Beyond the Standard Model

Andrea Wulzer



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BSM = **Behind** the SM (goal is explain SM mysteries)

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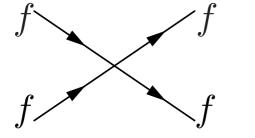
Plan of the lectures

- 1. No-Lose Theorems (or, why the Higgs is revolutionary)
- 2. The "SM-only" Option
- 3. The Naturalness Argument
- 4. What if Un-Natural?
- 5. Composite Higgs
- 6. The Minimal CH couplings (and other signatures)
- 7.SUSY theory
- 8.SUSY and Naturalness (or, why to care about SUSY)
- 9. Other virtues of SUSY

A number of guaranteed discoveries in the history of HEP

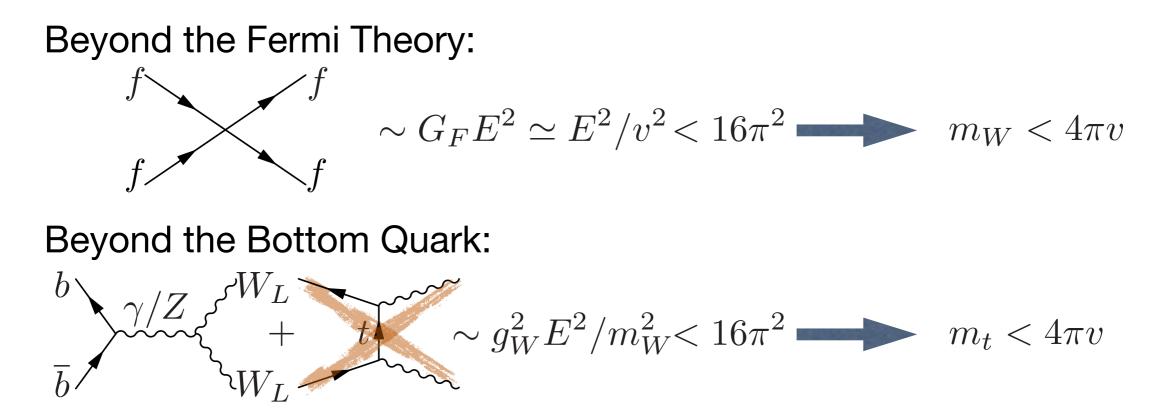
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Beyond the Fermi Theory:

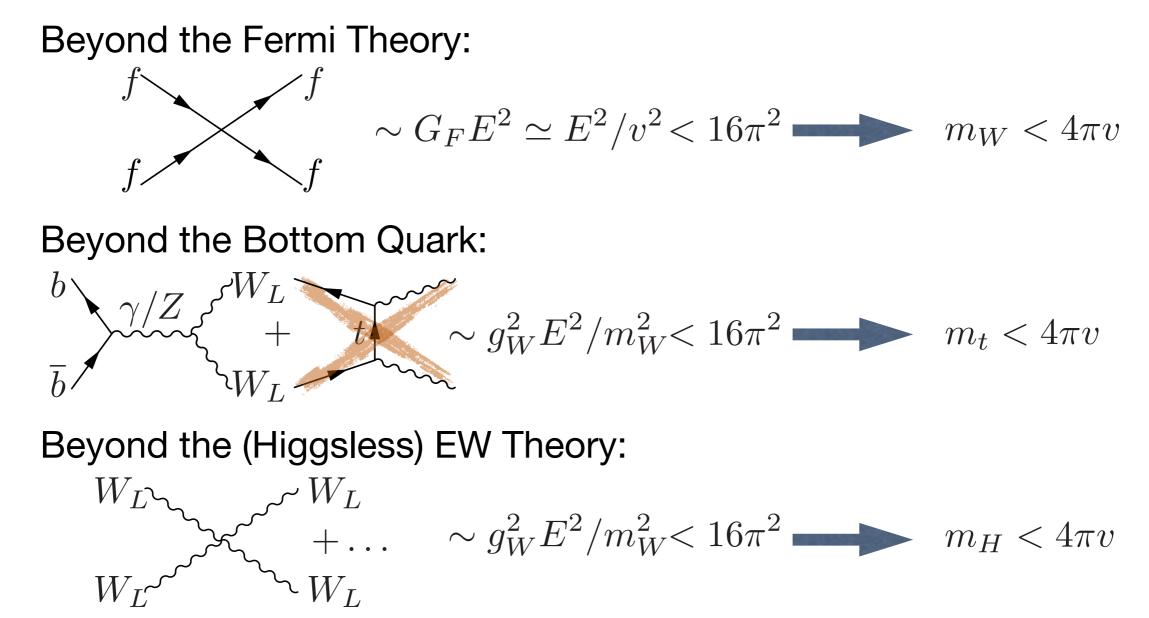


 $\int_{f}^{f} \sim G_F E^2 \simeq E^2 / v^2 < 16\pi^2 - m_W < 4\pi v$

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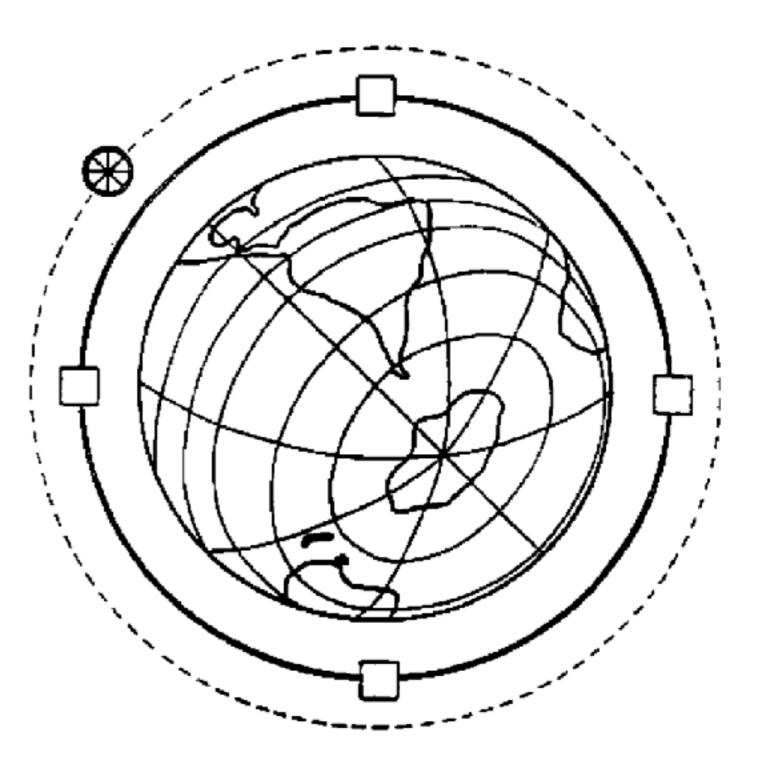
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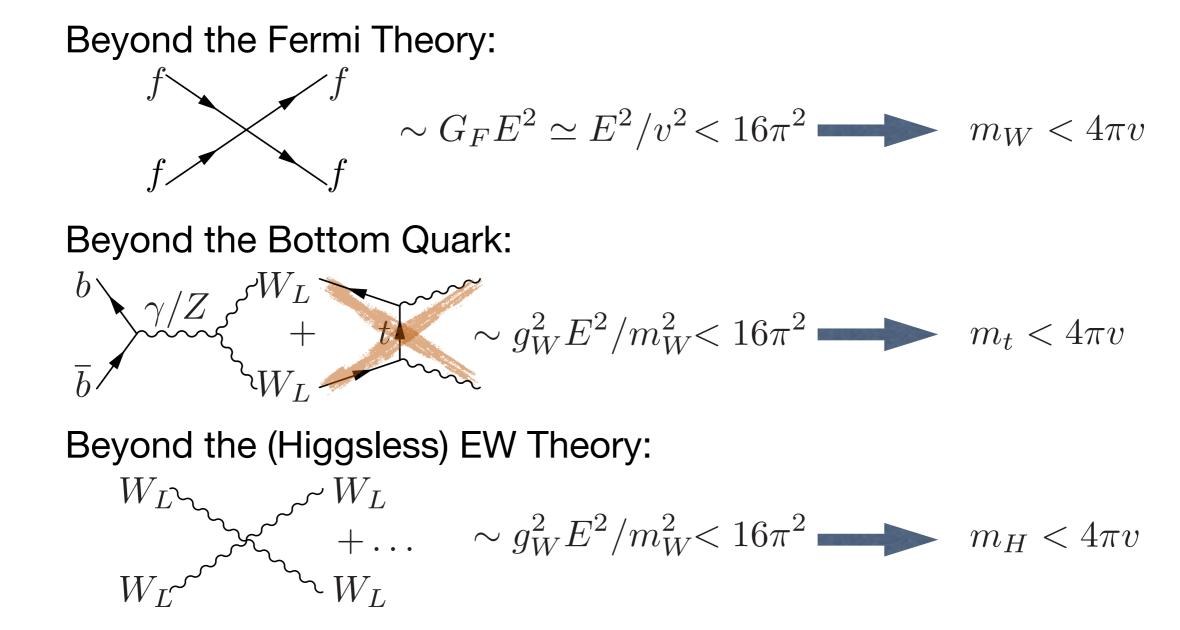
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Fermi's **Ultimate Accelerator**

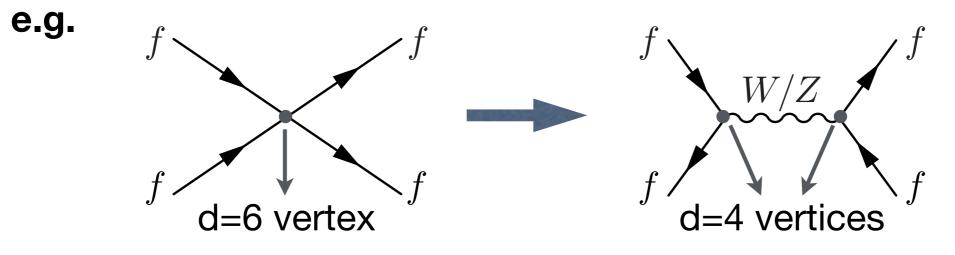


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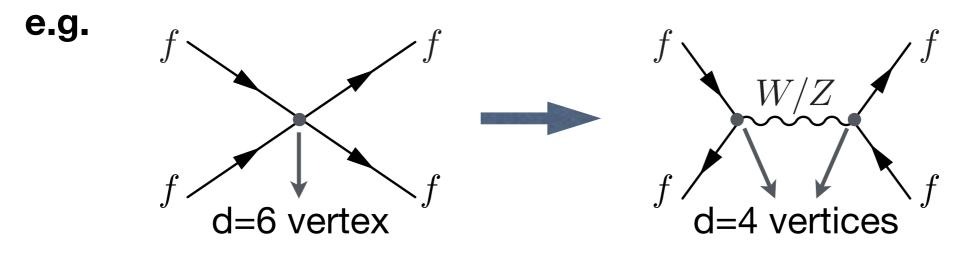


Each secretly due to d=6 non-renormalizable operators, signalling nearby new physics.

