

Multi-vertex fitQun for pion scattering measurements in WCTE Processes

**Institut de Física
d'Altes Energies**

Table of Contents

- 1 Introduction to fitQun
- 2 Strategy
- 3 Scattering angle and track length study
- 4 Statistics
- 5 Display
- 6 Conclusion



fiTQun

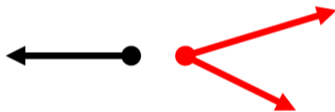
- FiTQun is a maximum likelihood estimation event reconstruction algorithm for WC experiments,
- FiTQun steps:
 - 1 Vertex pre-fitting,
 - 2 Hit clustering,
 - 3 Single-ring reconstruction,
 - 4 Multi-ring reconstruction.
- likelihood, function of the particle parameters specifying initial condition:
 - vertex position x, y, z , time t ,
 - zenith angle and azimuth of the direction θ, ϕ ,
 - momentum p ,
 - Eloss (visible energy), only for pion.

$$L(\mathbf{x}) = \prod_j^{unhit} P_j(unhit|\mathbf{x}) \prod_i^{hit} P_i(hit|\mathbf{x}) f_q(q_i|\mathbf{x}) f_t(t_i|\mathbf{x})$$

Likelihood to maximise → $L(\mathbf{x})$
 Candidate track hypothesis → \mathbf{x}
 Probability of no hit at PMT → $P_j(unhit|\mathbf{x})$
 Probability of hit at PMT → $P_i(hit|\mathbf{x})$
 Hit charge probability density → $f_q(q_i|\mathbf{x})$
 Hit time probability density → $f_t(t_i|\mathbf{x})$

Preparation for Multi-Vertex fitQun

- Normal fitQun only find the pion upstream track →
- Multi-Vertex needed to find pion scattering vertex ↘



1. Reconstruct the first ring
2. Search the second ring assuming the primary vertex.
3. Search the third ring assuming the primary vertex.

1. Reconstruct the first ring
2. Search second vertex
3. Search the second ring assuming the second vertex.
4. Search the third ring assuming the second vertex.

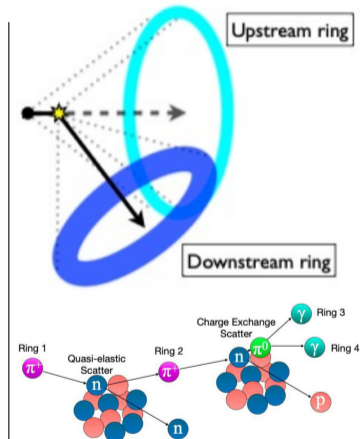


Figure: Pion scattering processes in WCTE

Strategy

- 1 Single Vertex fit ✓
- 2 Multi-ring Separation ✓
- 3 Implementation of Multi-Vertex fit ✓
- 4 Scattering angle and track length study
- 5 Multi-Vertex fit with constraint
- 6 e^-/π Multi-ring study (background)

Interaction processes

- Interactions of π^+ seen through WCSim track list to consider:
 - 1 π^+ scattering,
 - 2 Charge Exchange π^0 ,
 - 3 Double Charge Exchange π^- ,
 - 4 Δ Resonance with one π^+ ,
 - 5 Δ Resonance with two π^\pm ,
 - 6 Δ Resonance with three π^\pm ,
 - 7 Decay μ^\pm ,
 - 8 Other (e^\pm).

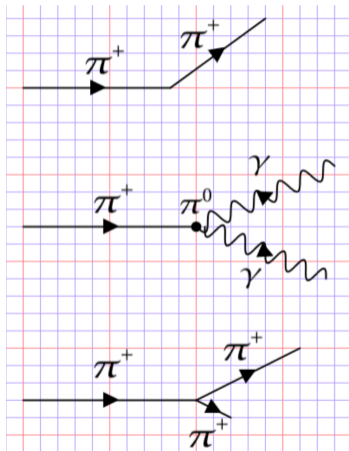


Figure: created from

<https://www.aidansean.com/feynman/>

Interaction processes

π^+ scattering

- $\pi^+ + X \rightarrow \pi^+ + X$

Decay μ^+

- $\pi^+ \rightarrow \mu^+ + \nu_\mu$

Charge Exchange π^0

- $\pi^+ + n \rightarrow \pi^0 + p \rightarrow \gamma + \gamma + p$

Double Charge Exchange π^-

- $\pi^+ + 2n \rightarrow \pi^- + 2p$

Δ Resonance with one π^+

- $\pi^+ + p \rightarrow \pi^+ + \pi^0 + p$
- $\pi^+ + n \rightarrow \Delta^+ \rightarrow \pi^+ + \pi^0 + n$
- $\pi^+ + p \rightarrow \Delta^{++} \rightarrow \pi^+ + \pi^0 + p$

Δ Resonance with two π^\pm

- $\pi^+ + p \rightarrow \pi^+ + \pi^+ + n$
- $\pi^+ + n \rightarrow \pi^+ + \pi^- + p$
- $\pi^+ + {}^{16}\text{O} \rightarrow \pi^+ + \pi^- + \pi^0 + \text{fragments}$
- $\pi^+ + p \rightarrow \Delta^{++} \rightarrow \pi^+ + \pi^+ + n$

