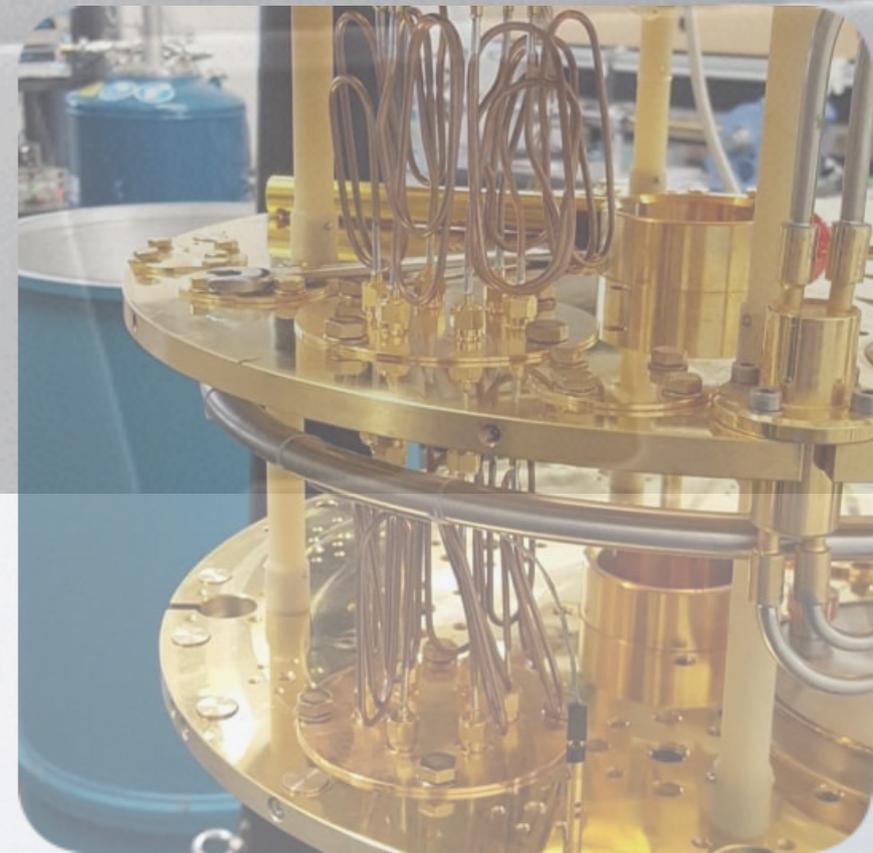


# SUPERCONDUCTING QUANTUM PROCESSORS

**Pol Forn-Díaz**

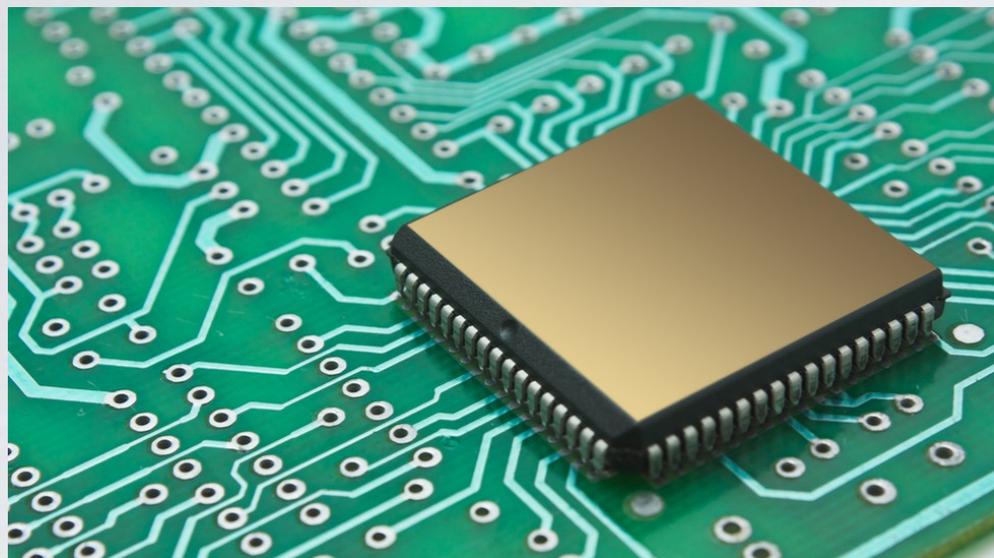
Colloquium IFAE  
11/03/2019



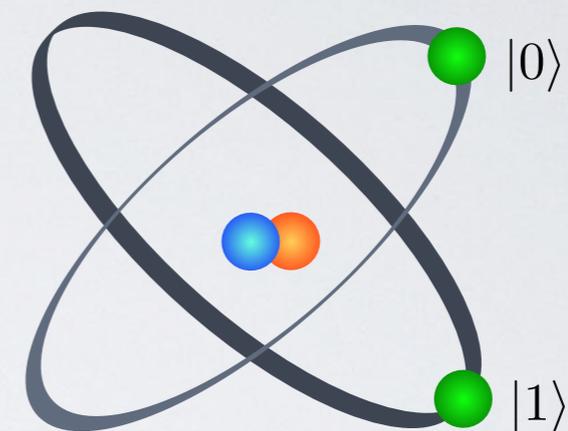
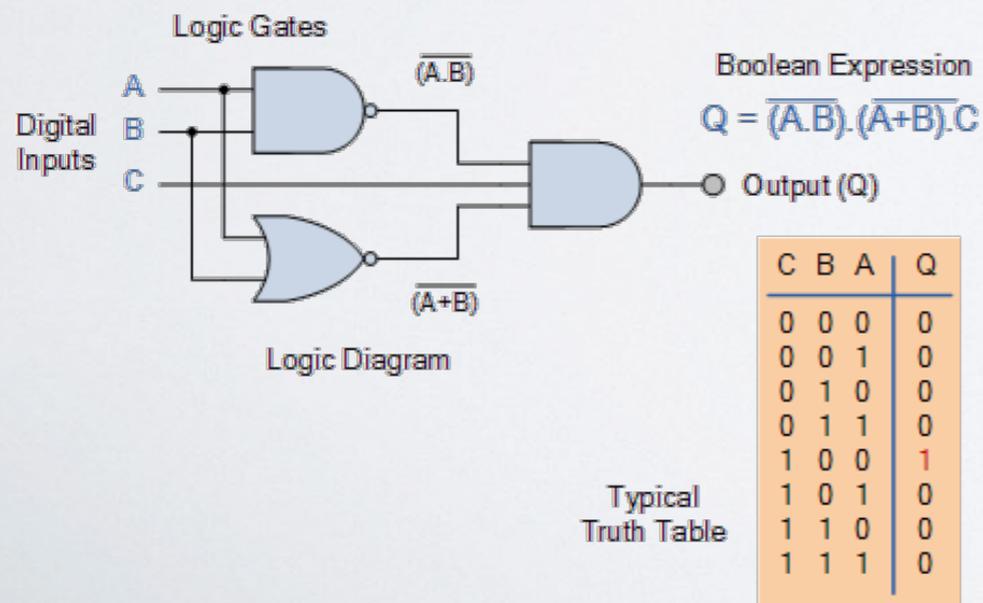
# OUTLINE

- **Q**uantum computation
- Superconducting qubits
- Qubit state control
- A superconducting quantum computer

# QUANTUM COMPUTATION



Classical systems can store information in classical variables (usually voltage).  
 Classical bit = minimal classical information unit with either of 2 options



Quantum systems can store information in their quantum states.  
 Quantum bit = qubit: minimal quantum information unit with 2 states

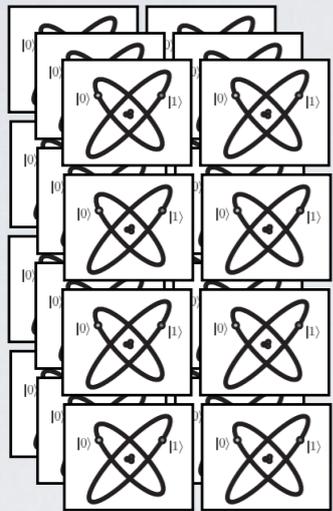
$$|\psi\rangle = \frac{|0\rangle + |1\rangle}{\sqrt{2}}$$