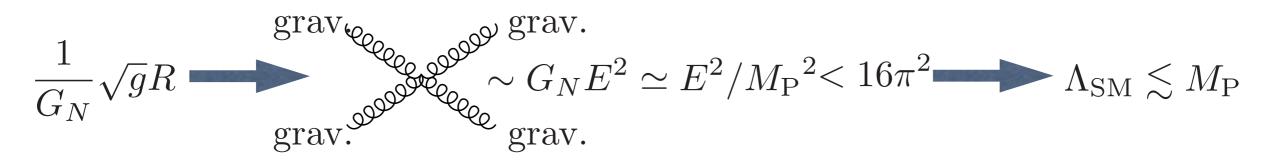
Each time we exploit one No-Lose Theorem, we get rid of one d=6 operator ...



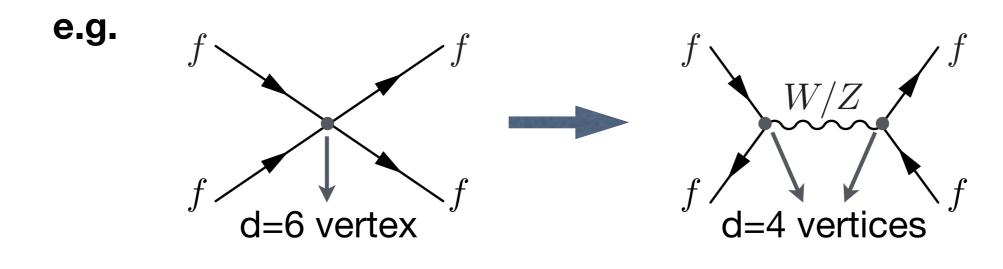
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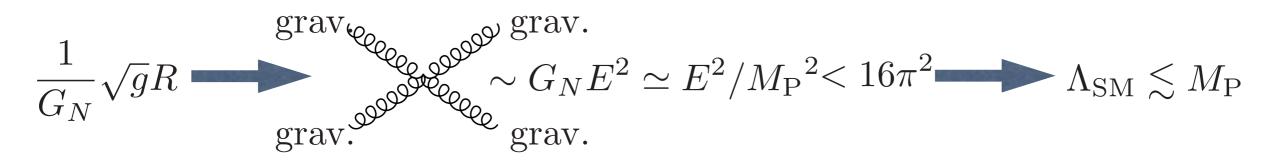
... and only one is left after Higgs discovery ...



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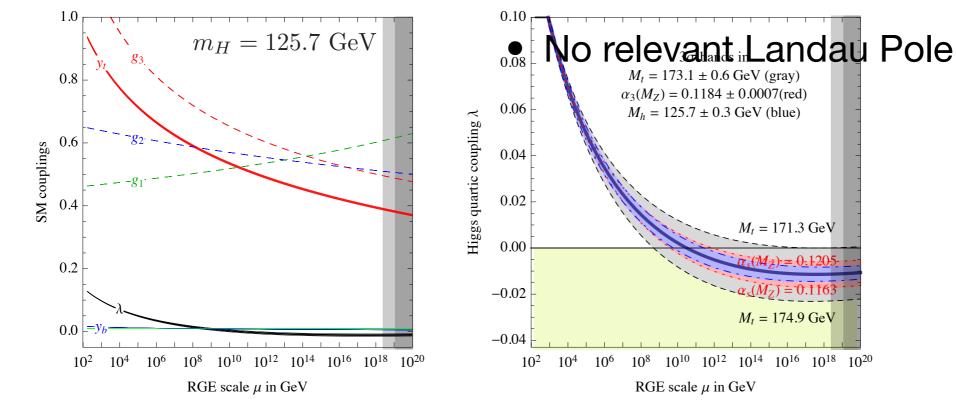


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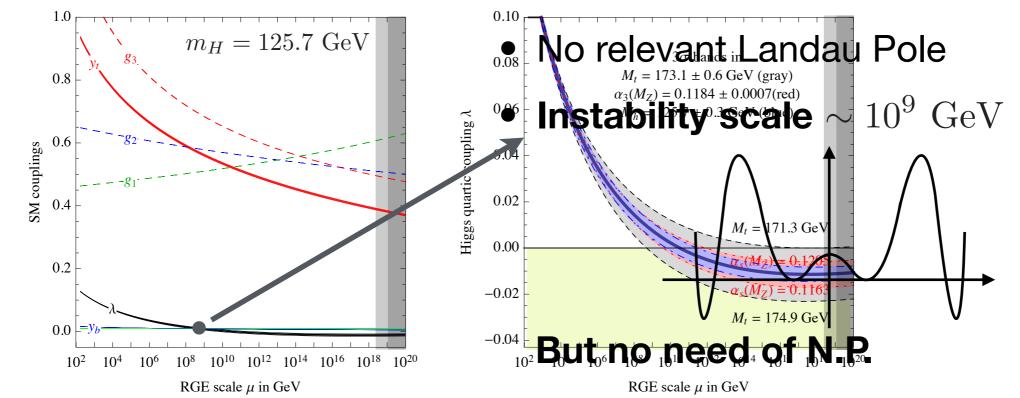


... the last, impractical, No-Lose Theorem is Q.G. at $M_{\rm P}$!

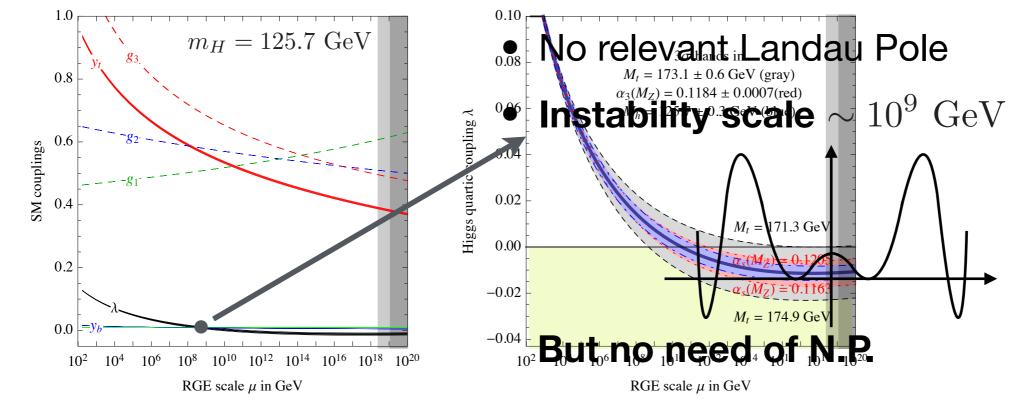
The statement survives quantum corrections:



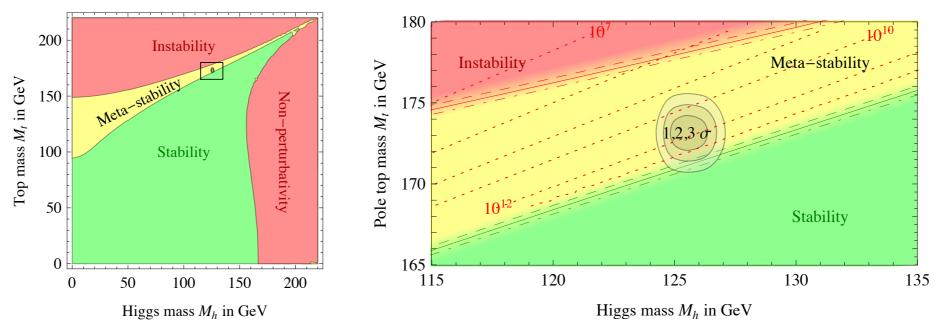
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Non trivial result. Depends on Higgs and Top mass:



