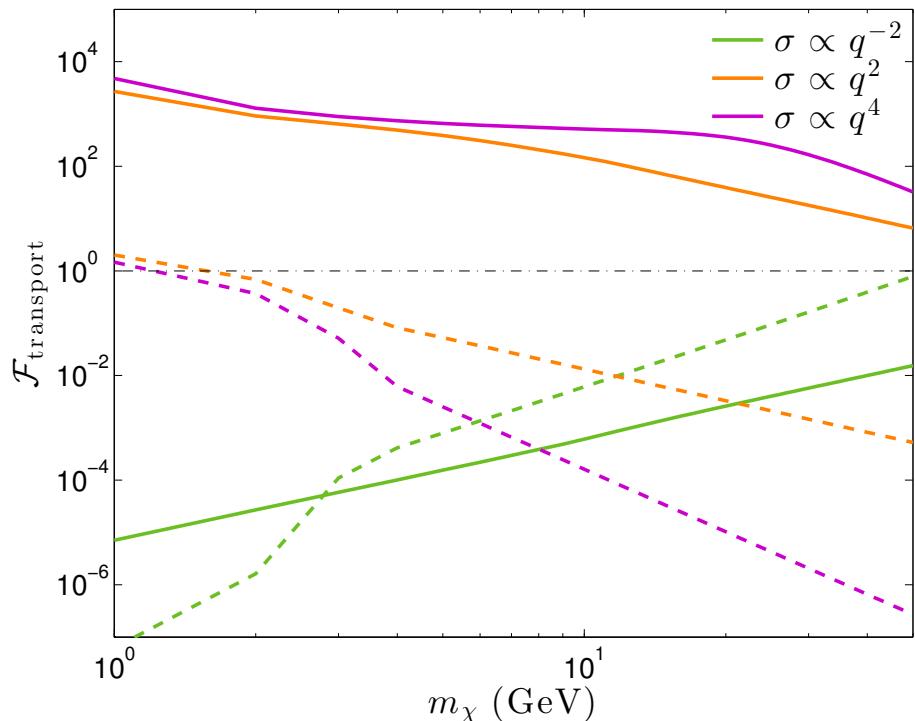
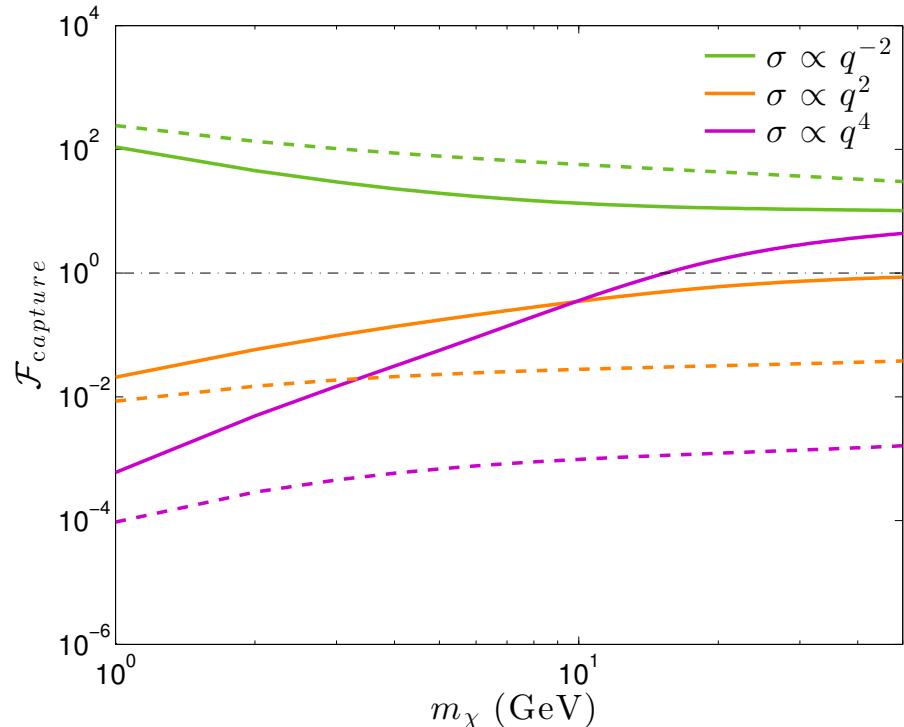
thermal conductivity

Two limiting behavior: LTE & Isothermal

Intermediate: Knudsen regime $\lambda_\chi \sim r_\chi \rightarrow$ Boltzmann eq.