Qubit can live in a superposition of 0 **and** 1

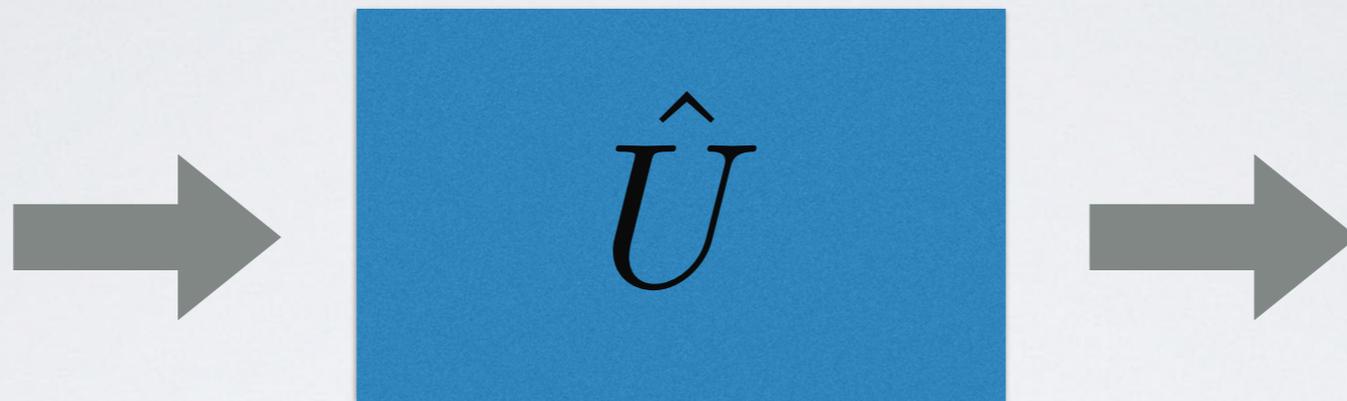
$$|\psi_N\rangle = \frac{1}{N^{1/2}} \prod_{i=1}^N (|0_i\rangle + |1_i\rangle)$$

# QUANTUM COMPUTATION

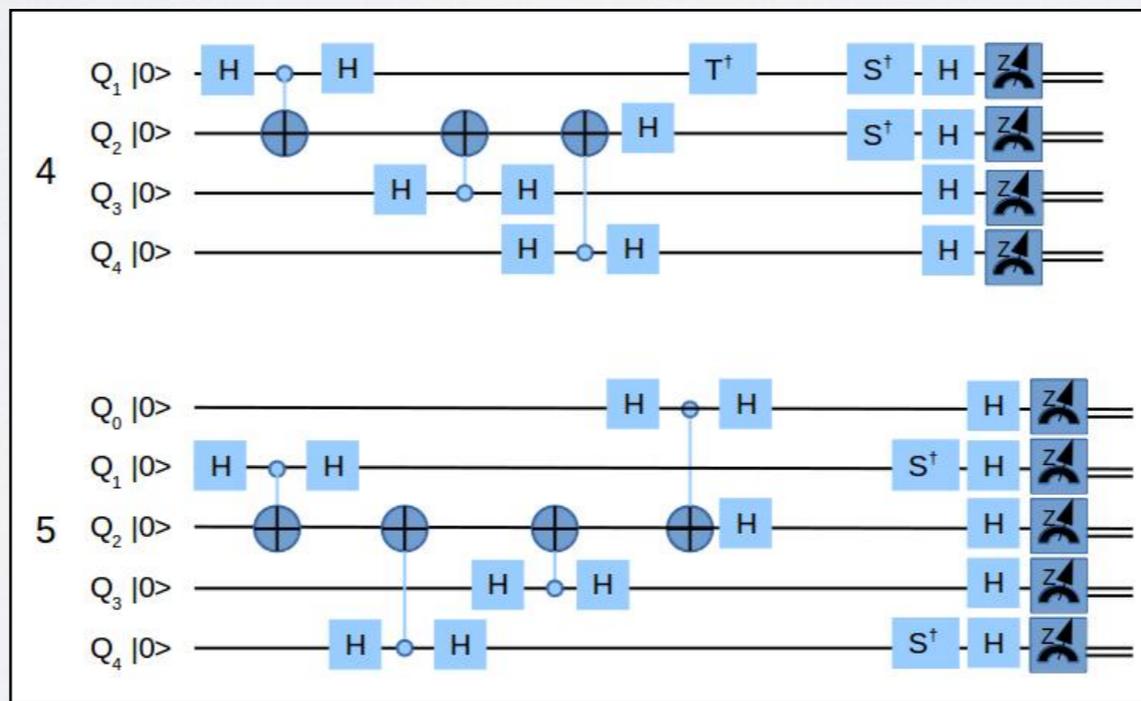
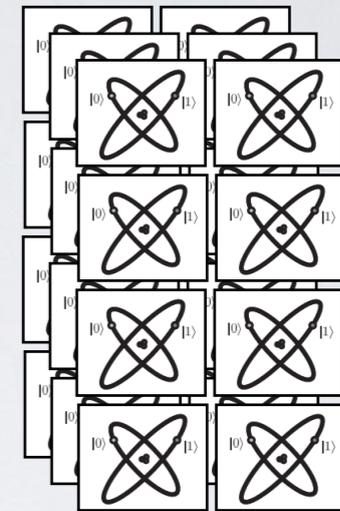
$|\Psi(0)\rangle$