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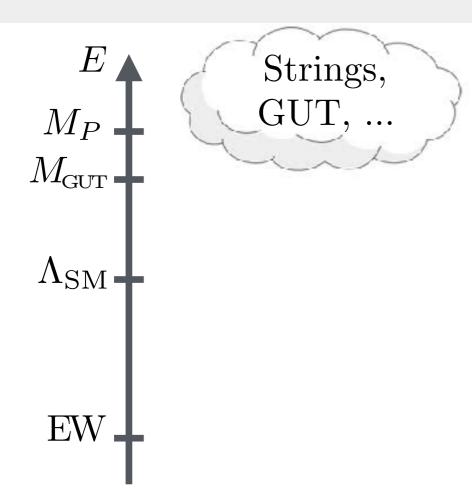
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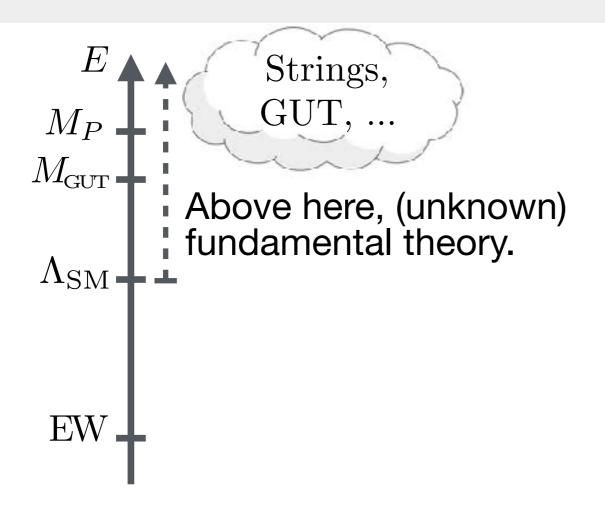
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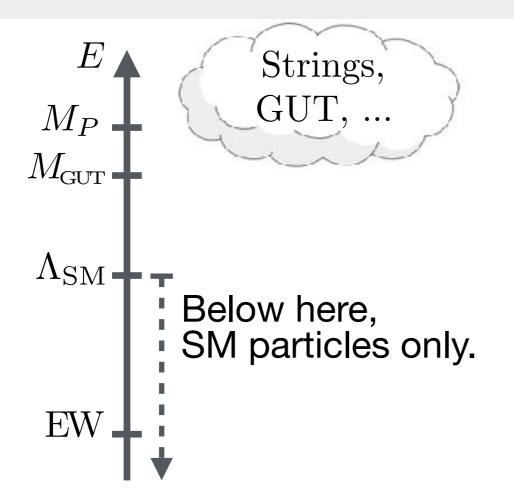
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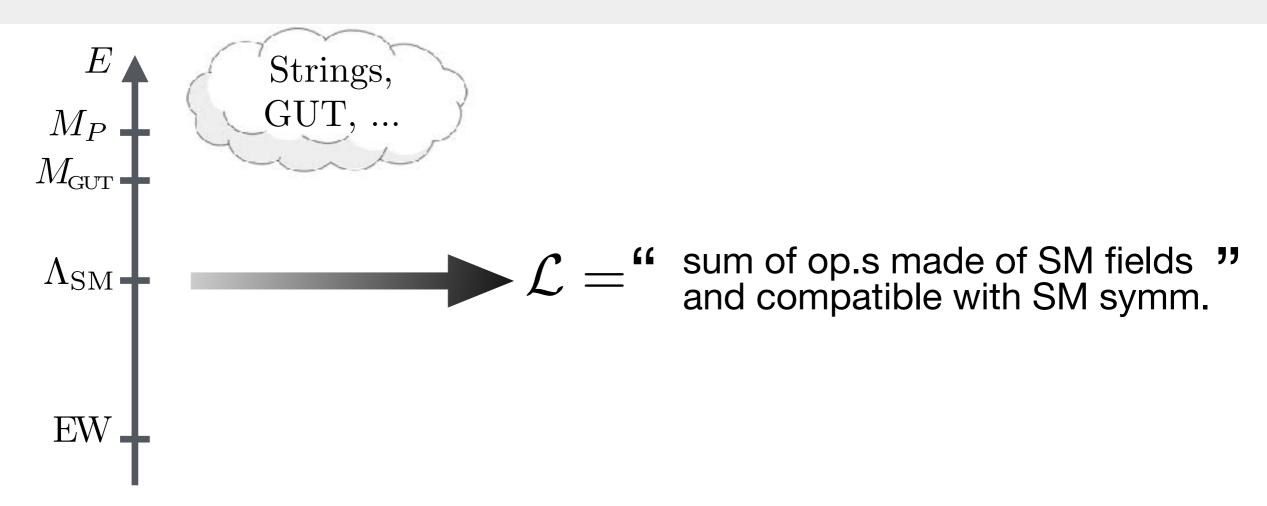
The Naturalness Problem: Why $m_H \ll \Lambda_{\rm SM}$? (to be discussed later)







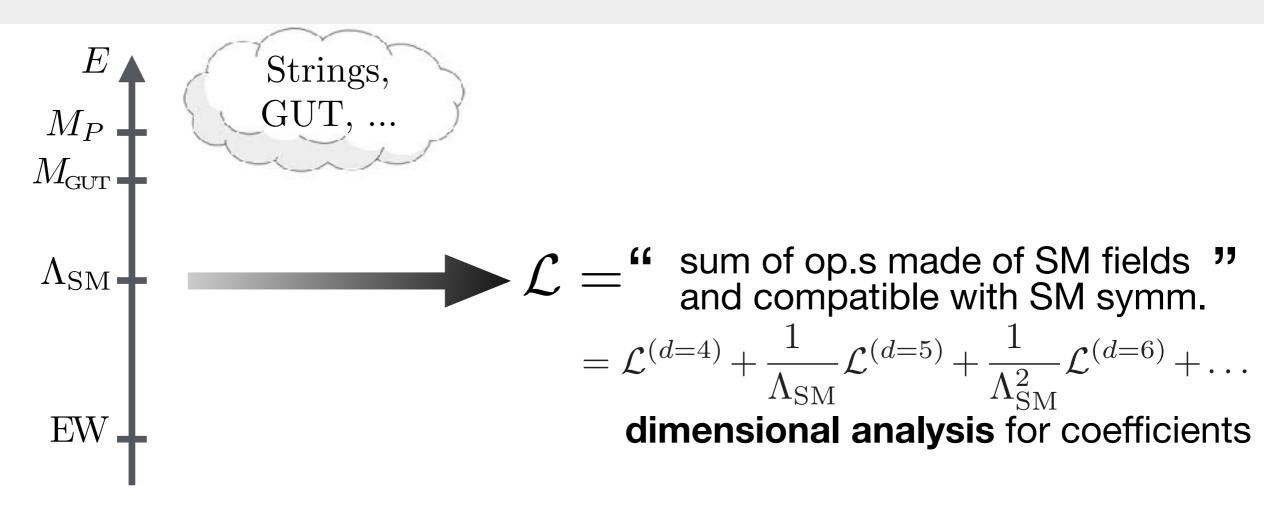
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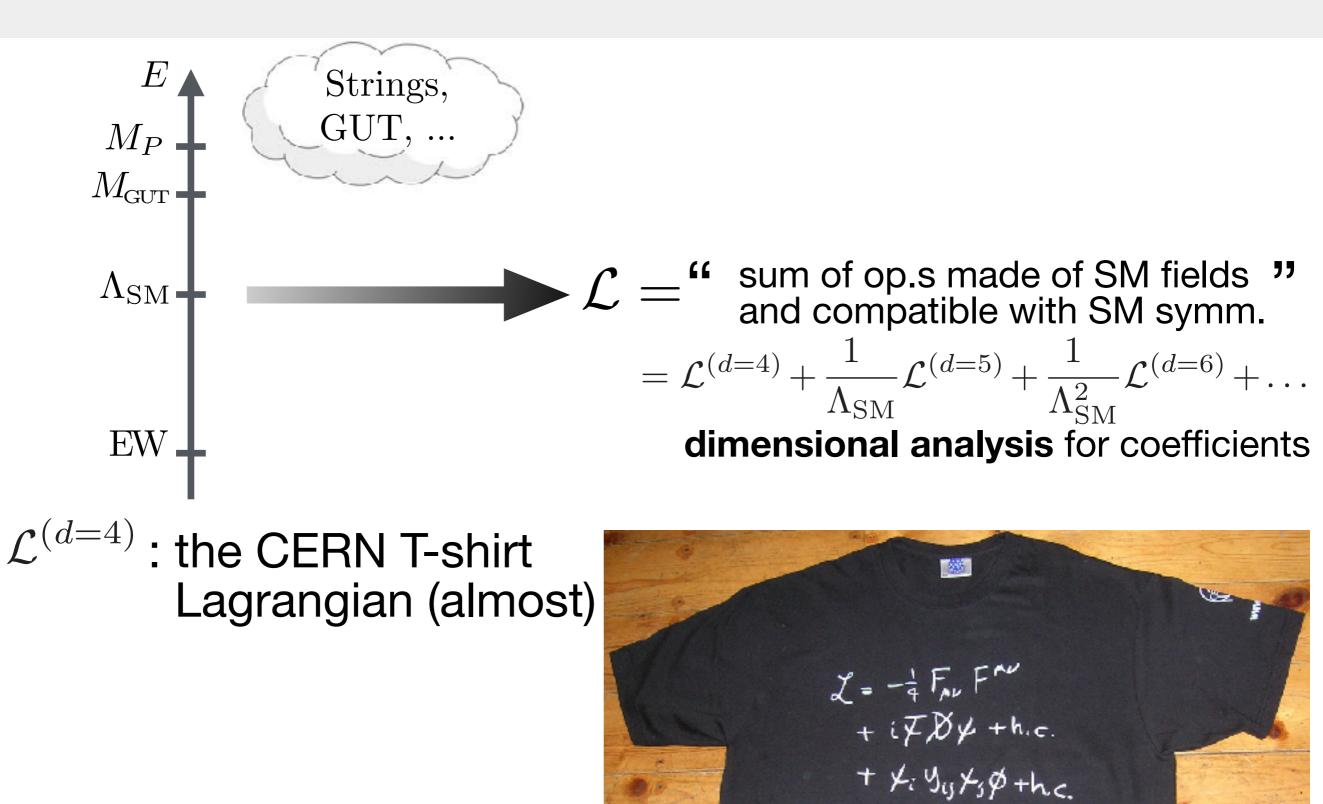
Fermi theory analogy: $G_F \sim \sum = \frac{1}{4\sqrt{2}}$