CAPTURE & TRANSPORT

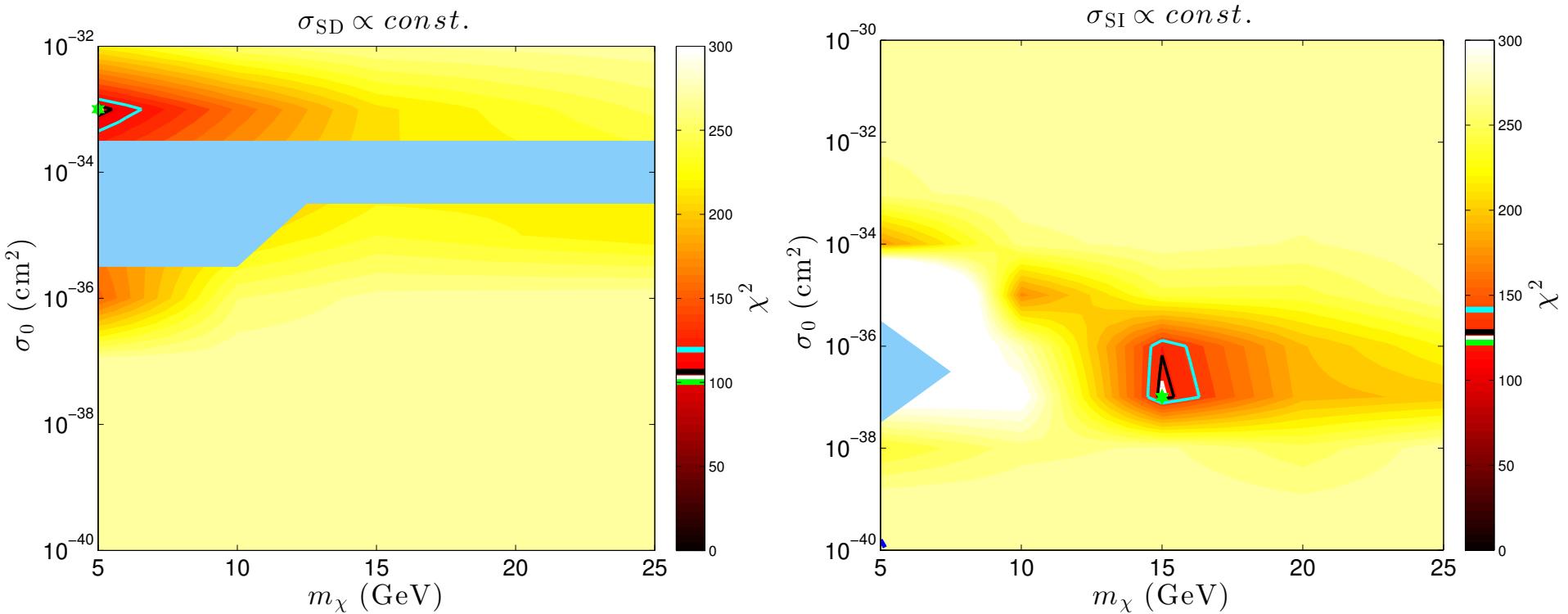
Enhancement/supresion factors



$$\sigma_0 = 10^{-35} \text{ cm}^2$$

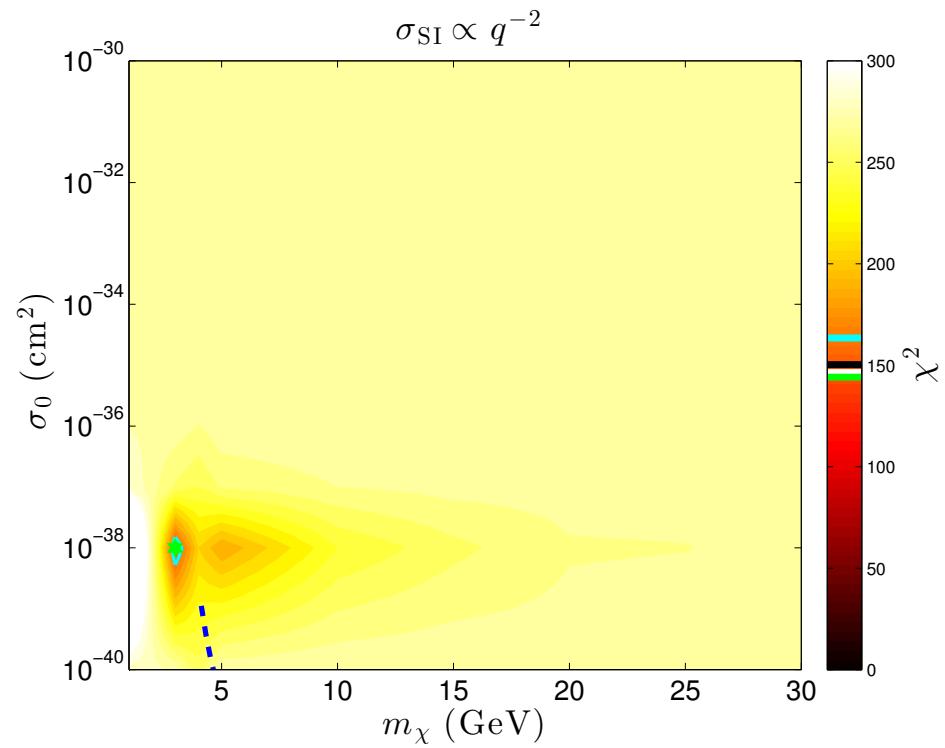
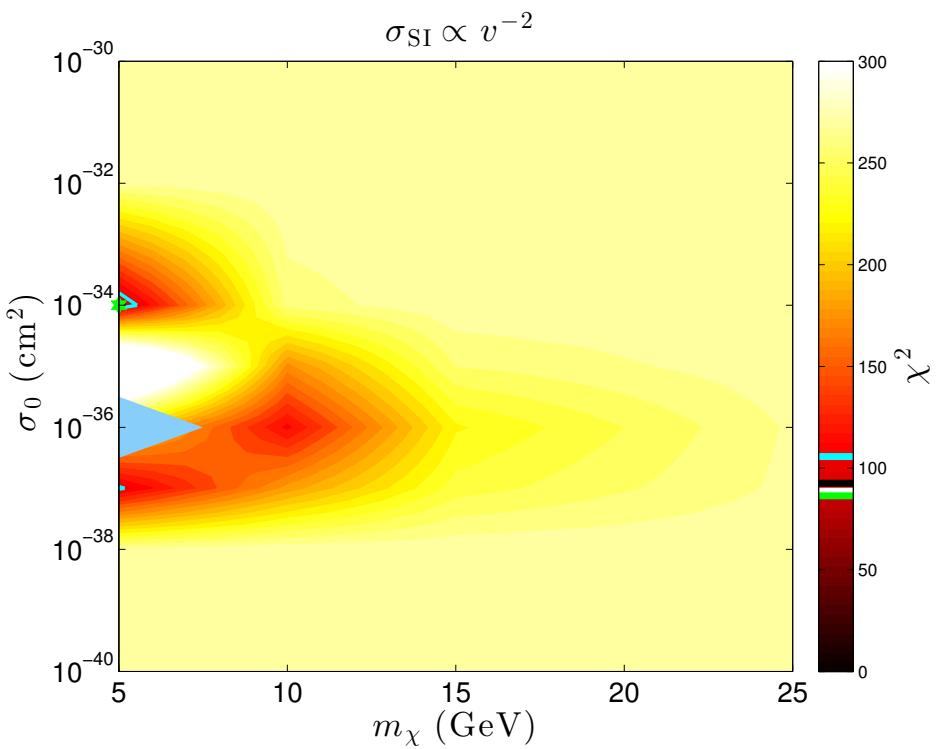
Solid = SI, Dashed = SD