Δ Resonance with three π^\pm

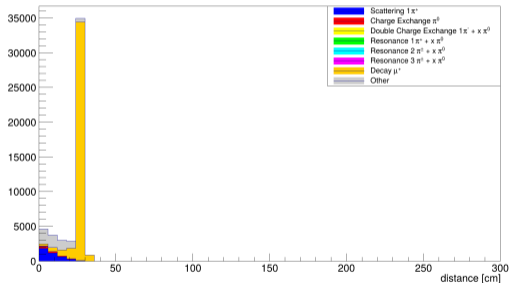
- $\pi^+ + {}^{16}\text{O} \rightarrow \pi^+ + \pi^- + \pi^+ + \text{fragments}$

Other

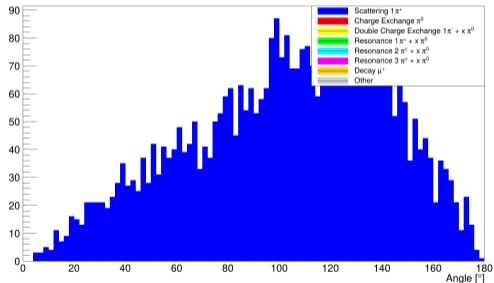
- $\pi^+ \rightarrow e^+ + \nu_e$
- $\pi^+ + {}^{16}\text{O} \rightarrow 2p + 2n + {}^{12}\text{C}$
- $\pi^+ + n \rightarrow p + \gamma$