Universal Quantum Computer



$|\Psi(t)\rangle$



Quantum gates circuit

Processing  $2^N$   
states simultaneously

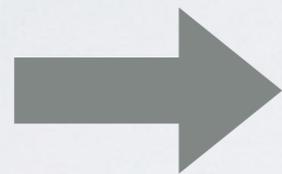
CONS:  
Requires quantum  
error correction:  $\sim 10^6$   
Long-term

PROS:  
Applicable to any  
quantum algorithm

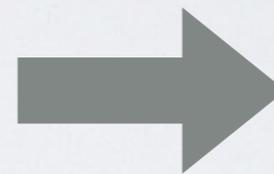
# QUANTUM COMPUTATION

## Adiabatic Quantum Computer

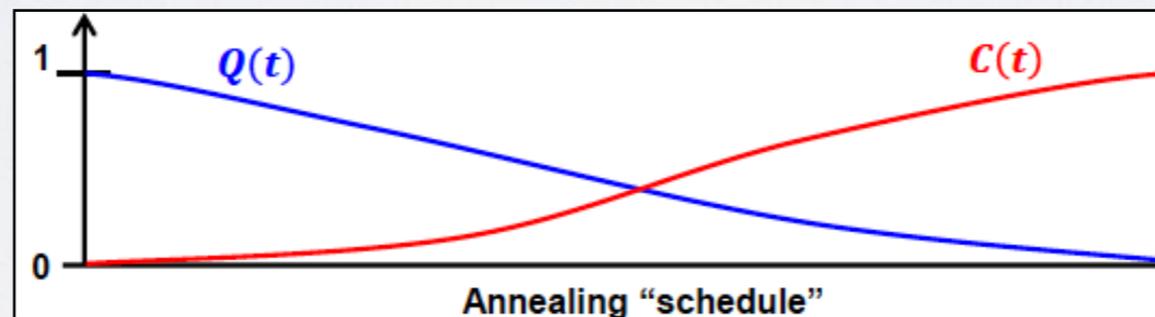
$$|\Psi_{GS}(0)\rangle$$



$$\mathcal{H}(t)$$



$$|\Psi_{GS}(t)\rangle$$



Final complex ground state maps into solution of optimization problem

**PROS:**  
Does not require quantum error correction.  
Near-term applications

$$\mathcal{H}(t) = Q(t)\mathcal{H}_D + C(t)\mathcal{H}_P$$

Trivial                      Problem

**CONS:**  
Non universal processor, only optimization problems

# QUANTUM COMPUTATION

Why do we need Quantum Computers?



390 TB ~ 51 qubits

Quantum supremacy (US)