IMPACT ON OBSERVABLES: SI, SD - CONSTANT



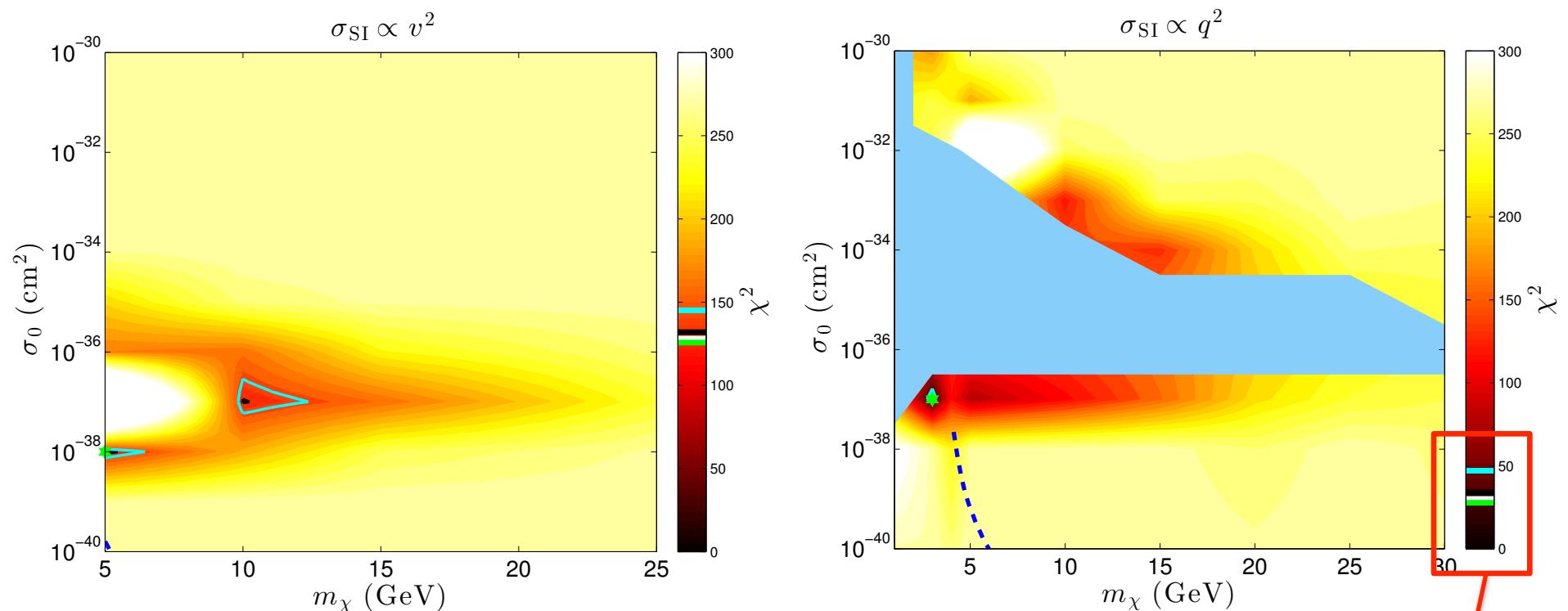
${}^7\text{Be}$ & ${}^8\text{B}$ neutrinos + convective radius + surface helium
Frequency separation ratios r_{02} , r_{13}