Length and scattering angle for pions of 200 MeV momentum

Length of 1st π^+ for 200 MeV

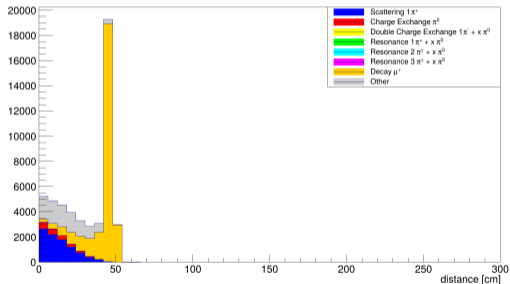


Angle between 1st π^+ track WCSim and 2nds π^+ for 200 MeV

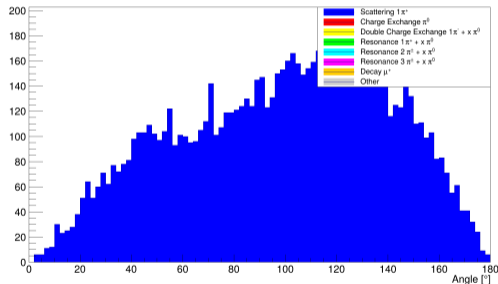


Length and scattering angle for pions of 250 MeV momentum

Length of 1st π^+ for 250 MeV

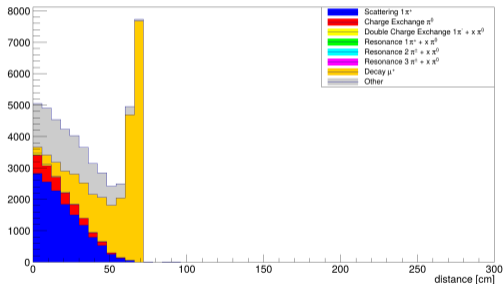


Angle between 1st π^+ track WCSim and 2nd π^+ for 250 MeV

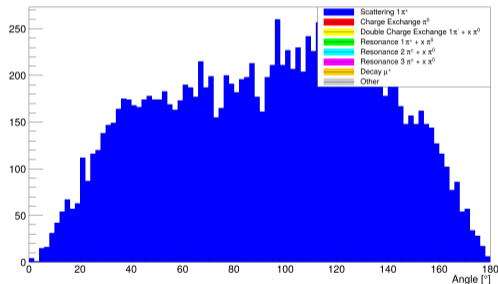


Length and scattering angle for pions of 300 MeV momentum

Length of 1st π^+ for 300 MeV

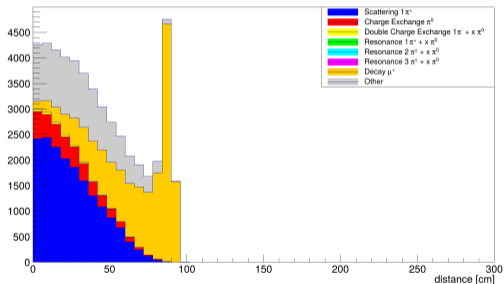


Angle between 1st π^+ track WCSim and 2nd π^+ for 300 MeV

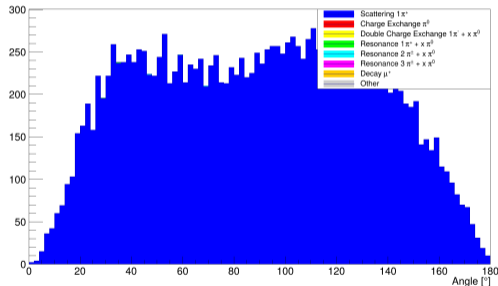


Length and scattering angle for pions of 350 MeV momentum

Length of 1st π^+ for 350 MeV

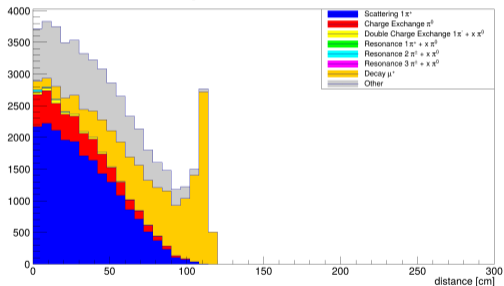


Angle between 1st π^+ track WCSim and 2nds π^+ for 350 MeV

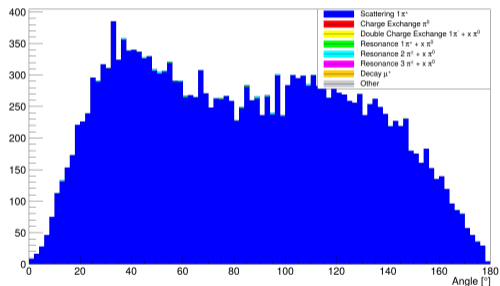


Length and scattering angle for pions of 400 MeV momentum

Length of 1st π^+ for 400 MeV

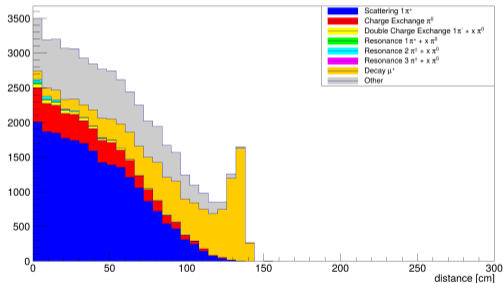


Angle between 1st π^+ track WCSim and 2nd π^+ for 400 MeV

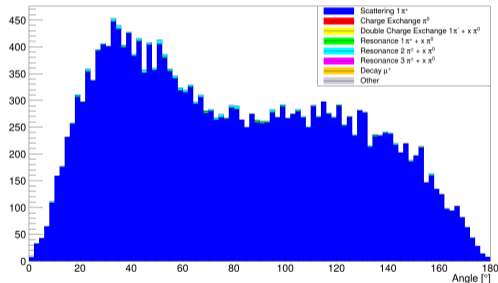


Length and scattering angle for pions of 450 MeV momentum

Length of 1st π^+ for 450 MeV

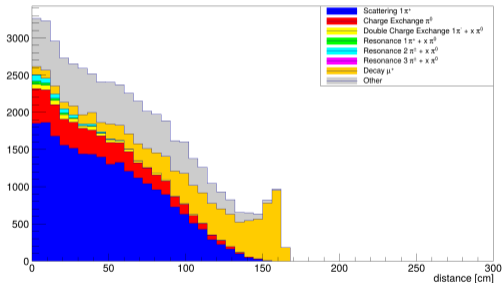


Angle between 1st π^+ track WCSim and 2nd π^+ for 450 MeV

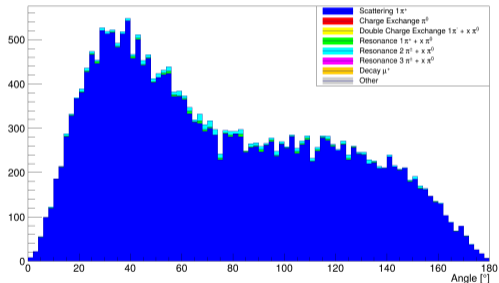