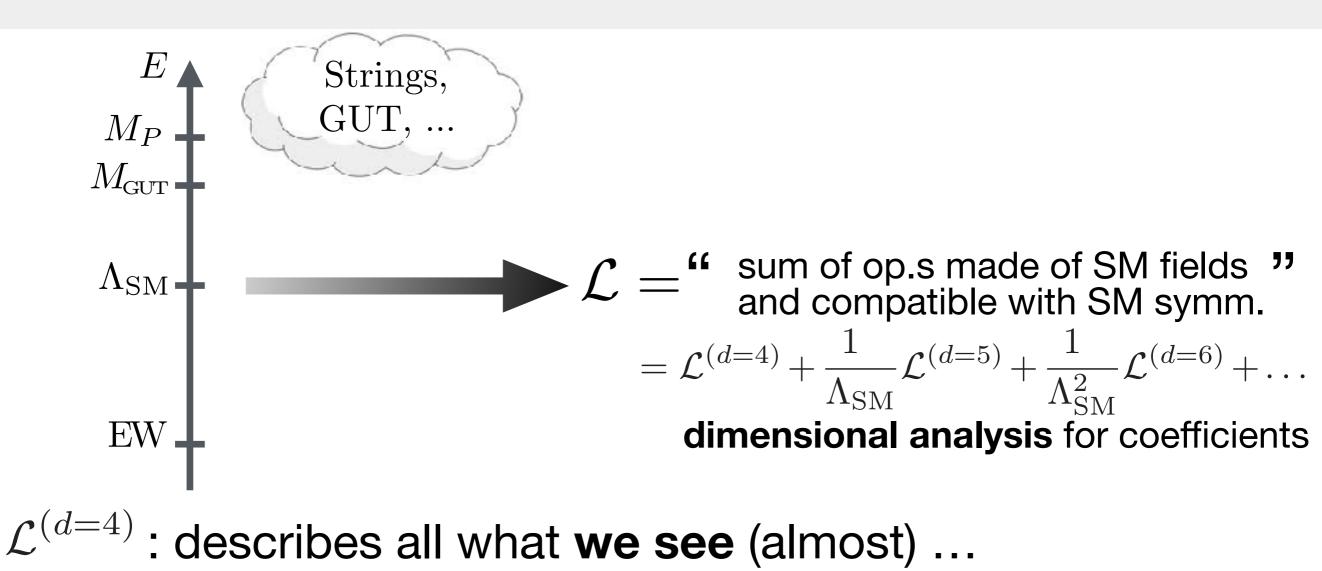
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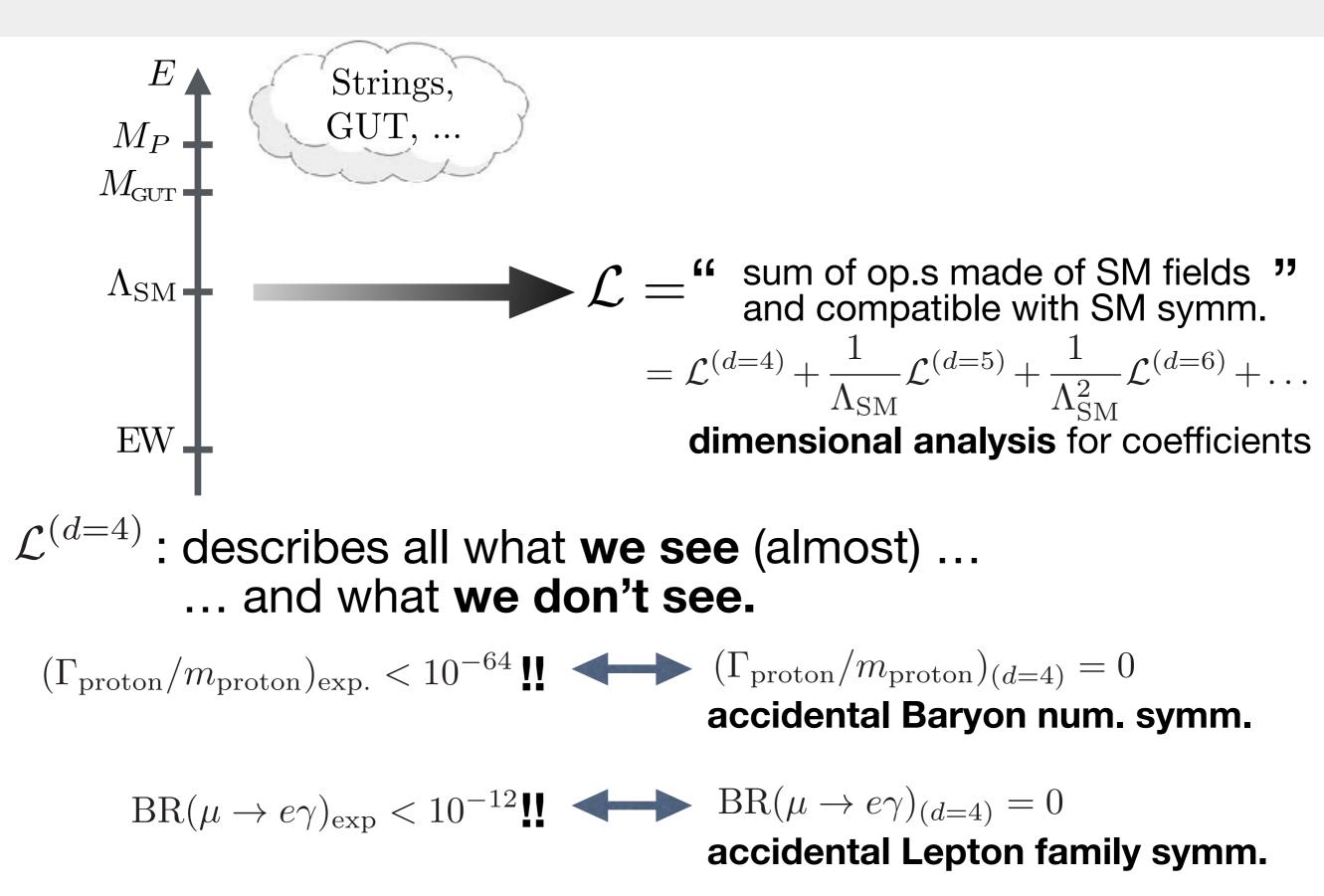
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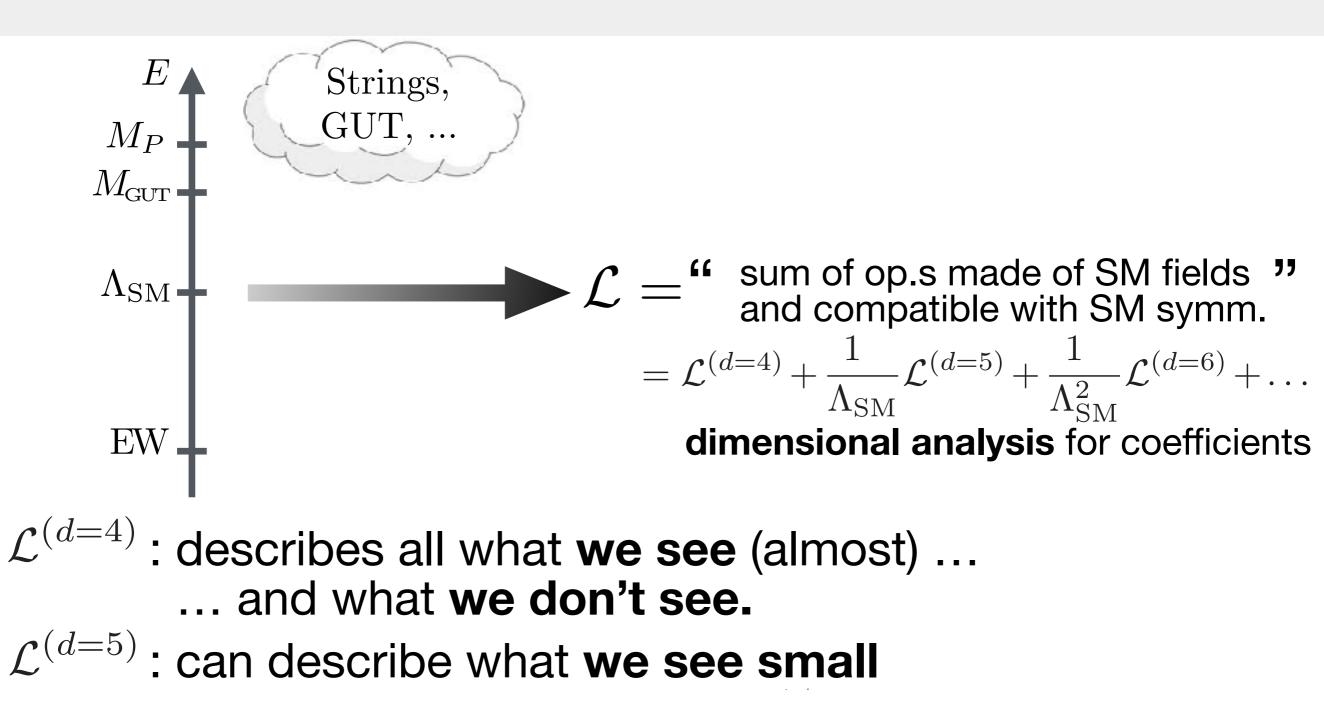
Fermi theory analogy: $G_F \sim \sum = \frac{g_W^2}{4\sqrt{2}m_W^2}$



