

Multi-vertex fiTQun for pion scattering measurements in WCTE

Adding constraints

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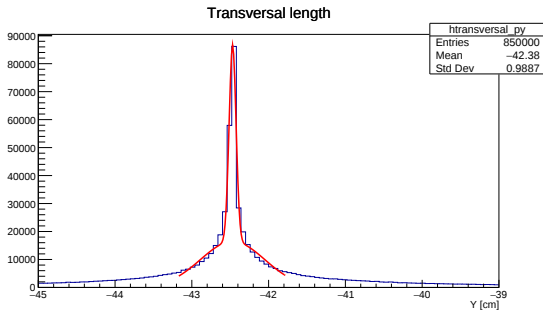
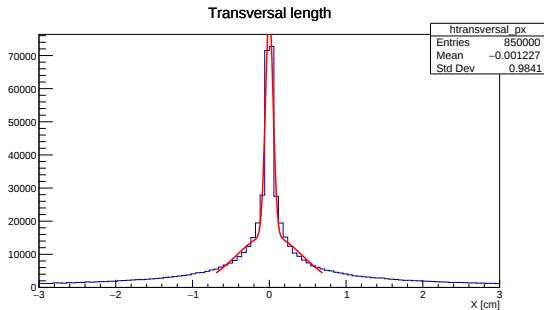
Strategy

- 1 Single Vertex fit ✓
- 2 Multi-ring Separation ✓
- 3 Implementation of Multi-Vertex fit ✓
- 4 Multi-Vertex fit with constraints ✓
- 5 Redo multi-ring tuning
- 6 Scattering angle and track length study
- 7 e^-/π Multi-ring study (background)

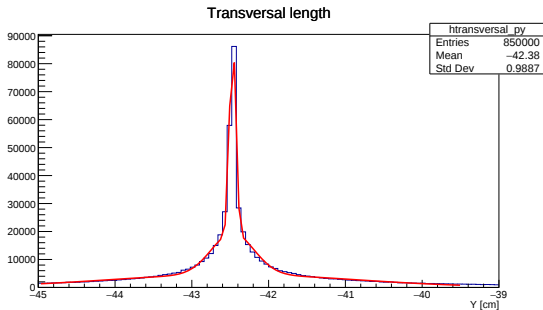
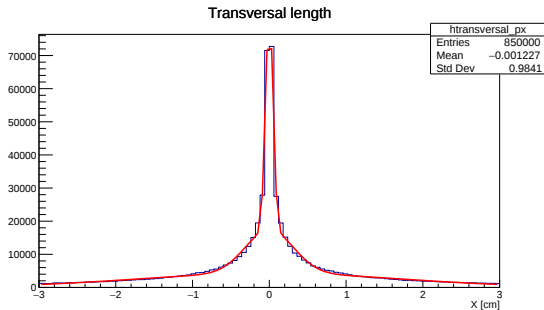
Adding constraints

- 2+ rings working as intended,
- 1 ring was not properly constrained, position was changed after fit → solved, production in process for tuning,
- Updated WCSim to version 1.12.21,
- fiTQun constraints:
 - First vertex, fix z at beam pipe, x and y in a 2.5 cm radius,
 - Second vertex, x and y in a 2.5 cm radius, and z from beam pipe to wall.
- New proposition to constrain the position in transversal plane of the beam for 1st and 2nd vertex using a PDF based on the first interaction point of pions.

First pion interaction point with a two Gaussian fit



First pion interaction point with a three Gaussian fit



Adding to the negative log likelihood

$$L(\mathbf{x}) = \prod_j^{unhit} P_j(unhit|\mathbf{x}) \prod_i^{hit} P_i(hit|\mathbf{x}) f_q(q_i|\mathbf{x}) f_t(t_i|\mathbf{x})$$

Likelihood to maximise (points to $L(\mathbf{x})$)

Candidate track hypothesis (points to $\mathbf{x}$)

Probability of no hit at PMT (points to $P_j(unhit|\mathbf{x})$)

Probability of hit at PMT (points to $P_i(hit|\mathbf{x})$)

Hit charge probability density (points to $f_q(q_i|\mathbf{x})$)

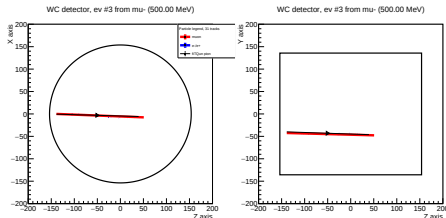
Hit time probability density (points to $f_t(t_i|\mathbf{x})$)

- In practice, fitQun is adding each component as negative log,

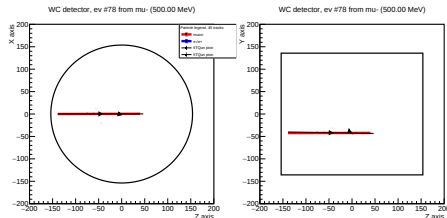
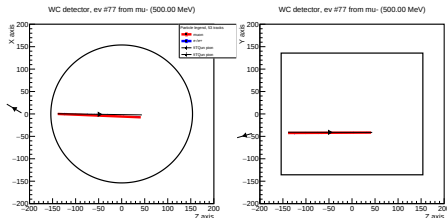
- Adding : $\text{Constant} \times -\log \sum_{i=1}^{2or3} \frac{A_i}{\sum_{j=1}^{2or3} A_j} G(x; \mu, \sigma_i)$

- The constant is there to control how much influence this restraint on the position should have.