Length and scattering angle for pions of 500 MeV momentum

Length of 1st π^+ for 500 MeV

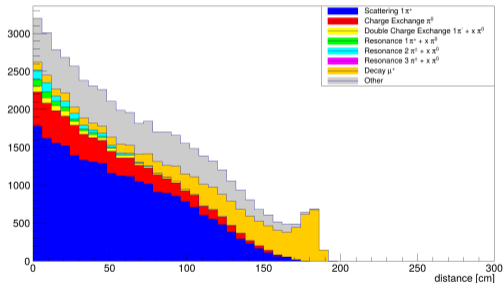


Angle between 1st π^+ track WCSim and 2nd π^+ for 500 MeV

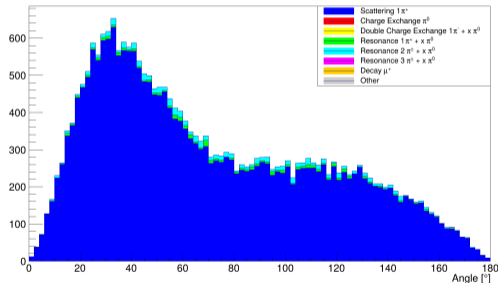


Length and scattering angle for pions of 550 MeV momentum

Length of 1st π^+ for 550 MeV

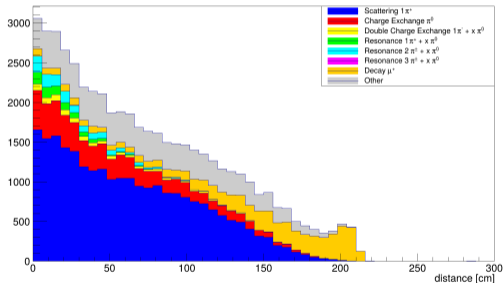


Angle between 1st π^+ track WCSim and 2nds π^+ for 550 MeV

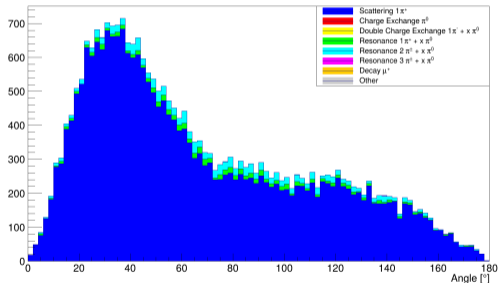


Length and scattering angle for pions of 600 MeV momentum

Length of 1st π^+ for 600 MeV

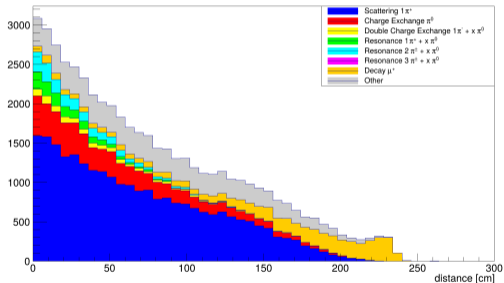


Angle between 1st π^+ track WCSim and 2nd π^+ for 600 MeV

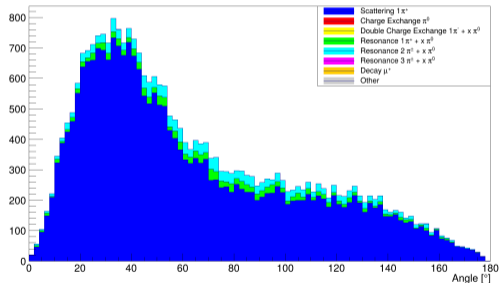


Length and scattering angle for pions of 650 MeV momentum

Length of 1st π^+ for 650 MeV

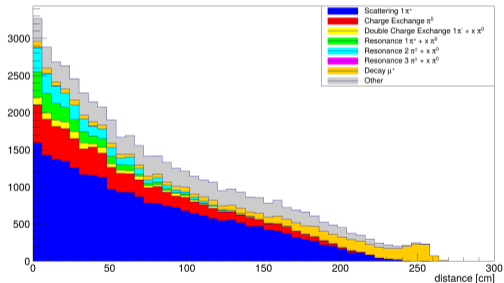


Angle between 1st π^+ track WCSim and 2nds π^+ for 650 MeV

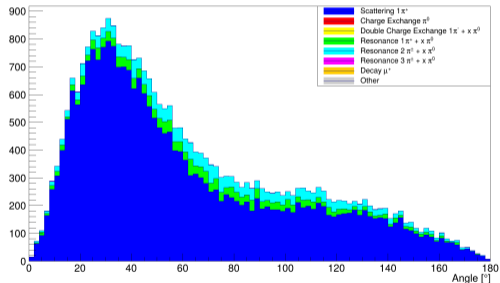


Length and scattering angle for pions of 700 MeV momentum

Length of 1st π^+ for 700 MeV

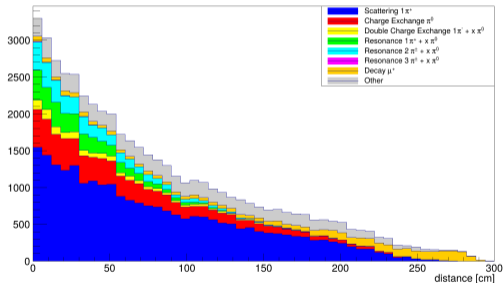


Angle between 1st π^+ track WCSim and 2nds π^+ for 700 MeV

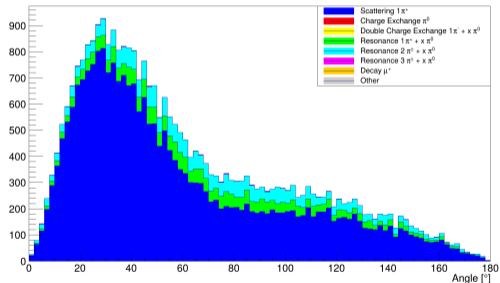


Length and scattering angle for pions of 750 MeV momentum

Length of 1st π^+ for 750 MeV

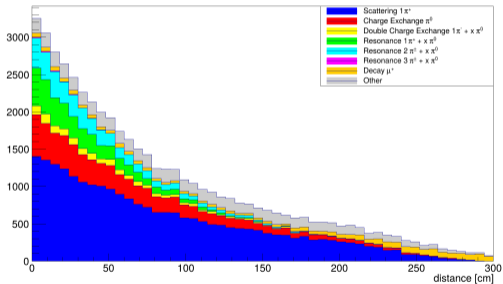


Angle between 1st π^+ track WCSim and 2nds π^+ for 750 MeV

