

The Axiflavor

A Minimal Axion Model from Flavor



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**based on arXiv: 1612.08040 with
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Outline

- **The Axion**



- **The Flavon**



- **The Axiflavin**



The Axion



The QCD θ -term

Gauge and Lorentz invariance allow QCD θ -term

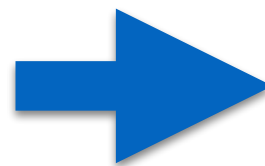
$$\mathcal{L} = \theta \frac{\alpha_s}{8\pi} G_a^{\mu\nu} \tilde{G}_{a,\mu\nu} = \theta \frac{\alpha_s}{16\pi} \epsilon_{\mu\nu\rho\sigma} G_a^{\mu\nu} G_a^{\rho\sigma}$$

Shifts under anomalous axial U(1) transformations that control complex phases in quark masses

for 1 quark generation:

$$\mathcal{L}_{\text{mass}} = -\bar{u}_L M_u u_R + \text{h.c.}$$

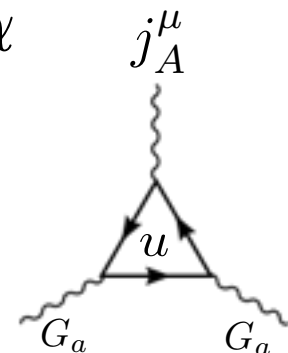
$$\left. \begin{aligned} u_{L,R} &\rightarrow e^{\mp \frac{i\alpha}{2}} u_{L,R} \\ u &\rightarrow e^{\frac{i\alpha}{2} \gamma_5} u \end{aligned} \right\}$$



$$M_u \rightarrow e^{i\alpha} M_u$$

$$\theta \rightarrow \theta - \alpha$$

**consequence of
ABJ anomaly**



The Physical QCD θ -term

for 3 SM quark generations:

$$q_i \rightarrow e^{\frac{i}{2}\alpha_i^q \gamma_5} q_i \quad \rightarrow \quad m_i^q \rightarrow e^{i\alpha_i^q} m_i^q, \quad \theta \rightarrow \theta - \sum_{i,q} \alpha_i^q$$

Can use axial U(1) transformations to move phases arbitrarily between quark mass terms and θ -term

Only invariant combination can be physical

$$\bar{\theta} \equiv \theta + \arg \det (m^u m^d)$$

[Note: if up-quark would be massless could set $\bar{\theta} = \theta \rightarrow 0$]

The Strong CP Problem

Eff. θ -term violates CP and contributes to neutron EDM

$$d_n \approx 4 \times 10^{-16} \bar{\theta} \text{ e cm} \quad \longleftrightarrow \quad |d_n|_{\text{exp}} < 3 \times 10^{-26} \text{ e cm}$$

Why $\bar{\theta} \equiv \theta + \arg \det (m^u m^d) < 10^{-10} \text{ ?}$

Would expect both θ -term and complex Yukawa matrices to be present in Lagrangian and $\bar{\theta} \sim \mathcal{O}(1)$

[Note: cannot impose CP since need complex Yuks for (large) CKM phase]

Solving the Strong CP Problem

- Massless up-quark would be solution, but **ruled out**
- Can impose CP and break it spontaneously such that large CKM phase induced but determinants stay real

Nelson-Barr solution [pure UV, difficult to test]

- If $\bar{\theta}$ would be dynamical field without any other potential, non-perturbative dynamics would generate potential for $\bar{\theta}(x)$ with trivial minimum

Axion solution [new ultra-light, decoupled, stable particle]

The Axion Solution

I. Field without potential is Goldstone boson: need new global symmetry that is spontaneously broken
[remains as shift symmetry $a \rightarrow a + \alpha$]

II. Want to couple Goldstone to gluons: need also anomalous breaking of global symmetry
[shift symmetry broken by $aG\tilde{G}$]

QCD Axion: Goldstone boson of new global symmetry with QCD anomaly

The Peccei-Quinn Mechanism

[Peccei, Quinn '77]

Introduce new global $U(1)_{PQ}$ symmetry with fermion charges such to have QCD anomaly

[non-conserved Noether current $\partial_\mu j_{PQ}^\mu \sim \frac{\alpha_s}{4\pi} G\tilde{G}$]