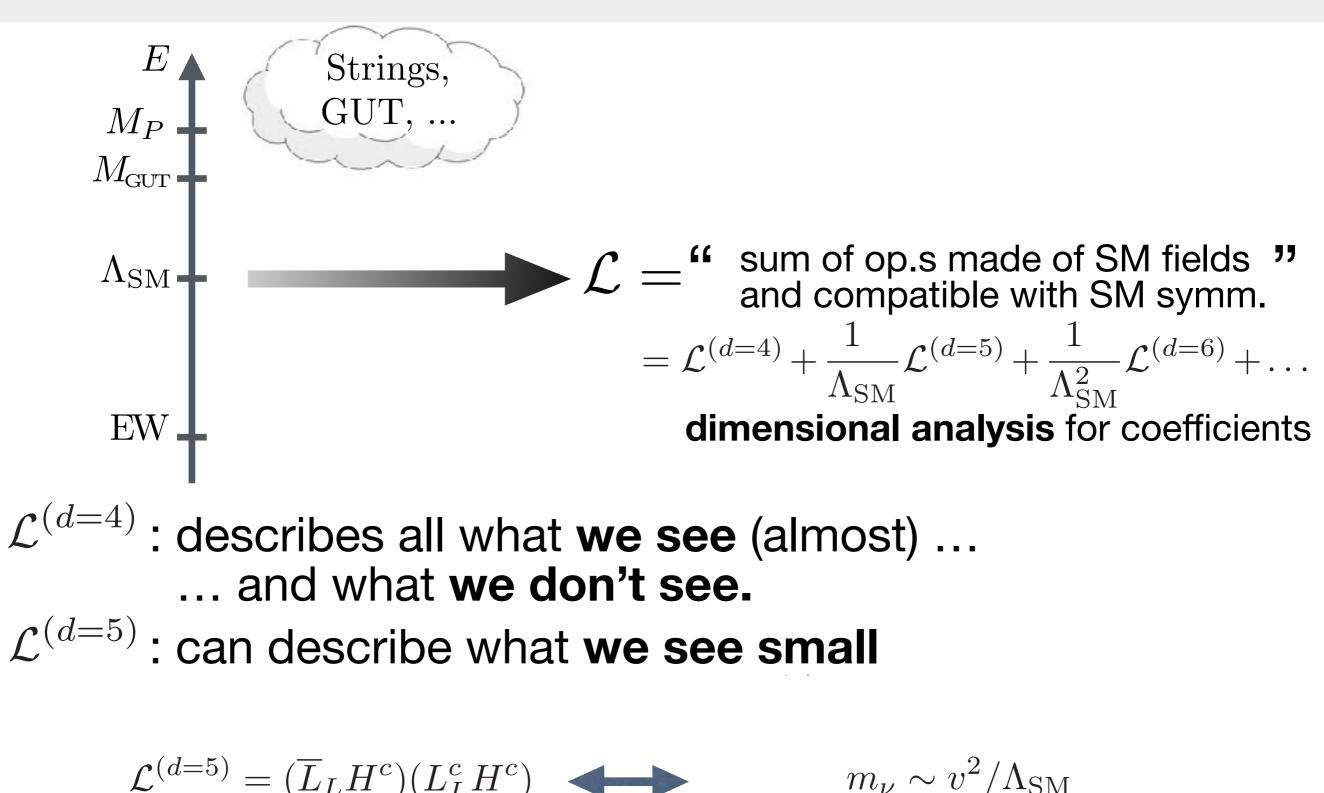
 $+|\mathbf{p}_{g}|^{2}-V(\mathbf{\phi})$





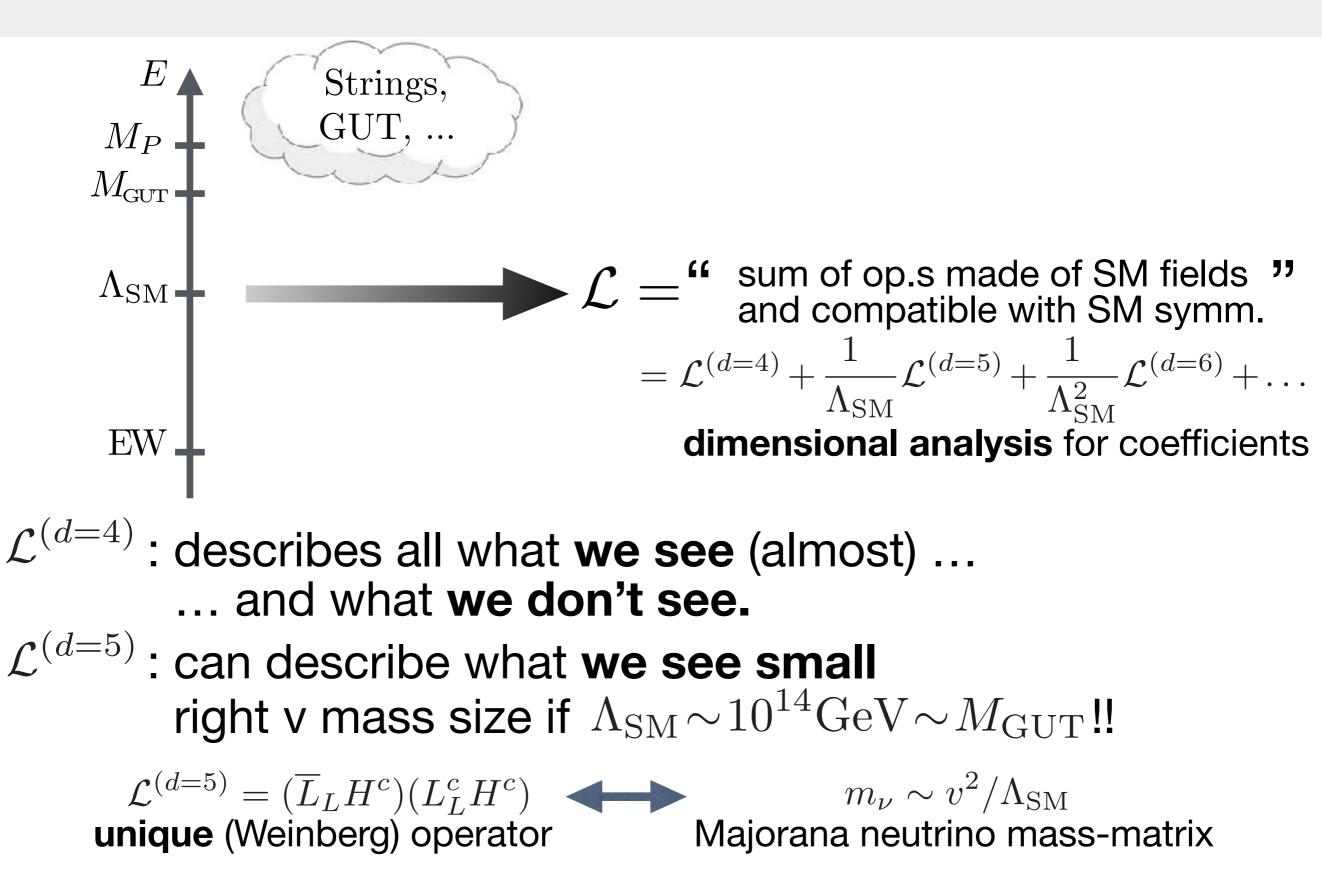


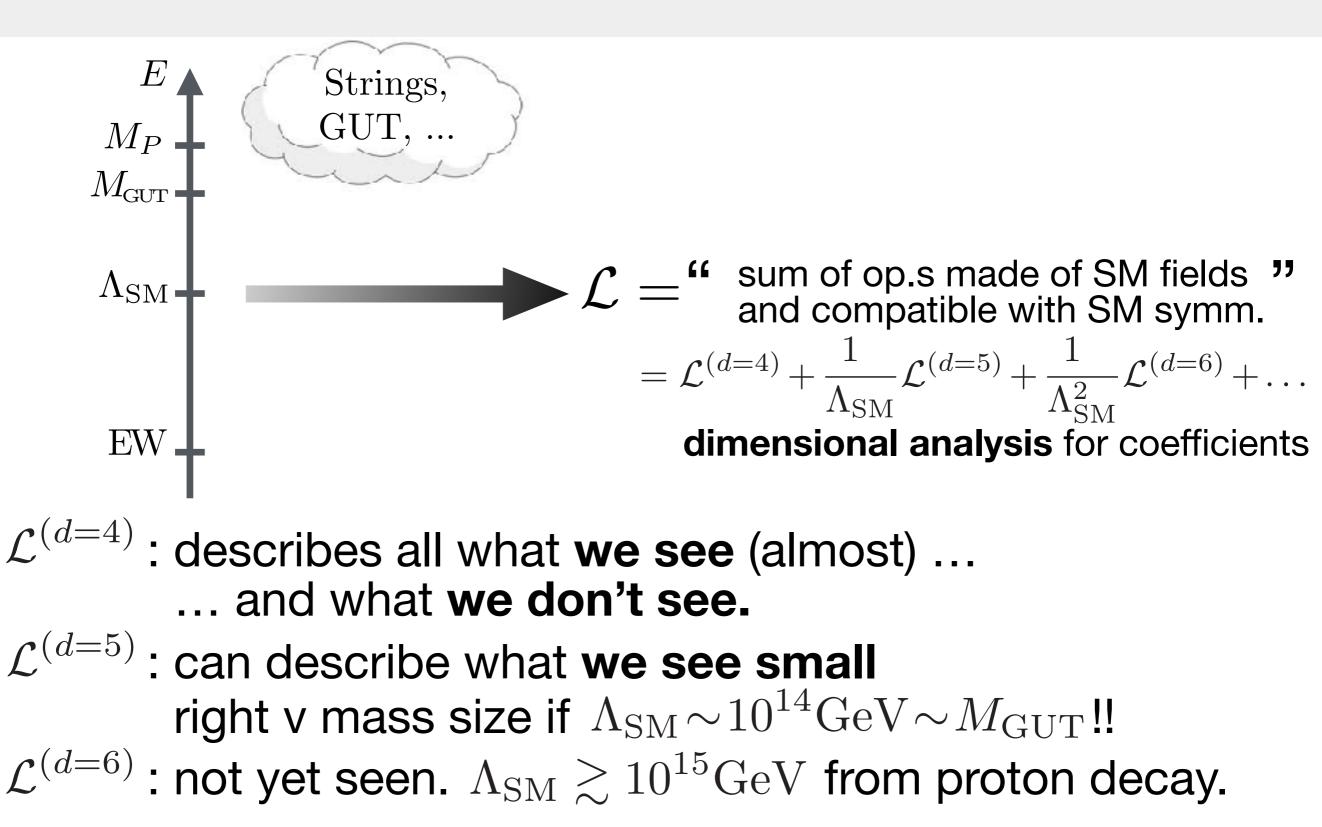
 $\mathcal{L}^{(d=5)} = (\overline{L}_L H^c) (L_L^c H^c)$ unique (Weinberg) operator