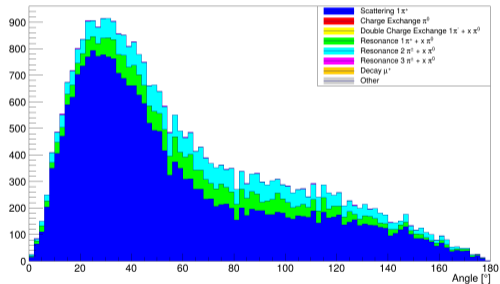


Length and scattering angle for pions of 800 MeV momentum

Length of 1st π^+ for 800 MeV

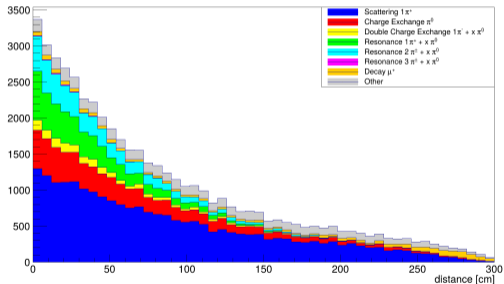


Angle between 1st π^+ track WCSim and 2nds π^+ for 800 MeV

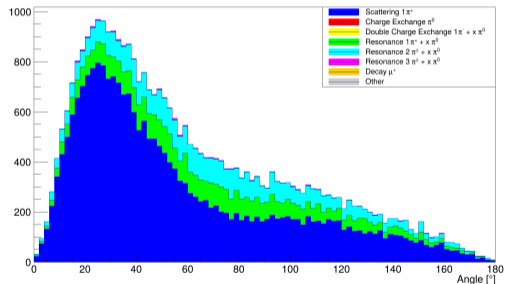


Length and scattering angle for pions of 850 MeV momentum

Length of 1st π^+ for 850 MeV

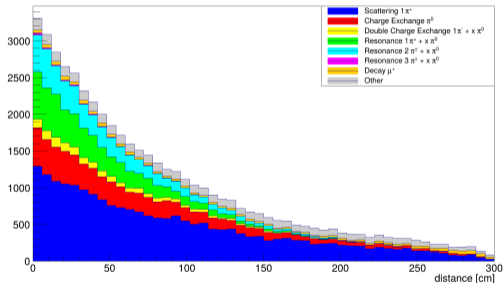


Angle between 1st π^+ track WCSim and 2nd π^+ for 850 MeV

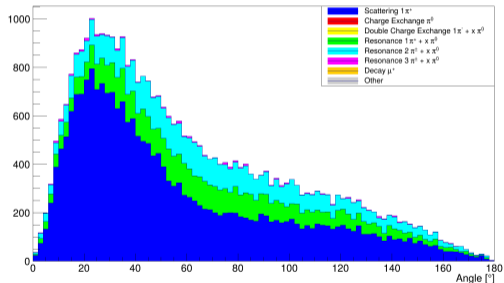


Length and scattering angle for pions of 900 MeV momentum

Length of 1st π^+ for 900 MeV

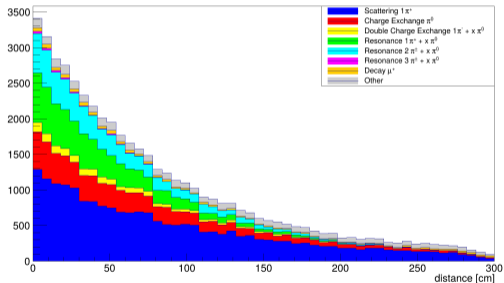


Angle between 1st π^+ track WCSim and 2nds π^+ for 900 MeV

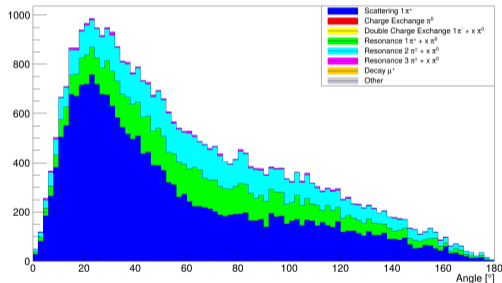


Length and scattering angle for pions of 950 MeV momentum

Length of 1st π^+ for 950 MeV

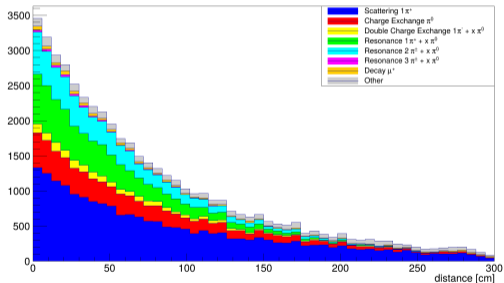


Angle between 1st π^+ track WCSim and 2nds π^+ for 950 MeV

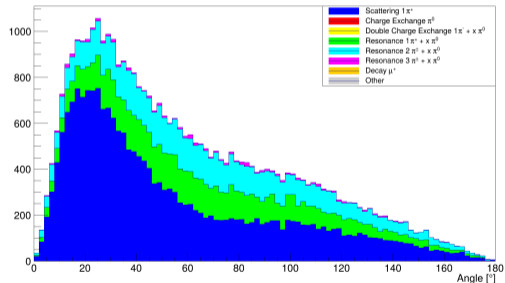


Length and scattering angle for pions of 1000 MeV momentum

Length of 1st π^+ for 1000 MeV



Angle between 1st π^+ track WCSim and 2^{nds} π^+ for 1000 MeV



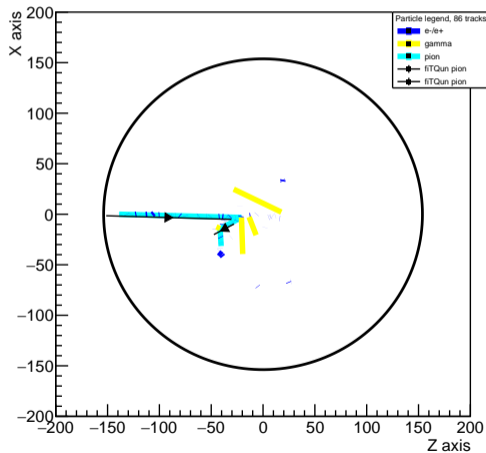
Interaction process statistics

| Momentum MeV | Scattering | Charge Exchange pi0 | Double CE pi- | resonance 1pi | resonance 2pi | resonance 3pi | decay mu+ | Other | total |