Break global $U(1)_{PQ}$ symmetry spontaneously at scale f by vev of complex scalar field with charge $+1$

$$\Phi = \frac{f + \phi(x)}{\sqrt{2}} e^{ia(x)/f}$$

$U(1)_{PQ}$ non-linearly realized as shift symmetry

$$\Phi \rightarrow e^{i\alpha} \Phi$$



$$a \rightarrow a + \alpha f$$

The Peccei-Quinn Mechanism

Effective Lagrangian at scales $\ll f$ contains only Goldstone boson $a(x)$, all other fields take mass at f

$$\mathcal{L}_{\text{eff}} = \bar{\theta} \frac{\alpha_s}{8\pi} G_a^{\mu\nu} \tilde{G}_{a,\mu\nu} + \frac{1}{2} \partial_\mu a \partial^\mu a + \underbrace{\mathcal{L}_{\text{a,int}}\left[\frac{\partial_\mu a}{f}, \psi_{\text{SM}}\right]}_{\text{Interactions with SM fermions}} + \frac{a}{f} \xi \underbrace{\frac{\alpha_s}{8\pi} G_a^{\mu\nu} \tilde{G}_{a,\mu\nu}}_{\text{ABJ term for QCD anomaly}} + \underbrace{\mathcal{L}_{\text{anom}}\left[\frac{a}{f} F \tilde{F}\right]}_{\text{ABJ term for other anomalies}}$$

[respects shift symmetry] [breaks shift symmetry] [cf. $\frac{\pi^0}{f_\pi} F \tilde{F}$]

Depends on $\bar{\theta}$ only through PQ invariant combination

$$\frac{\bar{a}(x)}{f_a} \equiv \bar{\theta} + \frac{a(x)}{f} \xi$$

[have essentially made $\bar{\theta}$ dynamical field]

The Peccei-Quinn Mechanism

Effective Lagrangian induces axion potential

$$V_{\text{eff}} = -\frac{\bar{a}(x)}{f_a} \frac{\alpha_s}{8\pi} G_a^{\mu\nu} \tilde{G}_{a,\mu\nu} \xrightarrow[\text{effects}]{\text{non-PT}} V(a) \sim -m_\pi^2 f_\pi^2 \left| \cos \frac{\bar{a}(x)}{f_a} \right|$$

Potential minimized at CP-conserving vev $\langle \bar{a}(x) \rangle = 0$

θ -term dynamically relaxed to zero

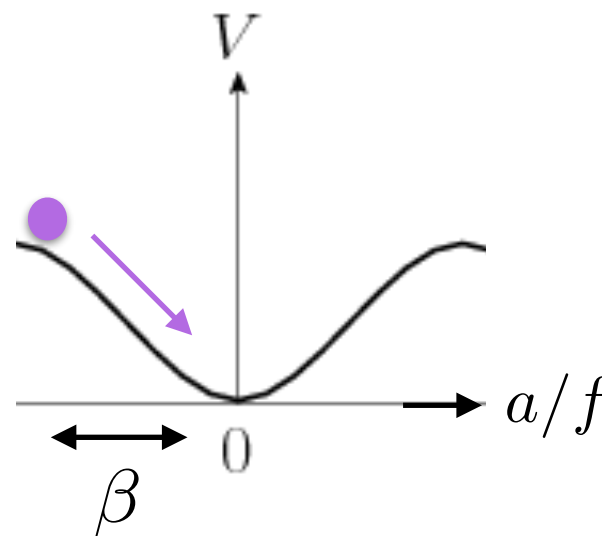
Generates also axion mass $m_a \sim m_\pi f_\pi / f_a$
couples to photons and SM fermions $\sim 1/f_a$

For large f_a axion is ultra-light and decoupled

Axions as Dark Matter

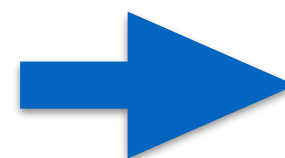
[axion essentially stable for $m_a \lesssim 20 \text{ eV}$]