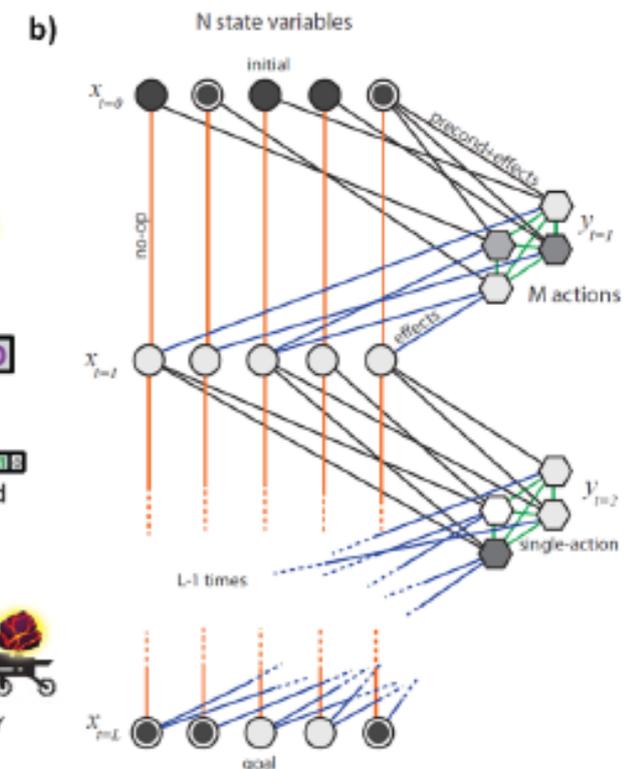
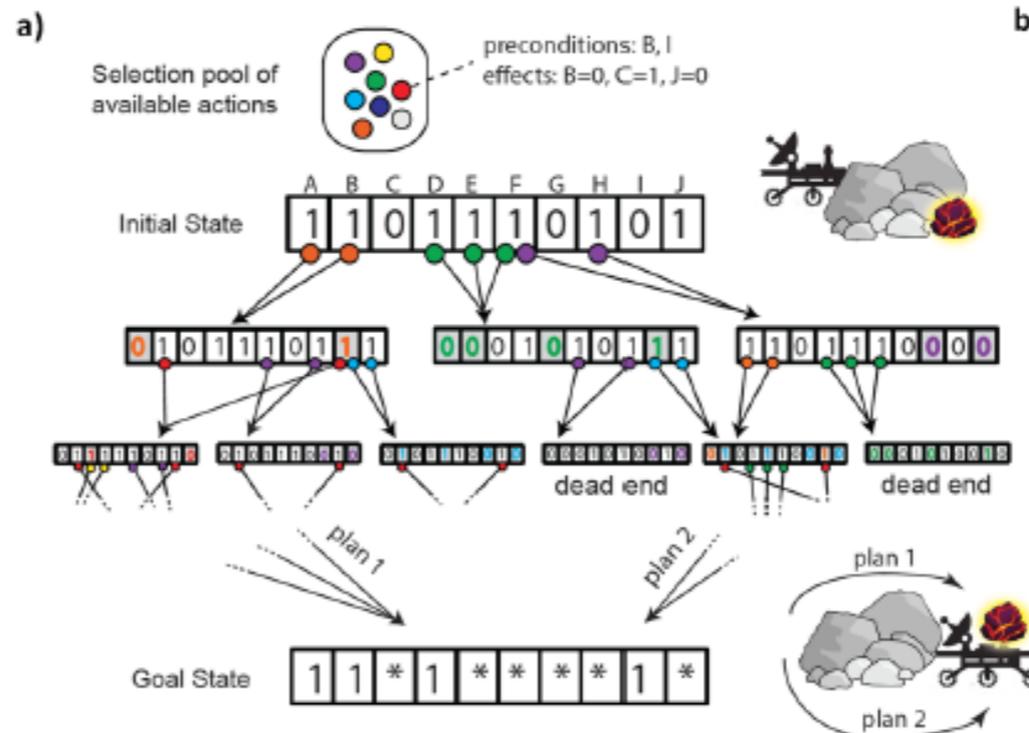
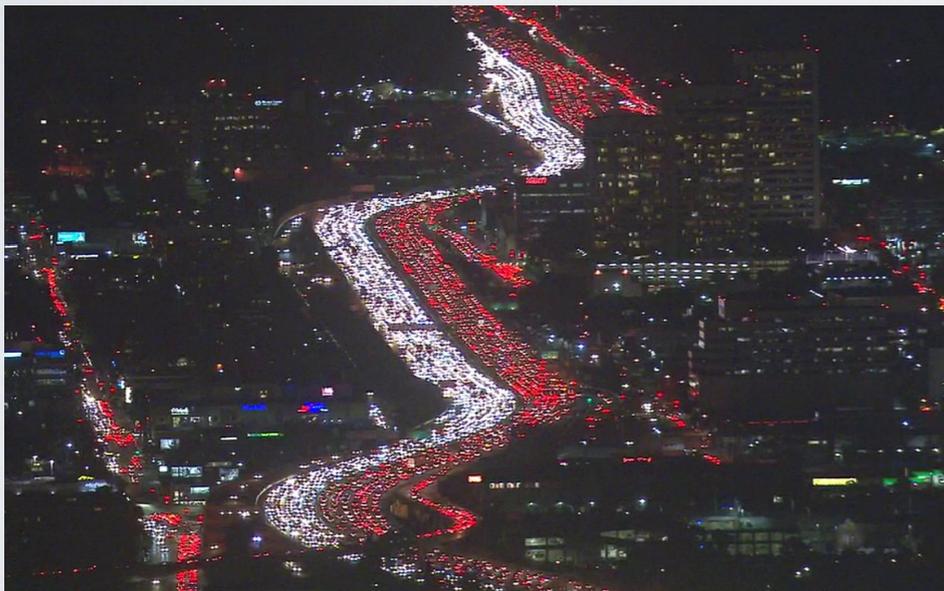
Quantum advantage (EU):  
outperforming classical  
computation