|--------------|------------|---------------------|---------------|---------------|---------------|---------------|-----------|-------|-------|
| 200 | 3885 | 781 | 0 | 26 | 0 | 0 | 38447 | 6861 | 50000 |
| 250 | 9123 | 1777 | 0 | 69 | 0 | 0 | 28893 | 10138 | 50000 |
| 300 | 13892 | 2801 | 0 | 155 | 1 | 0 | 22083 | 11068 | 50000 |
| 350 | 17341 | 3550 | 2 | 257 | 4 | 0 | 17284 | 11562 | 50000 |
| 400 | 20427 | 4244 | 16 | 357 | 49 | 0 | 13509 | 11398 | 50000 |
| 450 | 22340 | 4696 | 61 | 458 | 157 | 0 | 10973 | 11315 | 50000 |
| 500 | 23731 | 5250 | 169 | 586 | 379 | 0 | 8804 | 11081 | 50000 |
| 550 | 24368 | 5796 | 394 | 748 | 673 | 0 | 7321 | 10700 | 50000 |
| 600 | 24924 | 6172 | 762 | 810 | 1193 | 2 | 6003 | 10134 | 50000 |
| 650 | 25263 | 6504 | 1267 | 946 | 1669 | 1 | 5120 | 9230 | 50000 |
| 700 | 25219 | 6975 | 1997 | 1155 | 2312 | 12 | 4117 | 8213 | 50000 |
| 750 | 24766 | 7162 | 2999 | 1332 | 3048 | 26 | 3397 | 7270 | 50000 |
| 800 | 24427 | 7437 | 3884 | 1464 | 3684 | 54 | 2805 | 6245 | 50000 |
| 850 | 23186 | 7518 | 5173 | 1608 | 4567 | 83 | 2443 | 5422 | 50000 |
| 900 | 22198 | 7757 | 6137 | 1656 | 5361 | 149 | 2003 | 4739 | 50000 |
| 950 | 21421 | 7765 | 7179 | 1698 | 5962 | 201 | 1706 | 4068 | 50000 |
| 1000 | 21188 | 7504 | 7851 | 1744 | 6461 | 273 | 1476 | 3503 | 50000 |

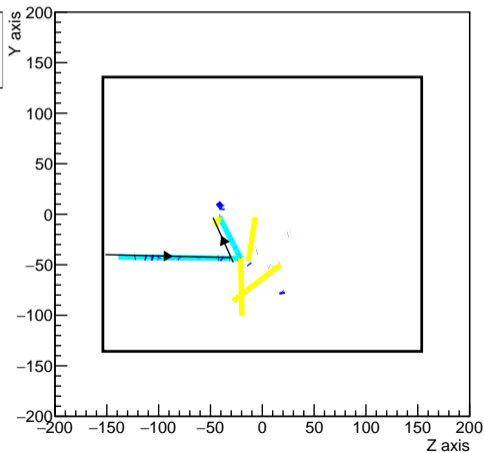
Process pi+Inelastic : 430357

Track display, good event

WC detector, ev #4 from pi+ (1000.00 MeV)