In early universe axion displaced from minimum



As universe expands axion rolls down and starts oscillating around minimum: energy stored in oscillations contributes to DM relic density

$$\Omega_{\text{DM}} h^2 \approx 0.1 \left(\frac{10^{-5} \text{ eV}}{m_a} \right)^{1.18} \beta^2$$



Right abundance for
 $10^{-8} \text{ eV} \lesssim m_a \lesssim 10^{-4} \text{ eV}$

Axion Models

Choose PQ charges of SM/BSM fermions for QCD anomaly

Models characterised by axion-photon couplings E/N
and PQ breaking scale/axion mass $f_a \leftrightarrow m_a$

- **PQWW axion** [Peccei, Quinn, Wilczek, Weinberg '78]

2HDM model without new fermions, $f_a \sim v$, $m_a \sim 30$ keV



- **DFSZ axion** [Dine, Fischler, Srednicki, Zhitnitsky '80]

2HDM model without new fermions but extra singlet scalar that
breaks PQ at scale f_a much above electroweak scale; $|E/N| \in [0.3, 2.7]$

- **KSVZ axion** [Kim, Shifman, Vainshtein, Zakharov '80]

SM model with new (heavy) fermions and extra singlet scalar that
breaks PQ at scale f_a much above electroweak scale; $|E/N| \in [0, 6]$

Axion Searches

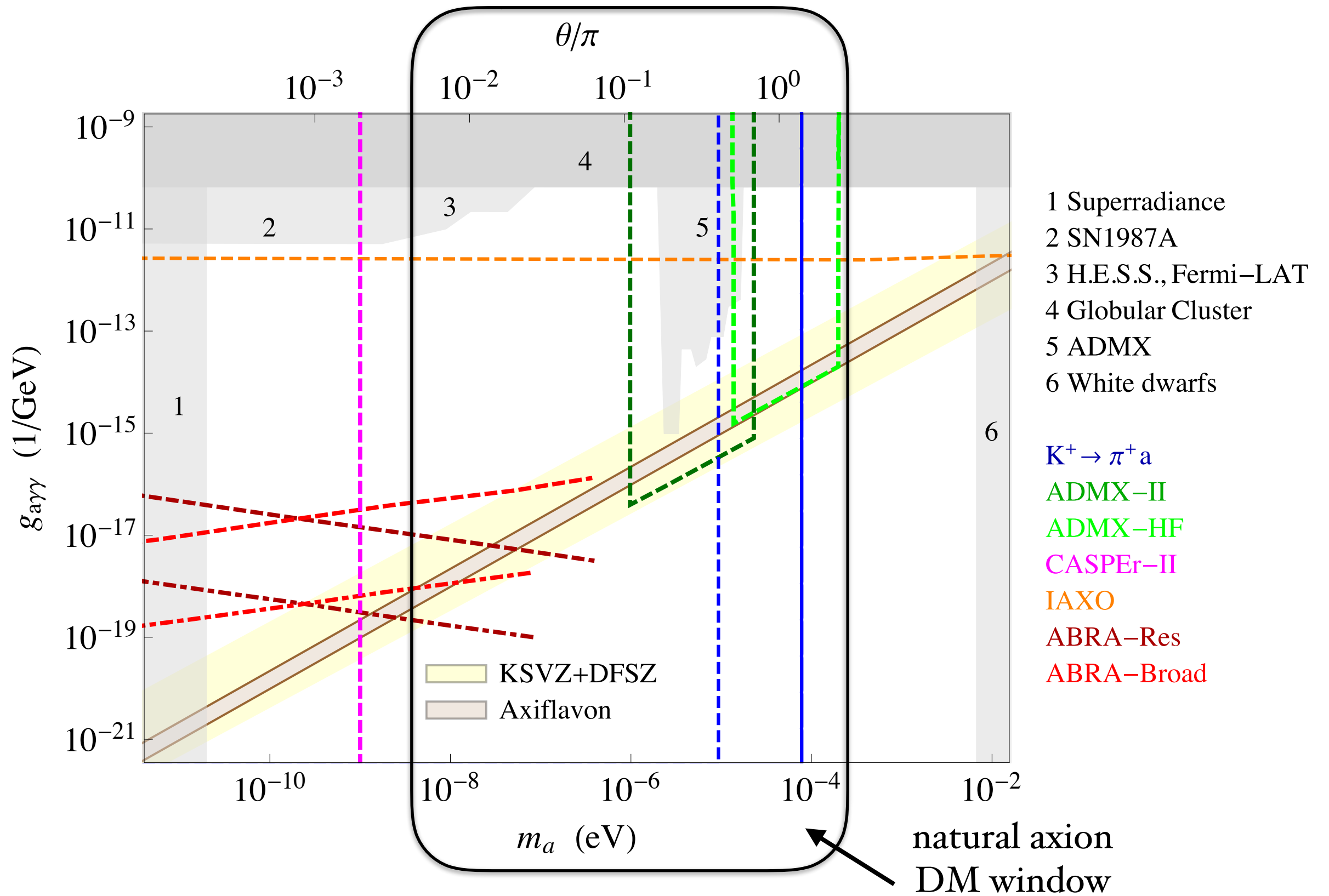
Axion searches typically rely on axion-photon coupling