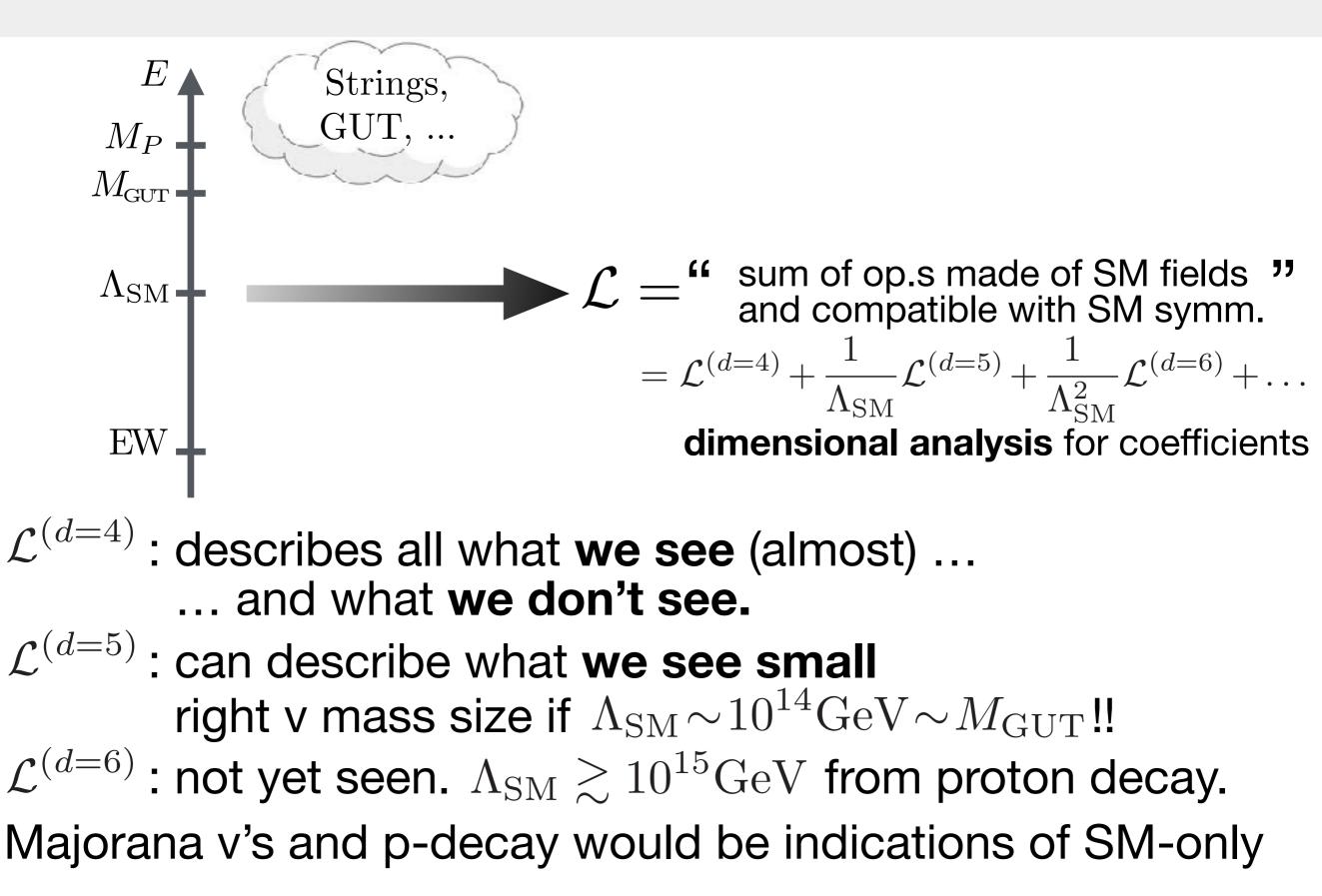


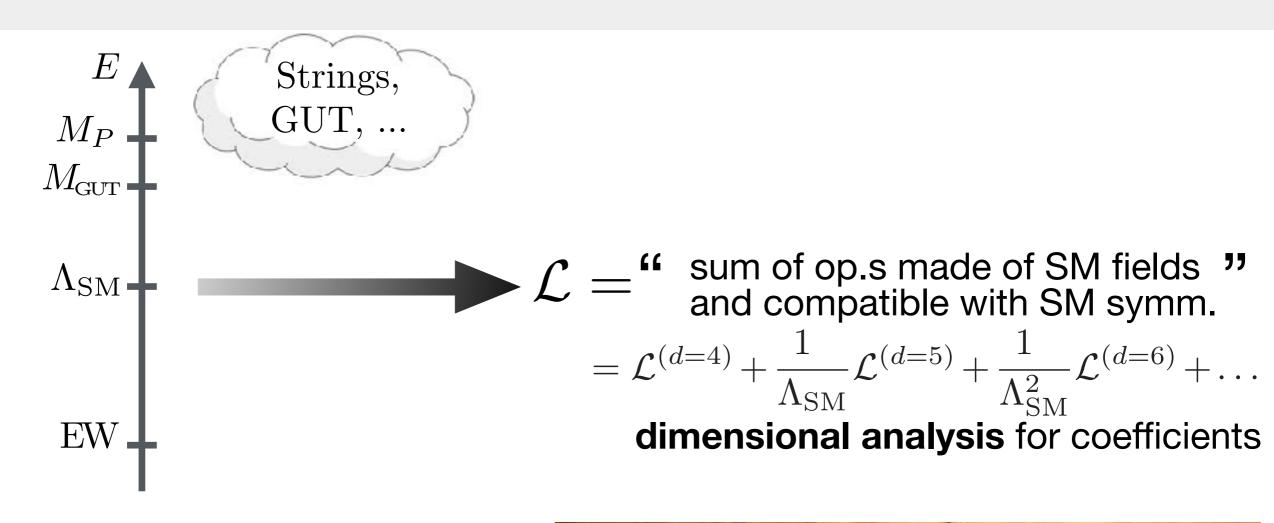
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Majorana neutrino mass-matrix



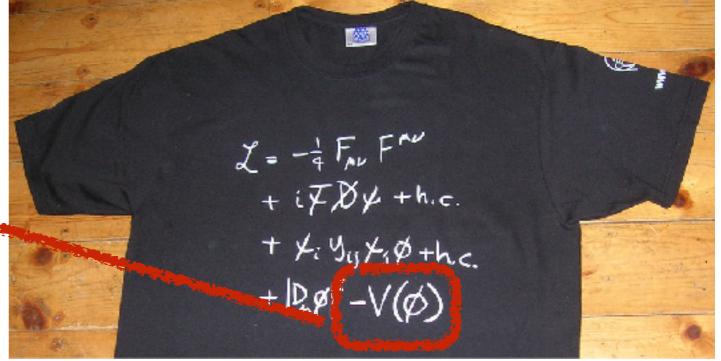


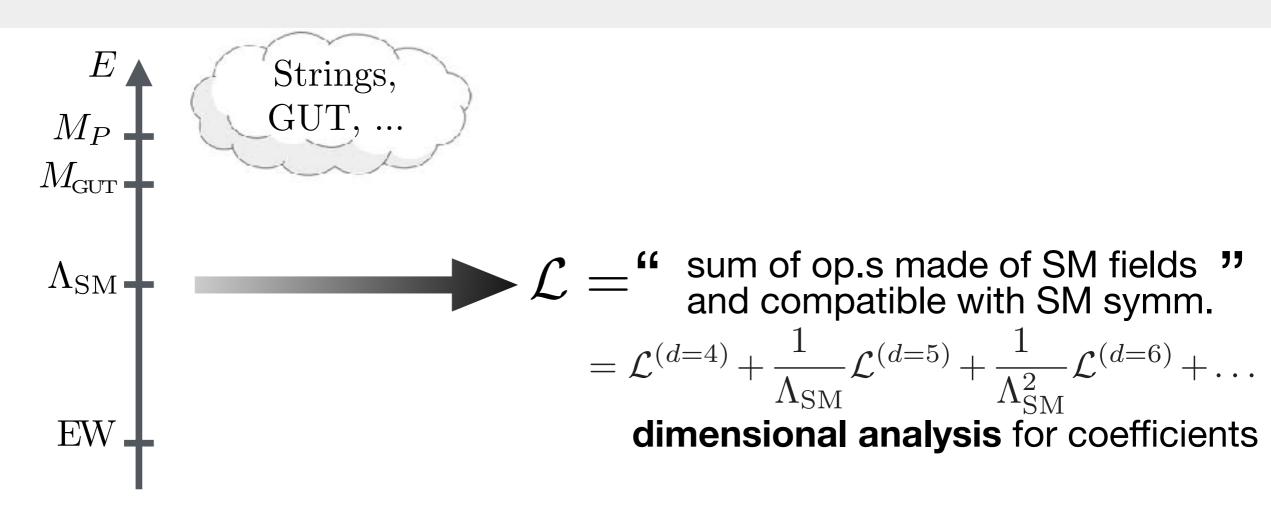




But we forgot one operator.