IMPACT ON OBSERVABLES: SI, v^{-2} , q^{-2}



${}^7\text{Be}$ & ${}^8\text{B}$ neutrinos + convective radius + surface helium
Frequency separation ratios r_{02} , r_{13}

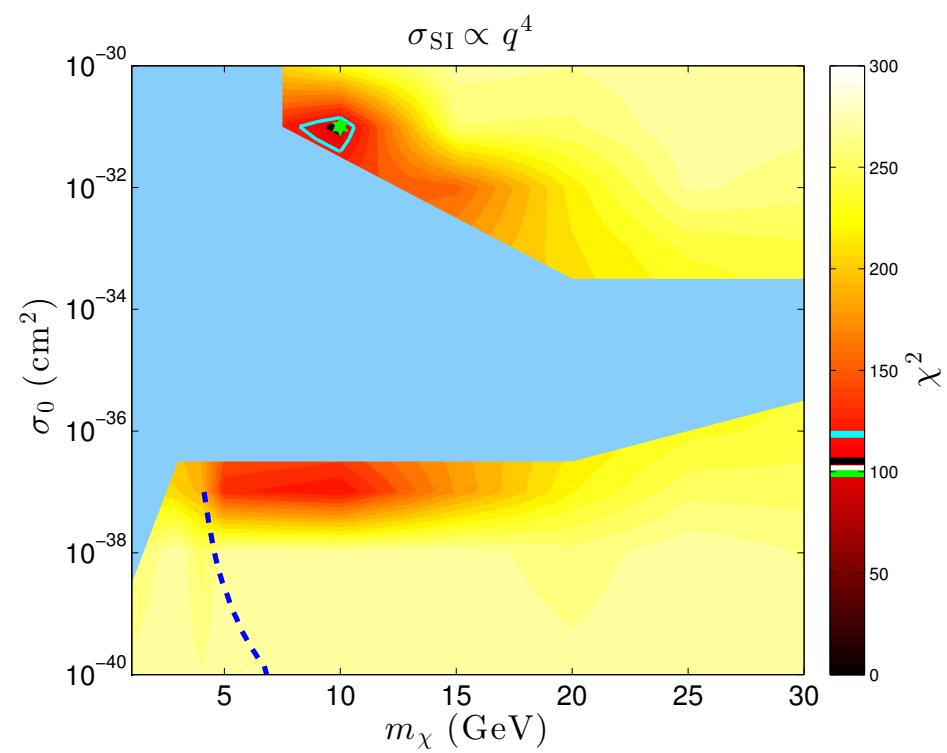
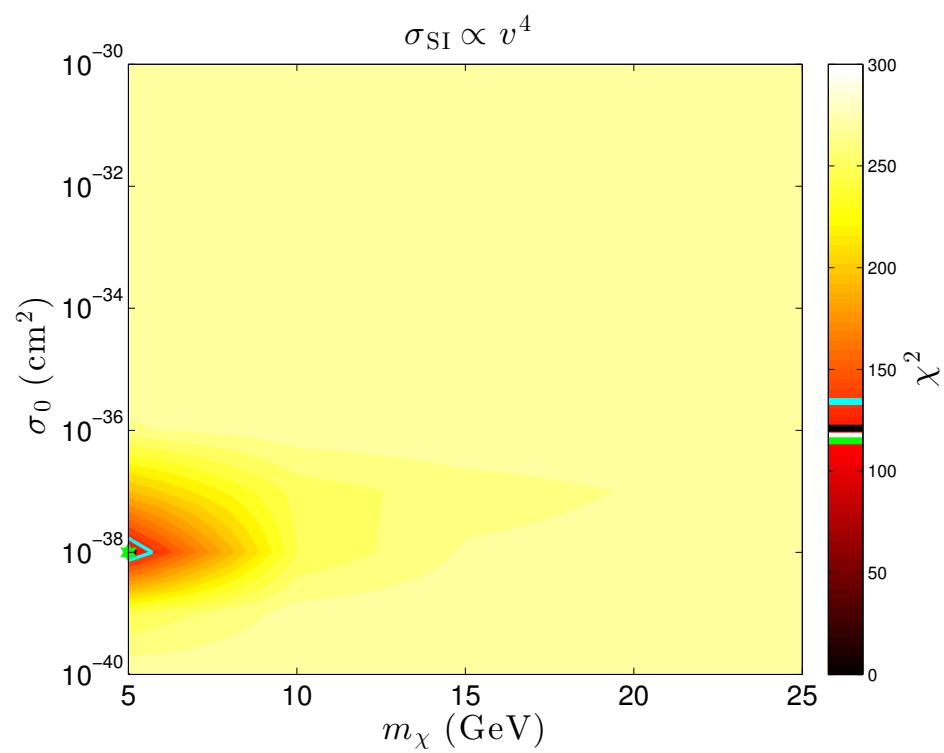
IMPACT ON OBSERVABLES: SI, v^2 , q^2