$$\mathcal{L} \supset g_{a\gamma\gamma} a \vec{E} \cdot \vec{B} \qquad g_{a\gamma\gamma} \sim \frac{E}{N} \frac{1}{10^{16} \text{GeV}} \frac{m_a}{\mu\text{eV}}$$

Haloscopes: DM axion $\xrightarrow{\text{static B-field}}$ photon $E_\gamma \sim m_a$
ADMX
resonantly detected by
microwave cavities of size $1/m_a$

Helioscopes: solar photon $\xrightarrow{\text{nuclear E-field}}$ axion $E_a \sim \text{keV}$
CAST/IAXO
converted back to X-ray
photons with static B-fields

Axion Searches



Axions and Flavor

In usual axions solution PQ symmetry and quantum numbers are ad-hoc and serve no other purpose than to solve strong CP problem

Interesting to connect PQ to other global symmetries, e.g. **flavor symmetries** that explain Yukawa hierarchies

$$\text{PQ} = \text{subgroup of } U(3)^5 \xrightarrow{\text{yuks}} U(1)_B \times U(1)_{L_i}$$

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(Received 20 September 1982)

Possible advantages of replacing the Peccei-Quinn $U(1)$ quasisymmetry by a group of genuine flavor symmetries are pointed out. Characteristic neutral Nambu-Goldstone bosons will arise, which might be observed in rare K or μ decays. The formulation of Lagrangians embodying these ideas is discussed schematically.

The Flavon



The SM Flavor Puzzle

Matter fields come in 3 families
with same gauge quantum numbers

Accounts for most parameters of SM:
fermion masses and mixings that are
strongly hierarchical

$y_u \sim \epsilon^{7 \div 8}$	$y_d \sim \epsilon^7$	$V_{ub} \sim \epsilon^3$
$y_c \sim \epsilon^{3 \div 4}$	$y_s \sim \epsilon^5$	$V_{cb} \sim \epsilon^2$
$y_t \sim 1$	$y_b \sim \epsilon^3$	$V_{us} \sim \epsilon$

$$\epsilon \approx 0.2$$

Why are these numbers so small?

Flavor Symmetries

Light fields charged under flavor symmetry G ,
which is spontaneously broken by “flavon” field ϕ

Effective Yukawa Lagrangian needs flavon
insertions in order to be invariant under G

The diagram shows the effective Yukawa Lagrangian $\mathcal{L}_{\text{eff}} \sim a_{ij} \left(\frac{\phi}{\Lambda_F} \right)^{x_{ij}} h \bar{q}_i u_j$ enclosed in a black rectangular box. Three blue arrows point to specific parts of the equation: one from the text 'from G selection rules' points to the exponent x_{ij} ; one from 'O(1) coefficients' points to the coefficient a_{ij} ; and one from 'cutoff scale' points to the denominator Λ_F in the fraction.

$$\mathcal{L}_{\text{eff}} \sim a_{ij} \left(\frac{\phi}{\Lambda_F} \right)^{x_{ij}} h \bar{q}_i u_j$$

Yukawas given by powers of small order parameter $\epsilon \equiv \frac{\phi}{\Lambda_F}$