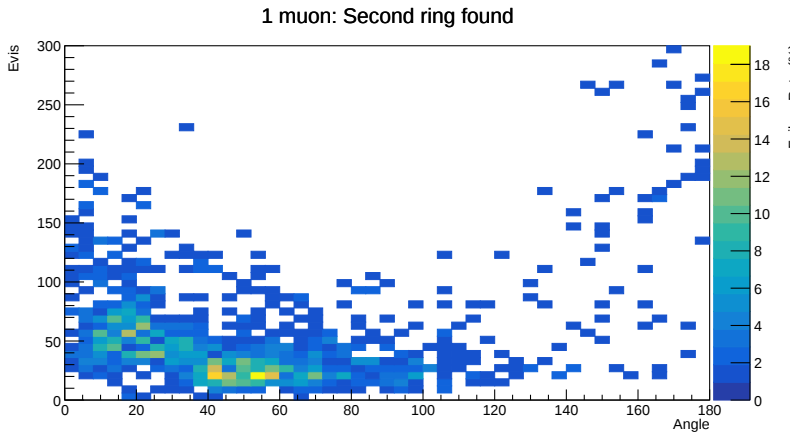
1 muon ring



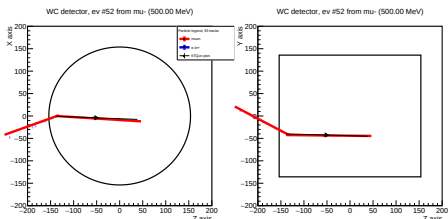
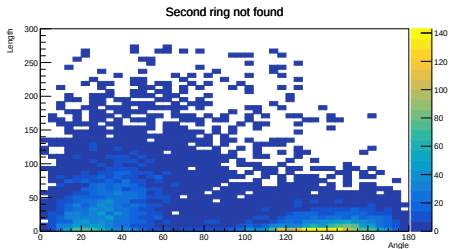
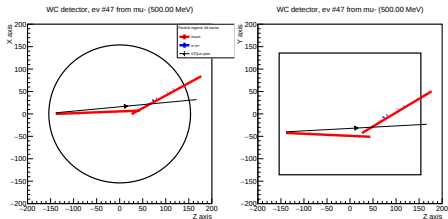
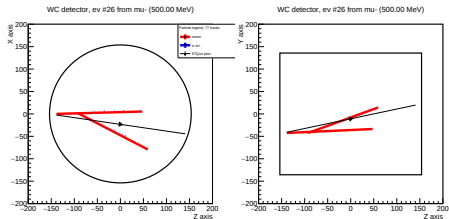
- Applied MR tuning, with 88.4% separation of 1/2 rings,
- When finding 1 ring: good
- Can sometimes find second ring outside (now added z constraints),
- Other times find a small ring.



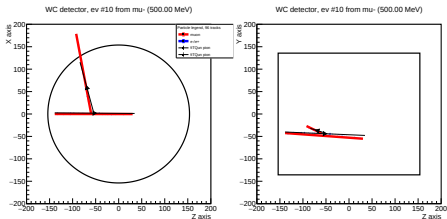
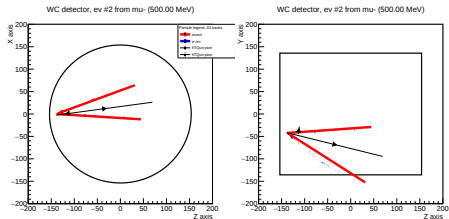
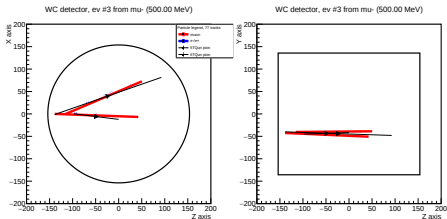
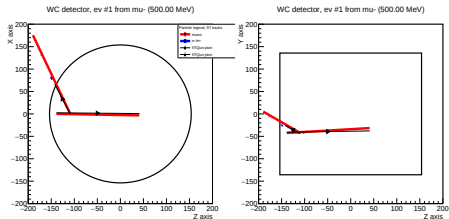
Visible energy of second ring and fiTQun angle between both rings



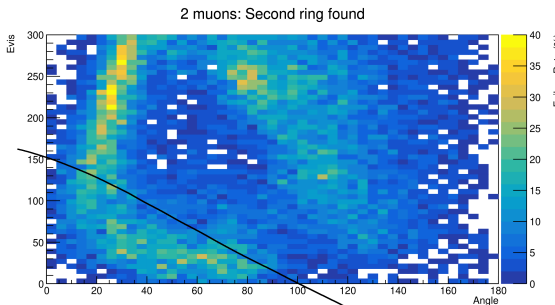
2 muon rings, rec. as one



2 muon rings, rec. as two



Visible energy of second ring and fiTQun angle between both rings for 2 muons



If cut applied on visible energy and angle between rings:

- 1 ring sample is improved (need to study statistics),
- 2 rings sample in the concerned region seems to be badly reconstructed, seeing the angular resolution.

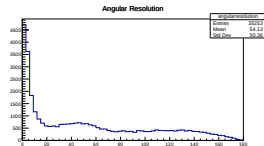


Figure: Above the line

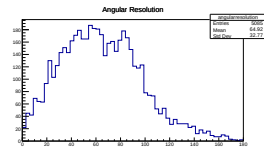


Figure: Below the line

Conclusion

- Solved the 1 ring constraints, now started with both vertices constrained,
- New idea to apply a PDF of the position to help the fit to focus on the desired region without having to block the fit range,
- Still need to consider the constant and how to tune that?
- Need to think of some cuts in order to improve the quality of the selection.