MareNostrum 4, Barcelona Supercomputing Center

# QUANTUM COMPUTATION

Why do we need small Quantum Computers?

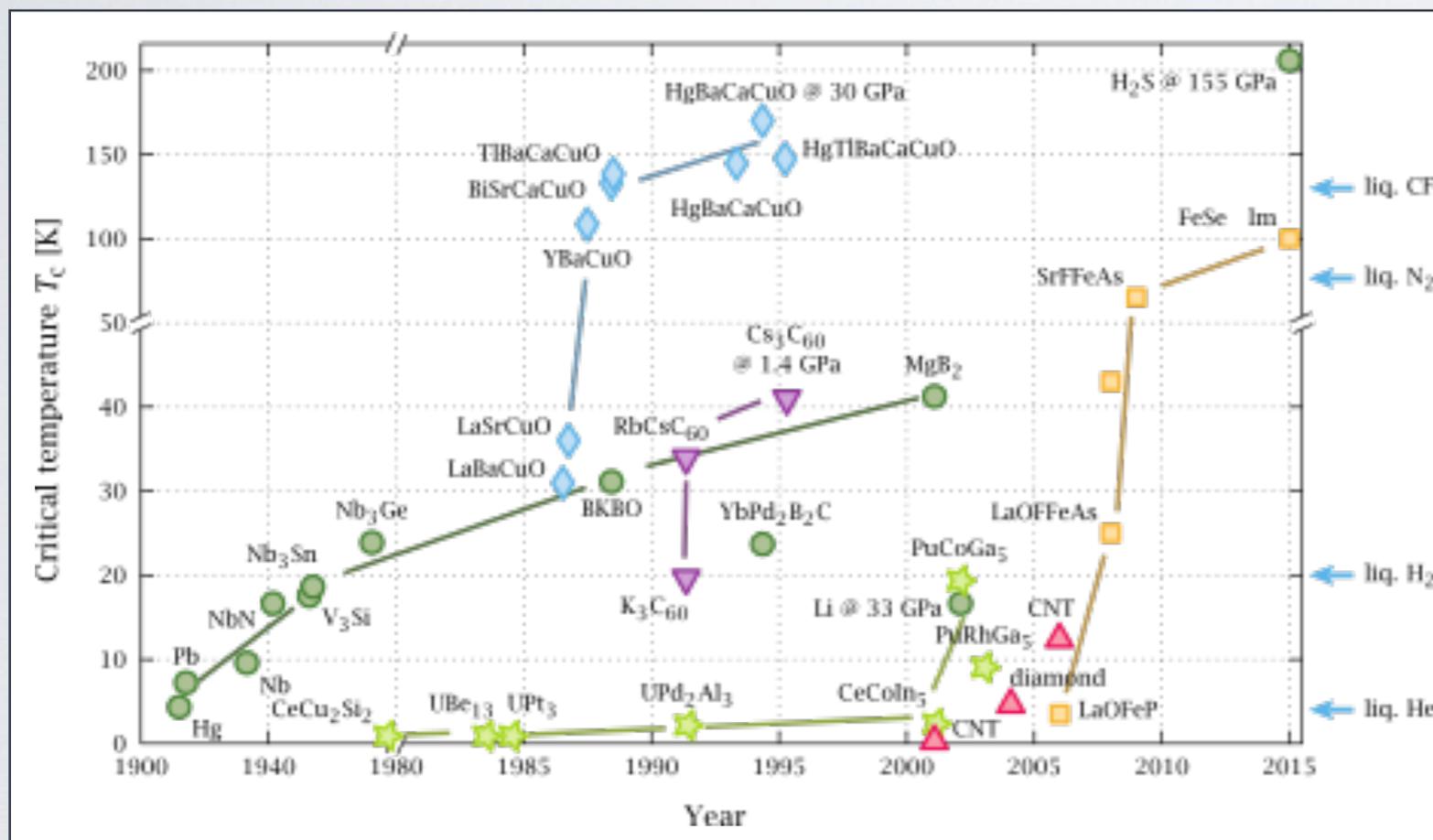
- Applications where small-sized quantum processors can outperform classical computers
- I. Optimization: traffic, navigation, scheduling, machine learning, etc.