U(1) Flavor Symmetries

	ϕ	\bar{q}_i	u_i	d_i	h
U(1)	-1	q_i	u_i	d_i	0

U(1) selection rule gives sum of charges

$$y_{ij}^U \sim \epsilon^{q_i + u_j} \quad y_{ij}^D \sim \epsilon^{q_i + d_j}$$

Simple pattern can reproduce all hierarchies, e.g.

$$q_i = (3, 2, 0)$$

$$u_i = (4, 2, 0)$$

$$d_i = (4, 3, 3)$$

$$y^U \sim \begin{pmatrix} \epsilon^7 & \epsilon^5 & \epsilon^3 \\ \epsilon^6 & \epsilon^4 & \epsilon^2 \\ \epsilon^4 & \epsilon^2 & 1 \end{pmatrix}$$

$$y^D \sim \begin{pmatrix} \epsilon^7 & \epsilon^6 & \epsilon^6 \\ \epsilon^6 & \epsilon^5 & \epsilon^5 \\ \epsilon^4 & \epsilon^3 & \epsilon^3 \end{pmatrix}$$

$$\epsilon \approx 0.2$$

U(1) Flavor Symmetries

Charge assignments are not unique because of
O(1) coefficients and order parameter $\sim 1/5$

Still can show that **U(1) is necessarily anomalous**

[Binetruy, Ramond '94]

$$\underbrace{\det m_u \det m_d / v^6}_{\approx 10^{-20}} = \underbrace{[\det a_u \det a_d]}_{\mathcal{O}(1)} \epsilon^{2N}$$

QCD anomaly coefficient \uparrow

$$\underbrace{\det m_d / \det m_e}_{\approx 0.7} = \underbrace{[\det a_d / \det a_e]}_{\mathcal{O}(1)} \epsilon^{\frac{8}{3}N - E}$$

EM anomaly coefficient \uparrow

Predictivity of Flavor Symmetries

All BSM effects suppressed by messenger scale

$$\mathcal{L}_{eff} \sim \frac{1}{\Lambda_F^2} \left(\frac{\phi}{\Lambda_F} \right)^{y_{ij}} (\bar{q}_i \gamma^\mu q_j)^2 + \dots$$

Overall cutoff scale/symmetry breaking scale is not determined, since explain *dimensionless* Yukawa couplings

No measurable effects if very large messenger scale:
need to combine with new low-energy dynamics

The Axiflavon



General Idea

Identify PQ symmetry with $U(1)$ flavor symmetry:
the phase of the flavon is the QCD axion = axiflapon

Can obtain pretty sharp prediction for axion-photon
coupling E/N [in contrast to broad range in usual axion models]

Get predictions for axion-fermion couplings, which
in general are flavor-violating [but $O(1)$ uncertainties]

Very predictive framework that is testable
both at axion and flavor experiments

Setup

Effective U(1) flavor model

$$\mathcal{L} \sim a_{ij}^u \left(\frac{\Phi}{\Lambda} \right)^{q_i + u_j} Q_i U_j^c H + \dots$$

$$\Phi = \frac{1}{\sqrt{2}} (V_\Phi + \phi) e^{ia/V_\Phi}$$

$V_\Phi \sim f_a \gg v$ decouples axion

SM Yukawas

$$y_{ij}^u = a_{ij}^u \epsilon^{q_i + u_j}$$

axion-fermion couplings

$$g_a f_i f_j \sim \frac{v}{V_\Phi} y_{ij}$$

axion mass

$$m_a = 5.7 \mu\text{eV} \left(\frac{10^{12} \text{GeV}}{f_a} \right)$$

usual
QCD
axion
relations

axion-photon couplings

$$g_{a\gamma\gamma} \sim \frac{E}{N} \frac{1}{10^{16} \text{GeV}} \frac{m_a}{\mu\text{eV}}$$