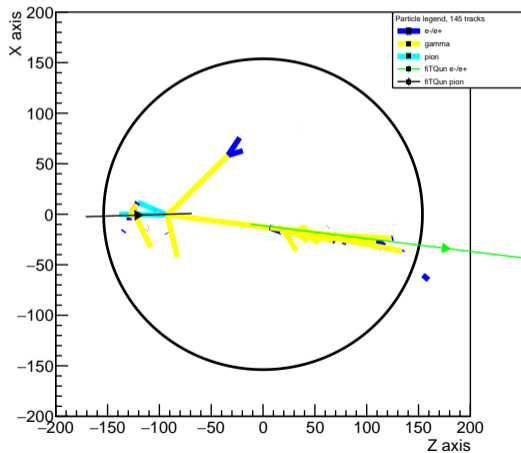


WC detector, ev #4 from pi+ (1000.00 MeV)

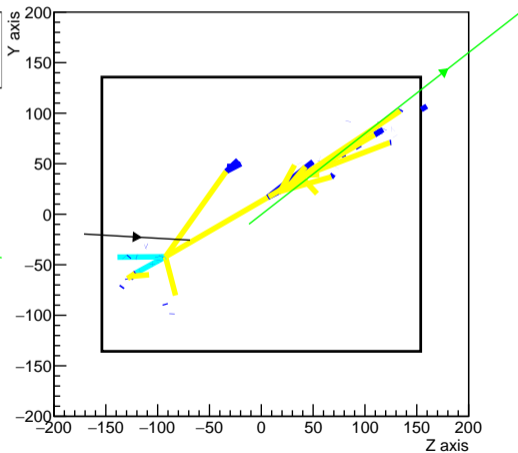


Track display, presence of π^0

WC detector, ev #0 from pi+ (1000.00 MeV)

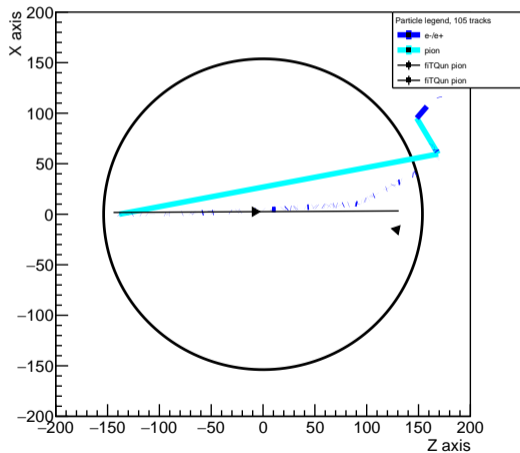


WC detector, ev #0 from pi+ (1000.00 MeV)

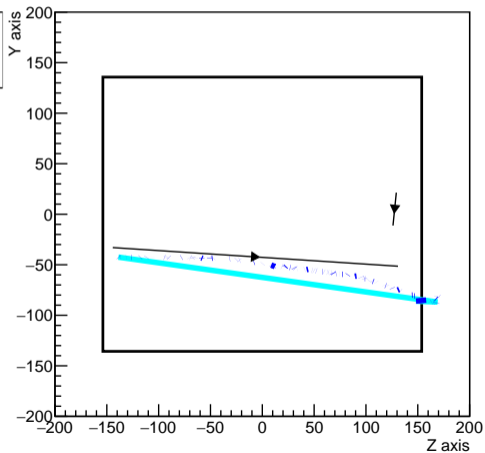


Track display, WCSim lack of information

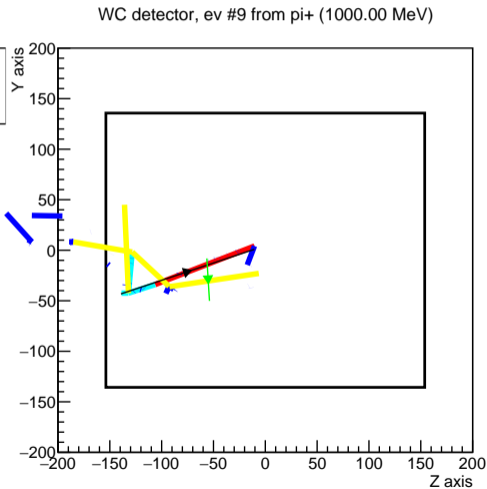
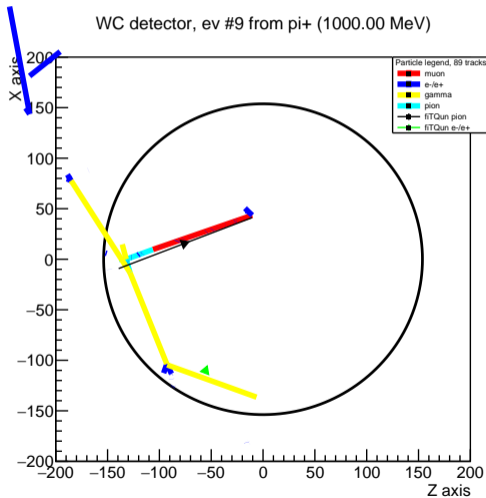
WC detector, ev #6 from pi+ (1000.00 MeV)



WC detector, ev #6 from pi+ (1000.00 MeV)