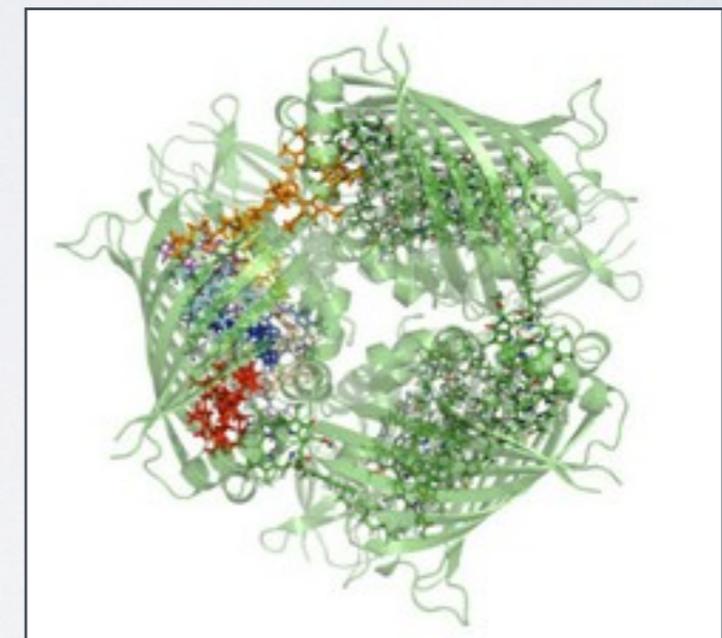
# QUANTUM COMPUTATION

Why do we need larger Quantum Computers?

- Applications where mid-sized quantum processors can outperform classical computers
- 2. Simulation: new materials, high energy physics, quantum chemistry, stock options, etc.



Simulate higher- $T_c$  superconductors



FMO complex, light energy harvesting

But also new fertilizers, gases to capture CO<sub>2</sub>, improve balance portfolios...

# QUANTUM COMPUTATION

Why do we need large-scale Quantum Computers?

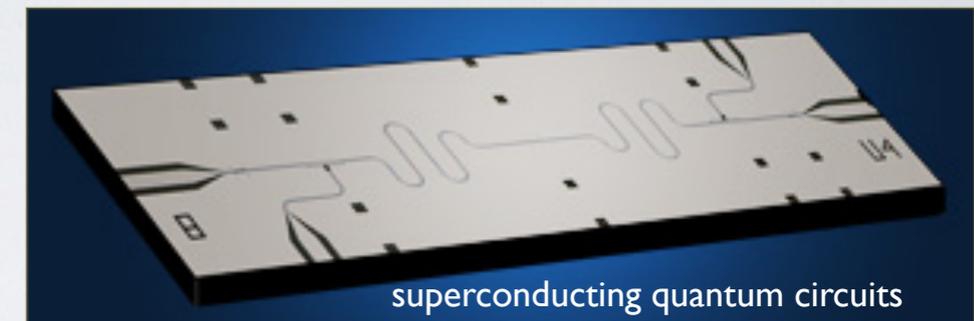
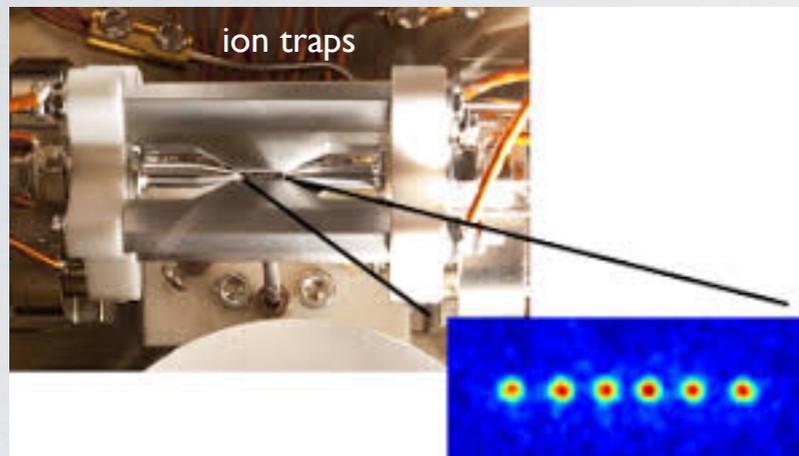
- Applications for universal quantum computers:
  1. Breaking RSA encryption codes
  2. Efficient search in massive data sets,
  3. Inversion of giant matrices
  4. ...