${}^7\text{Be}$ & ${}^8\text{B}$ neutrinos + convective radius + surface helium
Frequency separation ratios r_{02} , r_{13}

Notice χ^2

IMPACT ON OBSERVABLES: SI, v^4 , q^4

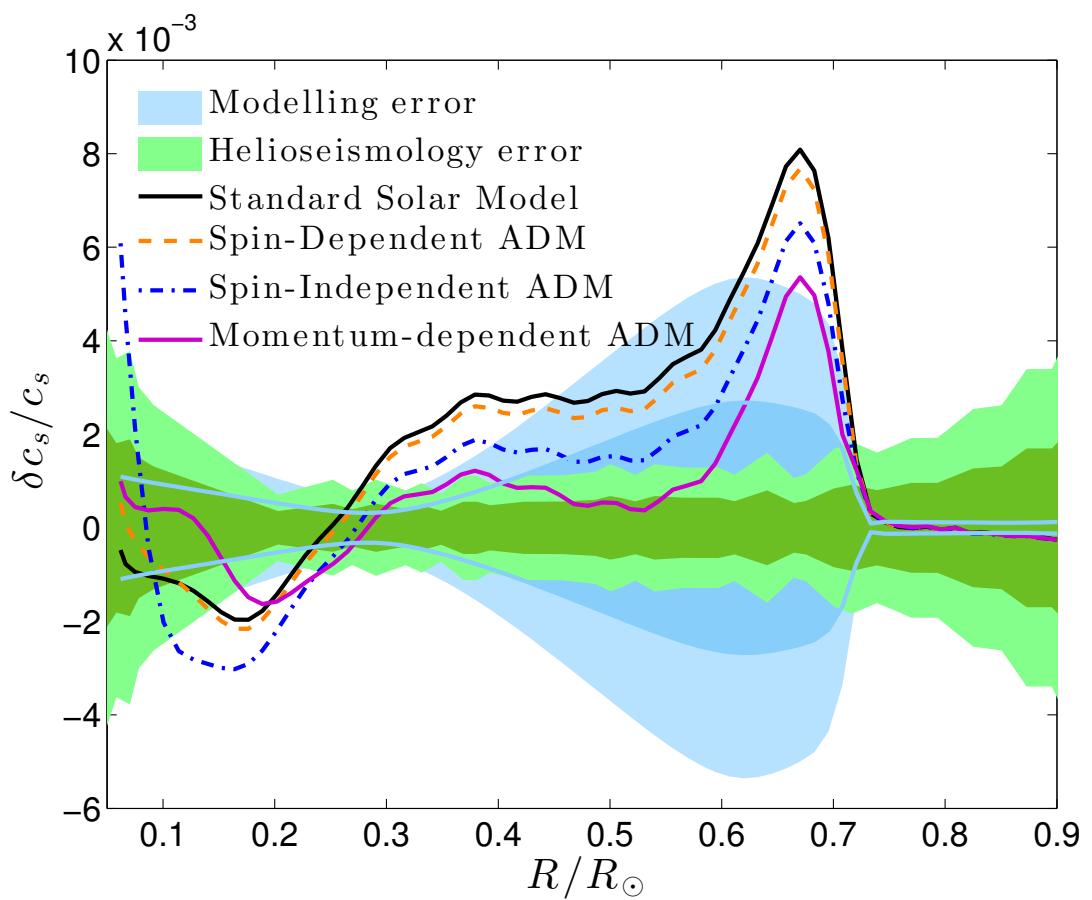


${}^7\text{Be}$ & ${}^8\text{B}$ neutrinos + convective radius + surface helium
Frequency separation ratios r_{02}, r_{13}