Photon couplings

Although have considerable freedom in fermion
 U(1) charges **can sharply predict E/N**

$$\frac{E}{N} \in [2.4, 3.0]$$

Direct consequence of fermion mass hierarchies

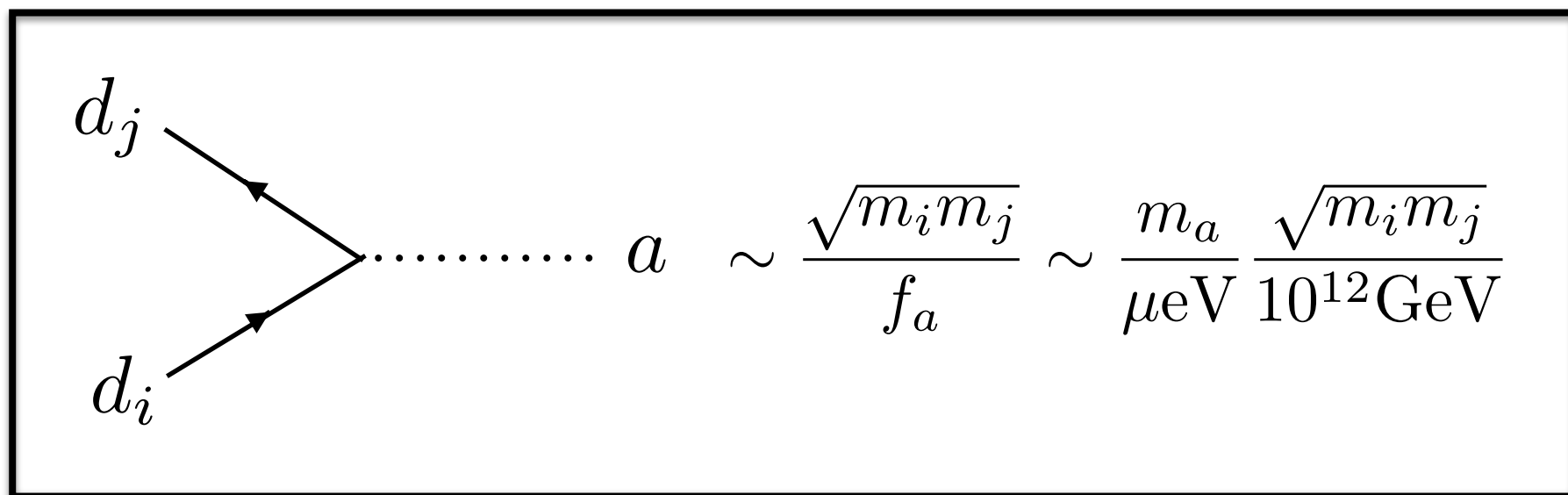
$$\frac{E}{N} = \frac{8}{3} - 2 \frac{\log \frac{\det m_d}{\det m_e} - \log \alpha_{de}}{\log \frac{\det m_u \det m_d}{v^6} - \log \alpha_{ud}}$$

-0.4
~0

2.7
-44
~0

Fermion couplings

Predicted with somewhat larger [but $O(1)$] uncertainties



The diagram shows two incoming fermion lines, labeled d_j and d_i , meeting at a vertex. From this vertex, a dotted line representing an axion a extends to the right. To the right of the diagram, the coupling is given by the formula:

$$\sim \frac{\sqrt{m_i m_j}}{f_a} \sim \frac{m_a}{\mu\text{eV}} \frac{\sqrt{m_i m_j}}{10^{12} \text{GeV}}$$

Axiflavoron essentially massless [$< \text{meV}$] and stable

Strongest bounds from flavor-violating meson decays with invisible massless particle

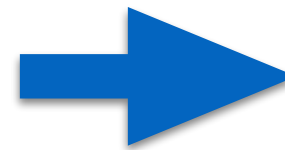
Probing the Axiflavor

Kaon Sector

$$\text{BR}(K^+ \rightarrow \pi^+ a) \simeq 1.2 \cdot 10^{-10} \left(\frac{m_a}{0.1 \text{ meV}} \right)^2 \underbrace{\left(\frac{\kappa_{sd}}{N} \right)^2}_{\mathcal{O}(1)}$$

90% CL combined bound from E787 + E949

$$\text{BR}(K^+ \rightarrow \pi^+ a) < 7.3 \cdot 10^{-11}$$



$$m_a \lesssim 0.08 \text{ meV}$$
$$f_a \gtrsim 7 \times 10^{10} \text{ GeV}$$

Expected improvement for NA62 is factor ~70

will probe up to

$$m_a \sim 9 \mu\text{eV}$$

Summary Plot