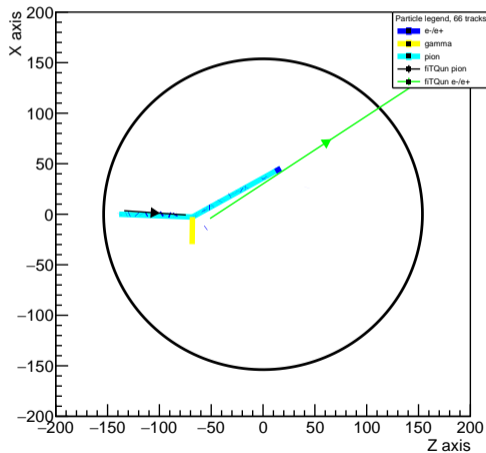


Track display, in-flight decay

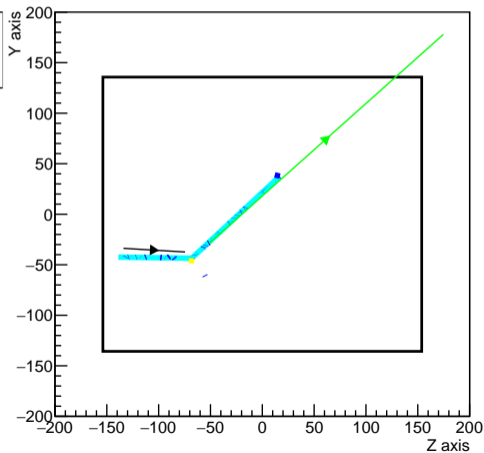


Track display, needs better MR tuning

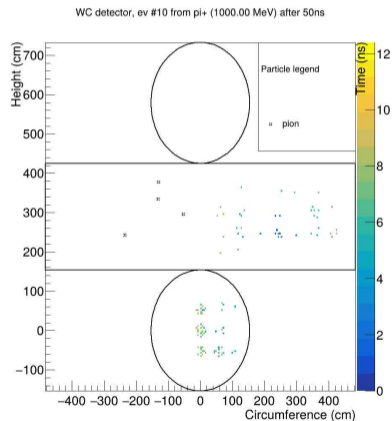
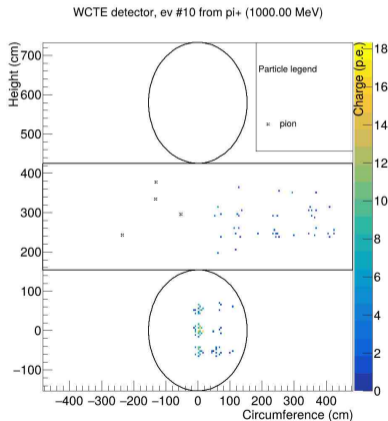
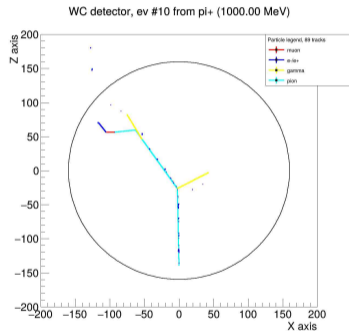
WC detector, ev #642920 from pi+ (750.00 MeV)



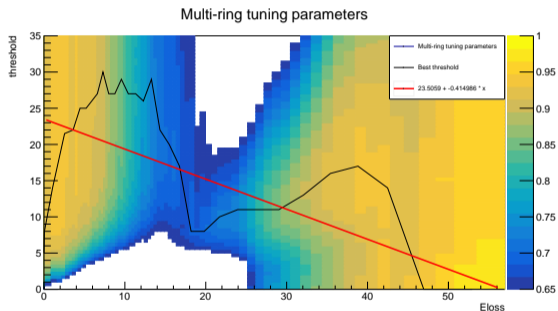
WC detector, ev #642920 from pi+ (750.00 MeV)



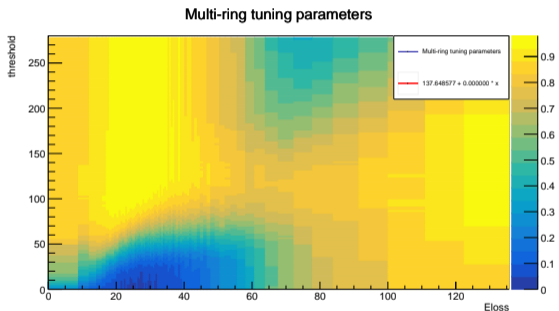
Track display, only few PMT hits



Multi-ring tuning with Multi-Vertex



- Muon at center, all directions
- 88.7% separation



- One muon at beam position, second 1m away
- 92.5% separation

Conclusion

- A lot of unexpected interactions with π^+ ,
- Couldn't find yet a good relation between fitQun reconstruction and the length or angle of WCSim tracks,
- It looks like fitQun try to perfect the reconstruction by using small electron track at times,
- CherenkovDigiHit sometimes does not go beyond few ns,
- I will add constraints on fitQun first track (position and direction),
- I am redoing the MR tuning with Multi-Vertex (new threshold found for 1/2 rings), with exponential distribution for second muon position.