BEST MODEL – q^2

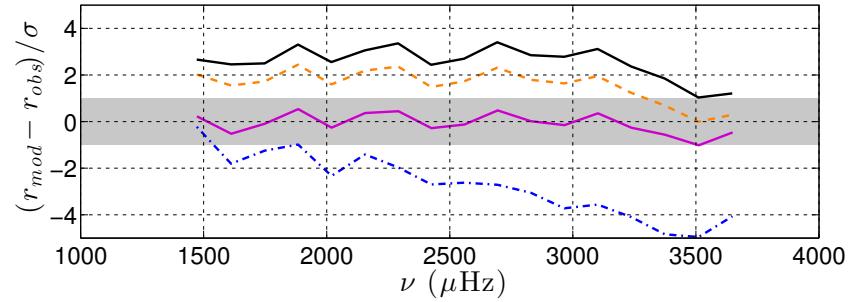
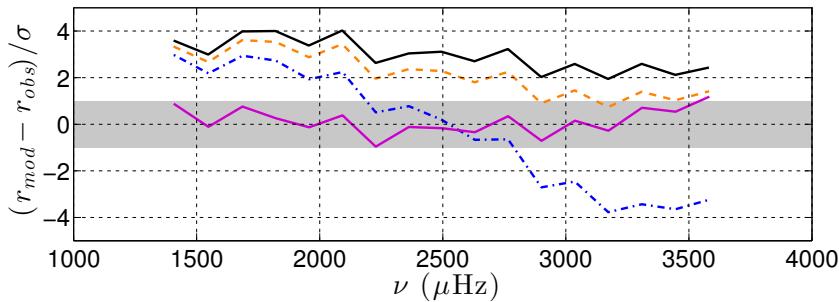
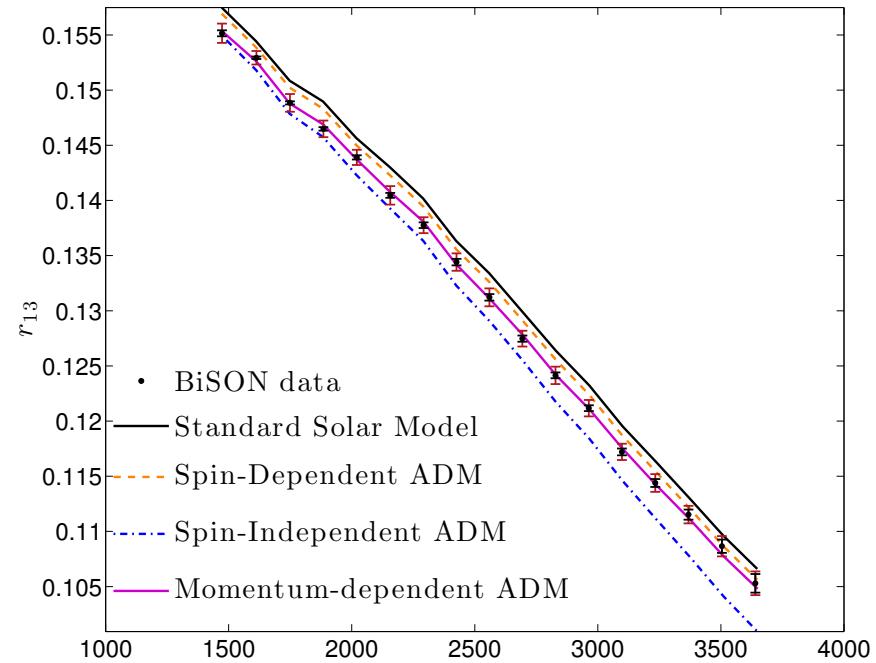
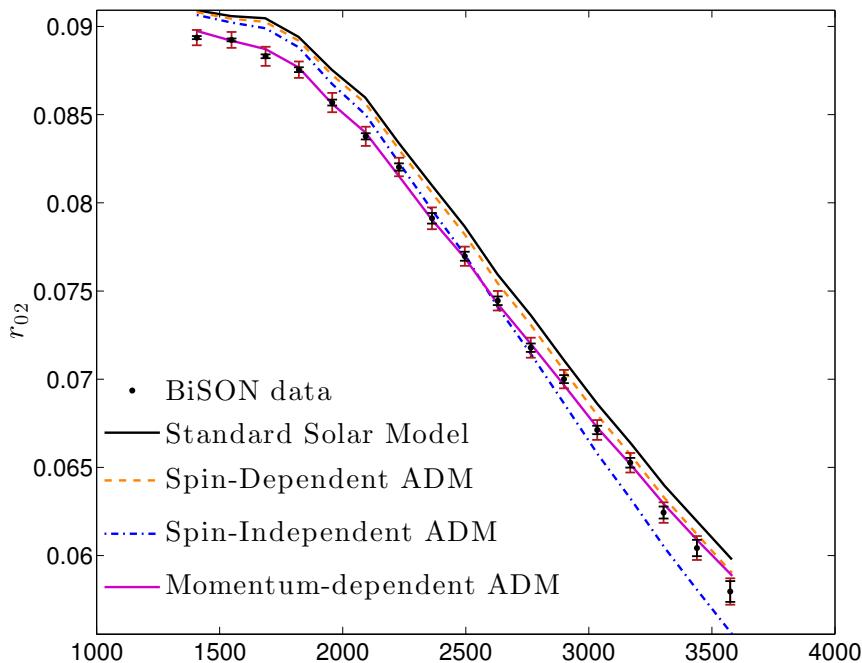
q^2 coupling
 $q_0 = 40 \text{ MeV}$
 $m_\chi = 3 \text{ GeV}$
 $\sigma_0 = 10^{-37} \text{ cm}^2$