$$\mathcal{L}^{(d=2)} = H^{\dagger}H$$

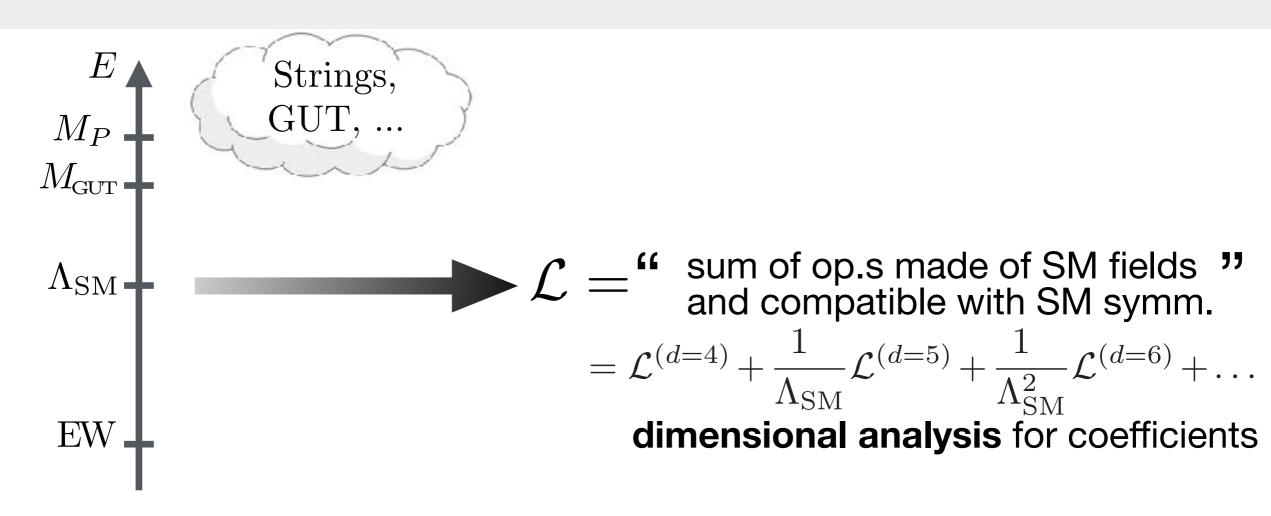




But we forgot one operator. Using again dim. analysis:

$$\mathcal{L}_{H\text{-mass}} = \Lambda_{\text{SM}}^2 \mathcal{L}^{(d=2)} = \Lambda_{\text{SM}}^2 H^{\dagger} H$$

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Instead, $\mathcal{L}_{H\text{-mass}} = \frac{m_H^2}{2} H^{\dagger} H$
The **Naturalness Problem**: Why $m_H \ll \Lambda_{\text{SM}}$?
(or, why dim. analysis works for d>4 and not for d<4?)

Exercise: Accidental Dark Matter

Extend the SM field content by one colour-neutral SU(2) $_{L}$ multiplet "X", considering the following possibilities:

- 1. X is a complex scalar doublet (with $U(1)_Y$ such that has neutral comp.)
- 2. X is a Majorana fermion triplet (Wino-like)
- 3. X is a Dirac fermion fourplet (with $U(1)_Y$ such that has neutral comp.)
- 4. X is a Majorana fermion quintuplet

Which of these choices respects the SM Accidental symmetries* at d=4?

Which one also respects, at d=4, an accidental Z_2 symmetry under which X is odd and all SM particles are even?

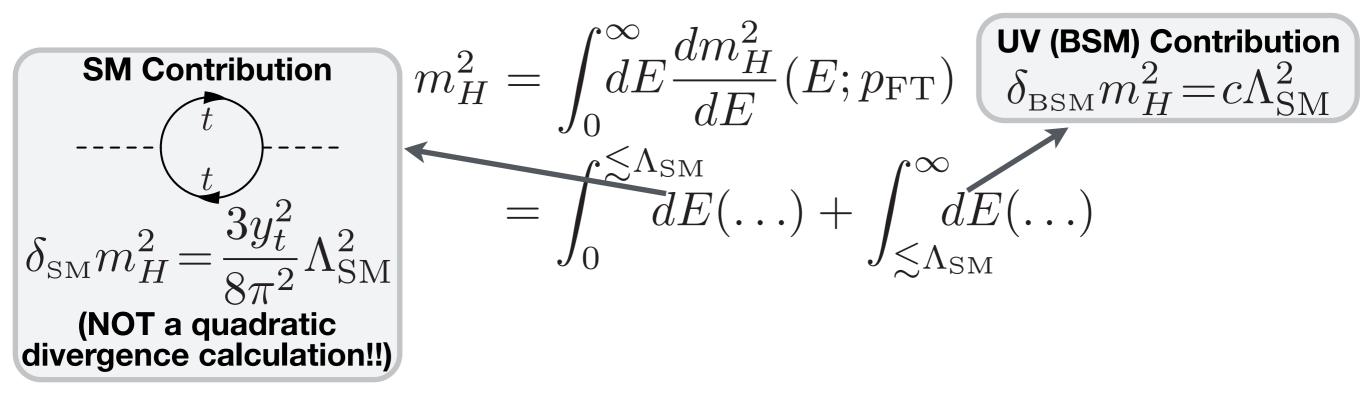
Which one breaks the accidental Z_2 symmetry at d=5? Which one at d=6? Denoting Λ_X the cutoff of the SM + X theory, estimate the lifetime of the lightest particle of the X multiplet in the two cases.

* the quark flavour group, broken only by the Yukawa's, is also an accidental symmetry

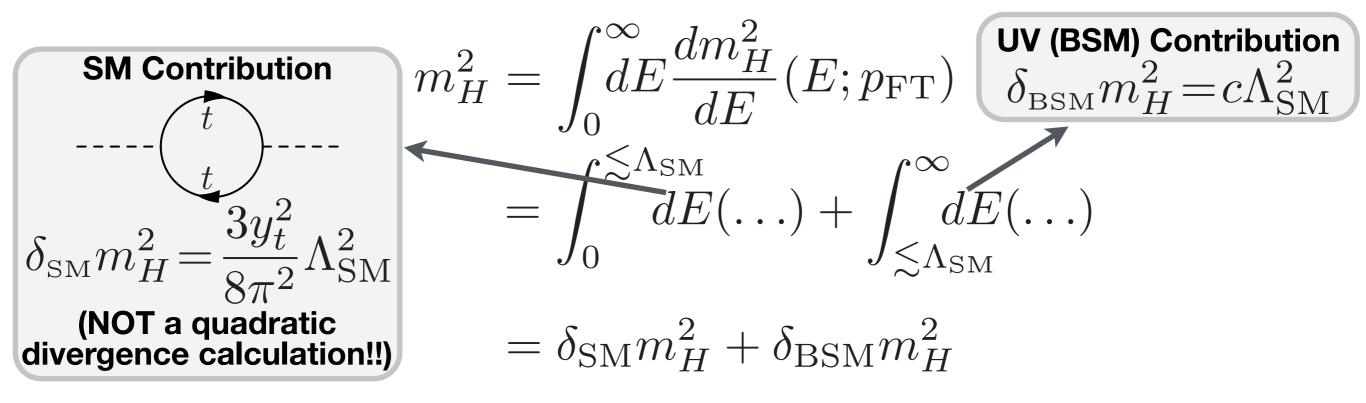
$$m_H^2 = \int_0^\infty dE \frac{dm_H^2}{dE} (E; p_{\rm FT})$$

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$$\begin{split} m_{H}^{2} &= \int_{0}^{\infty} \! dE \frac{dm_{H}^{2}}{dE}(E;p_{\rm FT}) & \begin{array}{l} \text{UV (BSM) Contribution} \\ \delta_{\rm BSM} m_{H}^{2} = c \Lambda_{\rm SM}^{2} \\ \delta_{\rm BSM} m_{H}^{2} = c \Lambda_{\rm SM}^{2} \\ \end{array} \\ &= \int_{0}^{\lesssim \Lambda_{\rm SM}} \! dE(\ldots) + \int_{\lesssim \Lambda_{\rm SM}}^{\infty} \! dE(\ldots) \end{split}$$



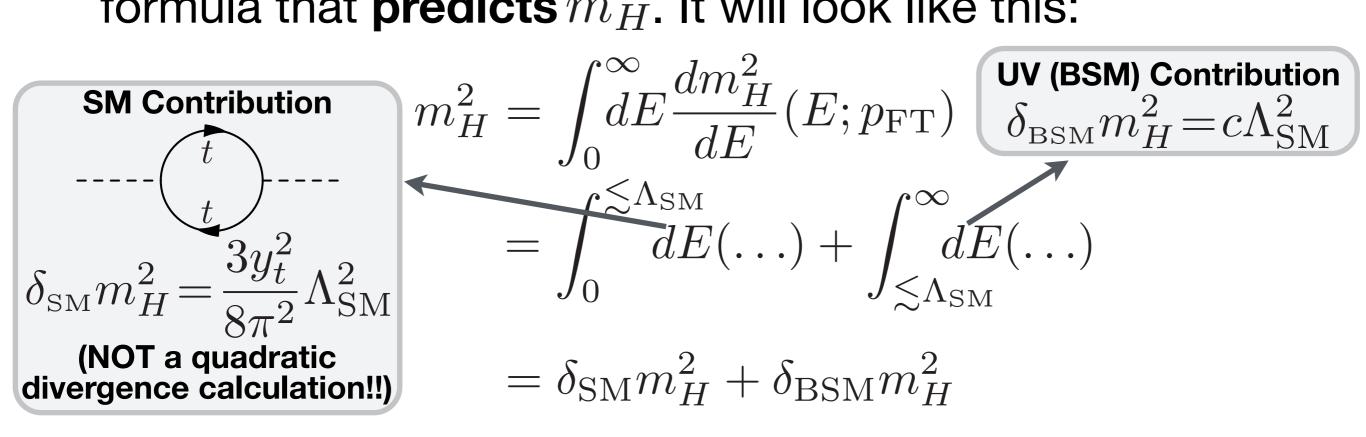
To understand Naturalness, think to the "Final Theory" formula that **predicts** m_H . It will look like this:



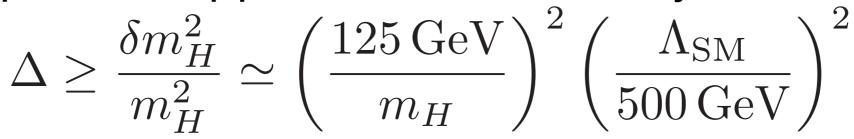
Since the result must be $(125 \,\mathrm{GeV})^2$, two terms must be ~ equal and opposite and cancel, by an amount

$$\Delta \ge \frac{\delta m_H^2}{m_H^2} \simeq \left(\frac{125\,\text{GeV}}{m_H}\right)^2 \left(\frac{\Lambda_{\text{SM}}}{500\,\text{GeV}}\right)^2$$

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Fine-tuning: quantifies the "degree of Un-Naturalness"

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 If we find it, go out and celebrate! (than come back and measure it better)

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Where to stop?