Sound speed for best q^2
SI and SD models



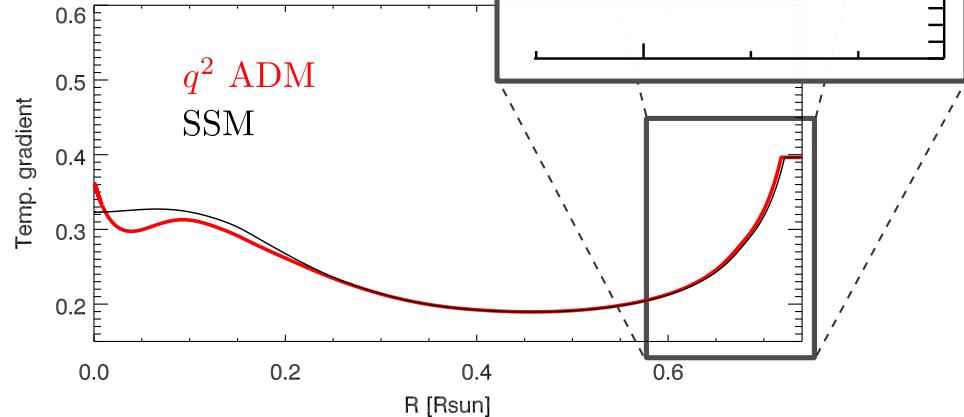
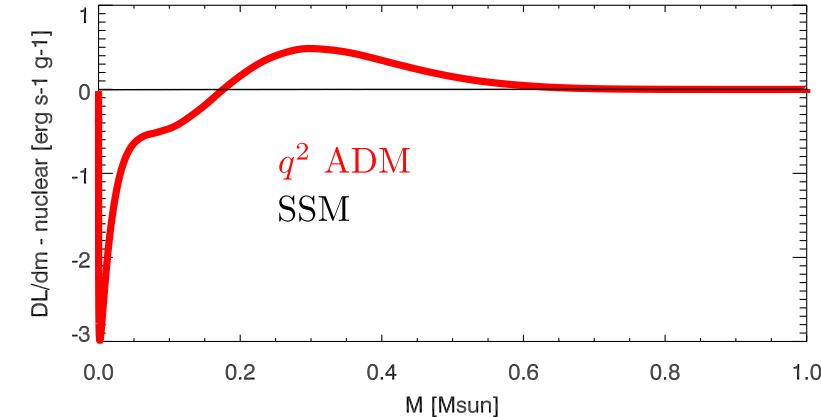
BEST MODEL – q^2

Frequency separation ratios – zooming into the solar core



CHANGES TO SOLAR STRUCTURE

- * Energy extracted from core $M < 0.2 M_{\odot}$
- * Deposited at intermediate range
- * Core change in T-gradient -- \rightarrow sound speed, frequencies, ν -fluxes
- * Smaller T-grad. change at R_{CZ} -- \rightarrow deeper convection



BEST MODEL – q^2

	SSM	SD	SI	q^2 SI	Obs. ^a	σ_{obs}	σ_{model}
$\phi_{\nu}^{8\text{B}}$ ^b	4.95	4.39	4.58	3.78	5.00	3%	14%
$\phi_{\nu}^{7\text{Be}}$ ^c	4.71	4.58	4.62	4.29	4.82	5%	7%
R_{CZ}/R_{\odot}	0.722	0.721	0.721	0.718	0.713	0.001	0.004
Y_s	0.2356	0.2351	0.2353	0.2327	0.2485	0.0034	0.0035
$\chi^2_{8\text{B}}$	0.0	0.9	0.9	4.9			
$\chi^2_{7\text{Be}}$	0.1	0.4	0.4	1.9			
$\chi^2_{R_{\text{CZ}}}$	4.8	3.8	3.8	1.5			
$\chi^2_{Y_s}$	7.0	7.5	7.3	10.5			
$\chi^2_{r_{02}}$	156.6	95.3	105.2	5.6			
$\chi^2_{r_{13}}$	119.3	50.7	67.2	3.1			
χ^2_{total}	287.8	158.5	185.2	27.5			
p	$<10^{-10}$	$<10^{-10}$	$<10^{-10}$	0.845			

PHYSICAL MOTIVATION

Standard models – dominant term constant in DM-quarks interactions

$$\chi\bar{\chi}Q\bar{Q} \rightarrow \sigma_{SI}$$

$$\chi\gamma_\mu\gamma_5\bar{\chi}Q\gamma^\mu\gamma_5\bar{Q} \rightarrow \sigma_{SD}$$

Going beyond: non-zero particle radius, parity violation coupling, etc...

$$(\bar{\chi}\gamma_5\chi)(\bar{Q}Q)$$

$$(\bar{\chi}\chi)(\bar{Q}\gamma_5Q)$$

$$(\bar{\chi}\gamma_5\chi)(\bar{Q}\gamma_5Q)$$

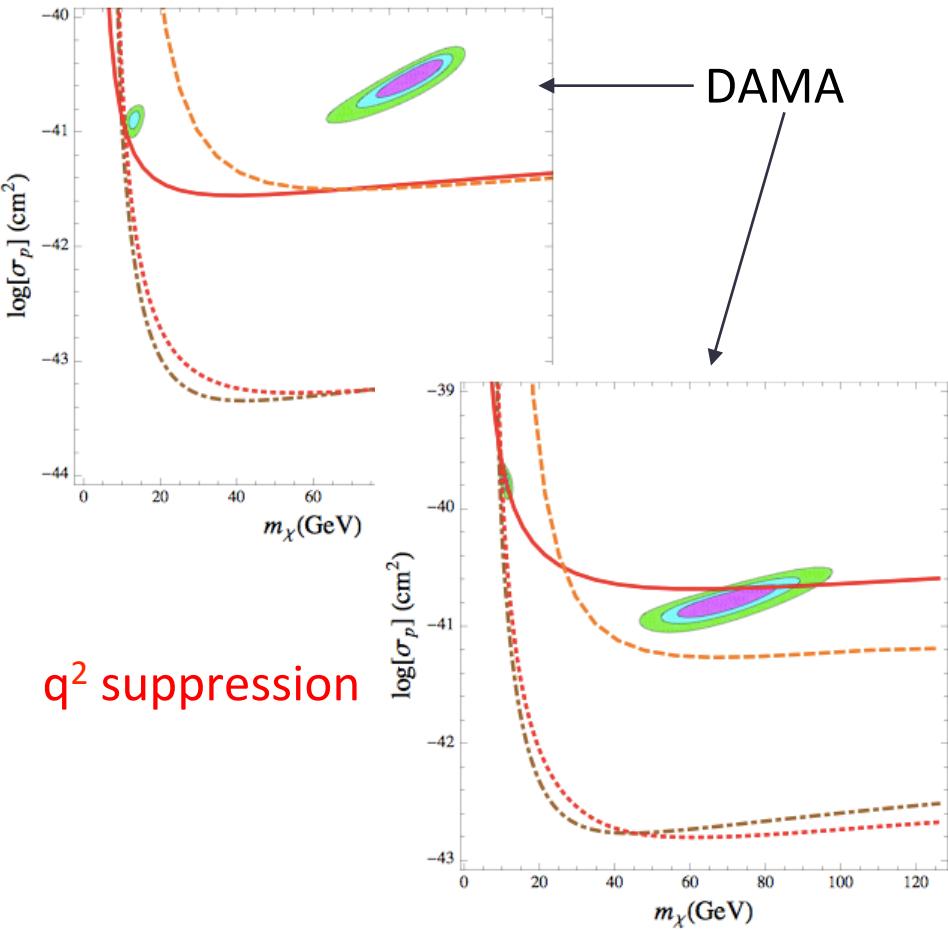
$$(\bar{\chi}\gamma_\mu\gamma_5\chi)(\bar{Q}\gamma^\mu Q)$$

can lead to dependence on the transferred momentum

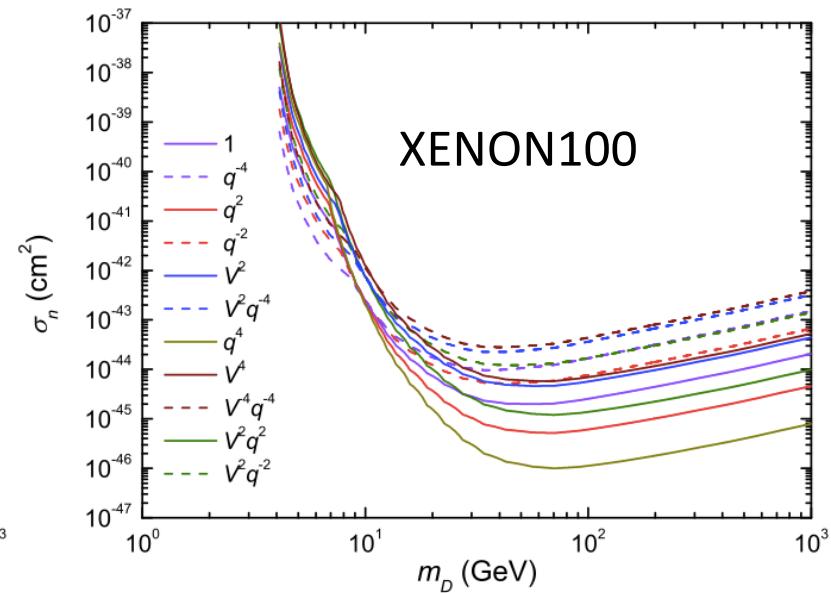
$$\sigma_{\chi q} \propto q^n$$

PHYSICAL MOTIVATION

Standard models – dominant term constant in DM-quarks interactions



Chang et al. 2010



Guo et al. 2014

SUMMARY

- * Seismic and pp-chain νs not sensitive to detail composition
- * Solar abundance problem circumvented in particle studies by letting composition free and input parameters move in constrained way
- * Combining helioseismic and solar νs data
- * Solar limit on axion-photon coupling used as test of method
- * Limit on hidden photon kinetic coupling revisited – x2 lower than previous

- * Momentum exchange q2 ADM models -- > agreement in solar data and models ($\sigma_0 = 10^{-37} \text{ cm}^2$, $m_\chi = 3 \text{ GeV}$)
- * Preferred mass and x-section range not excluded by direct experiment
- * Caveat: evaporation not accounted for (will do)