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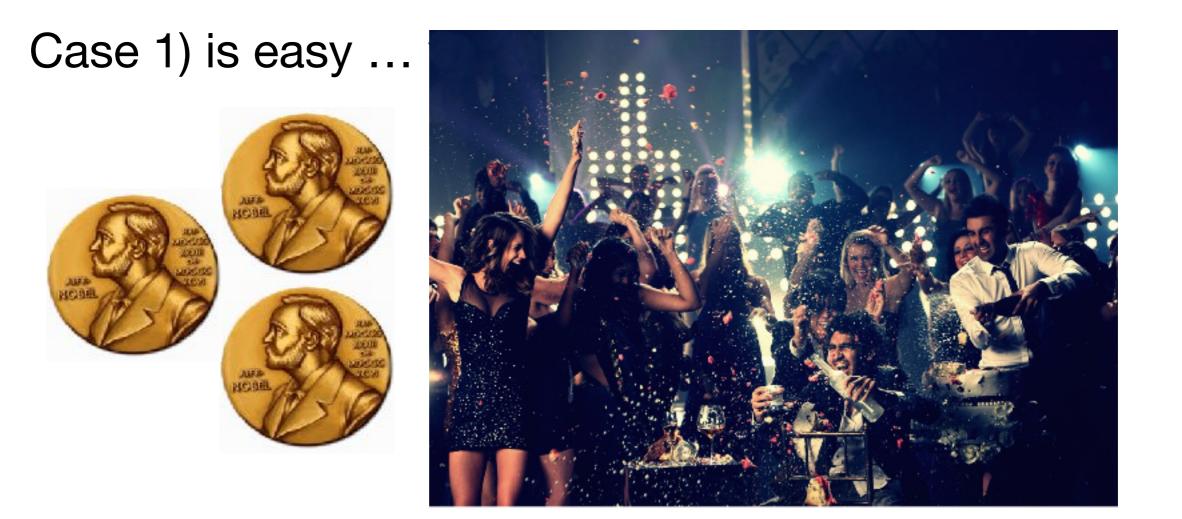
 $\Delta \sim 10$ definitely **OK** $\Delta \sim 1000$ probably **not OK**

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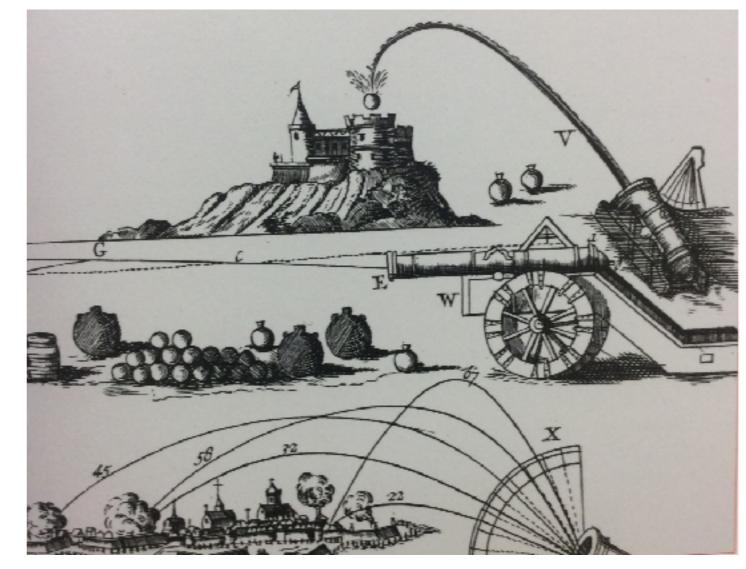
If Un-Natural, m_H has no **microscopic** origin (e.g. $\neq G_F$). It could:

- be a fundamental input par. of the Final Theory
- have environmental anthropic origin
- have dynamical (set by time evolution) origin

Environmental is a parameter whose value is dictated by external conditions

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Example is gravity of Earth $g = 9.81 \text{m/s}^2$. Fundamental input parameter of the theory of **Ballistics**.



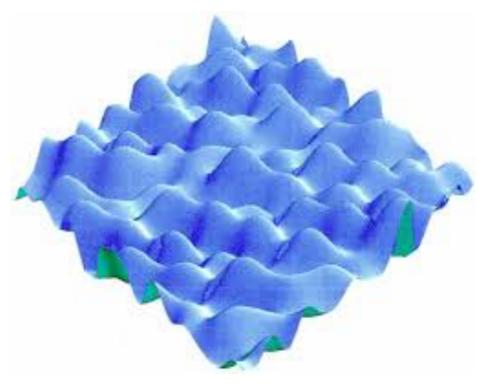
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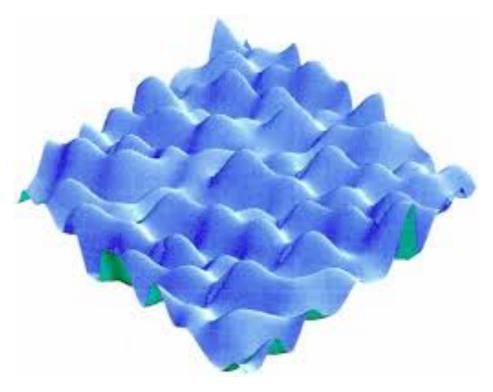
Higgs mass depends on the vacuum where we live.

Not quite like g. Vacua are **causally disconnected**. Cannot go there and check.

Landscape of vacua

Environmental is a parameter whose value is dictated by external conditions

Environmental in itself not a solution: why $m_H \ll \Lambda_{SM}$?

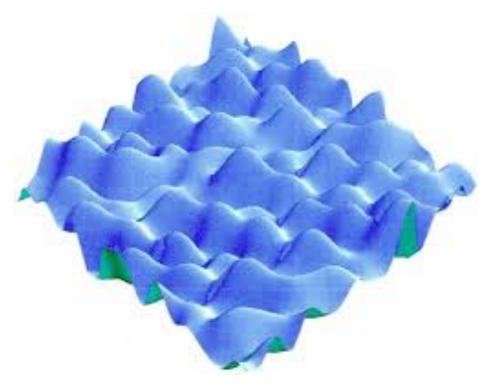


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Becomes solution only with anthropic selection: E.g., why 15°C is the average temperature of earth?

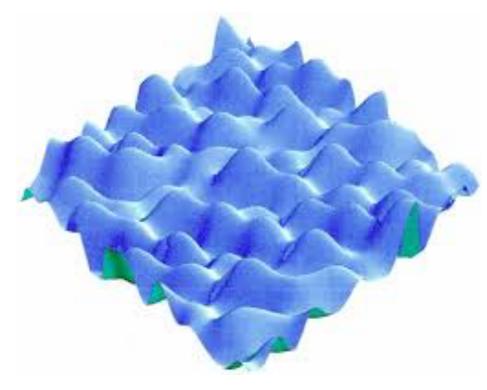


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We live where we can. There might be **upper bound** on m_H for us to exist.

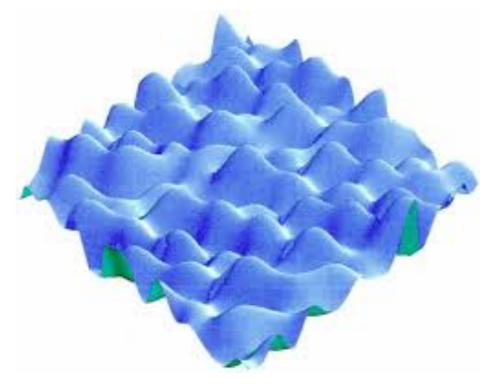
Landscape distribution peaks at $\Lambda_{\rm SM}$, but has a tail. Likely to live close to the upper bound.

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Successful Weinberg prediction of the Cosmological Constant: For galaxies to form, it must be: $\Lambda_{\rm c.c.} \lesssim ({\rm few} \cdot 10^{-3} {\rm eV})^4 \sim 10^{-120} M_P^4$

Observed value:

 $\Lambda_{\rm c.c.} \simeq (2 \cdot 10^{-3} {\rm eV})^4$

What if Un-Natural?

(to present-day understanding) [Graham, Kaplan, Rajendran, 2015]

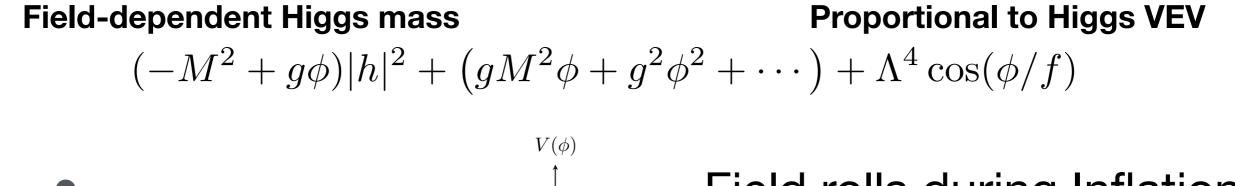
Dynamical is a parameter whose value is set by **time evolution**.

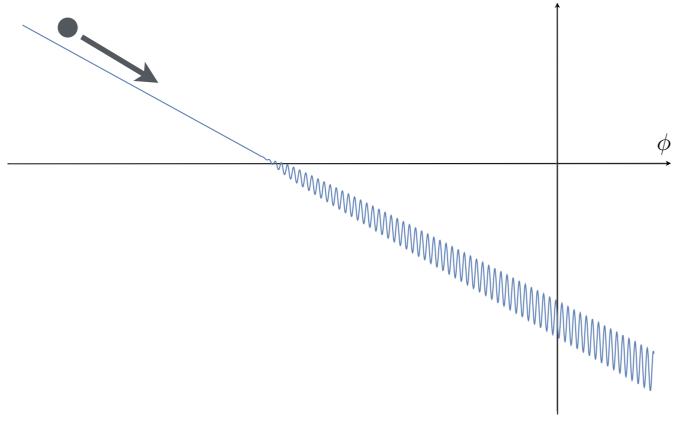
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Recent proposal: Relaxion





Field rolls during Inflation.

Stops right after $m_H^2 < 0$. Because of the cos term.

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