...and so much we do not know!

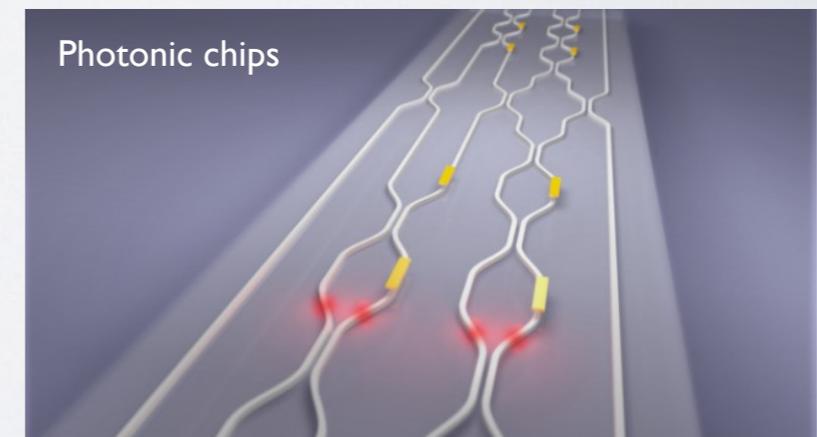
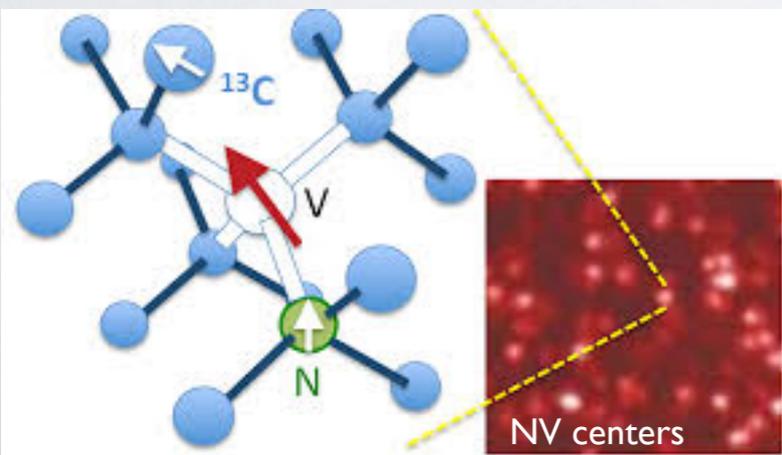
# QUANTUM COMPUTATION

But how close are we to all this?



2017: Quantum supremacy:  
outperforming classical computation

- 2024: Noisy Intermediate Scale quantum processors
- 2030: Universal quantum computers



# OUTLINE

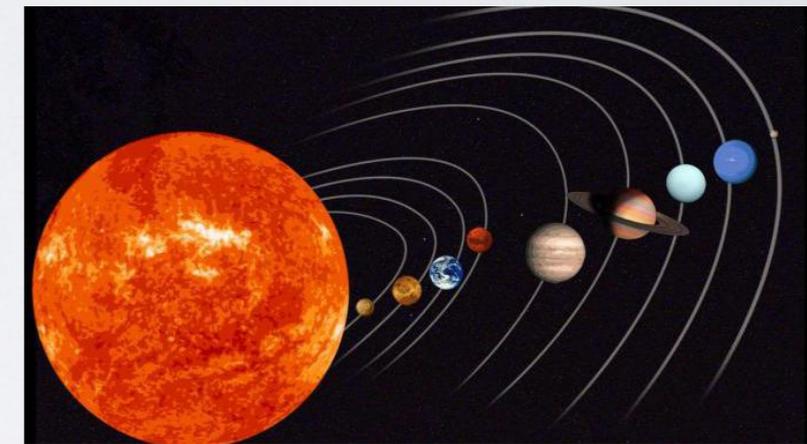
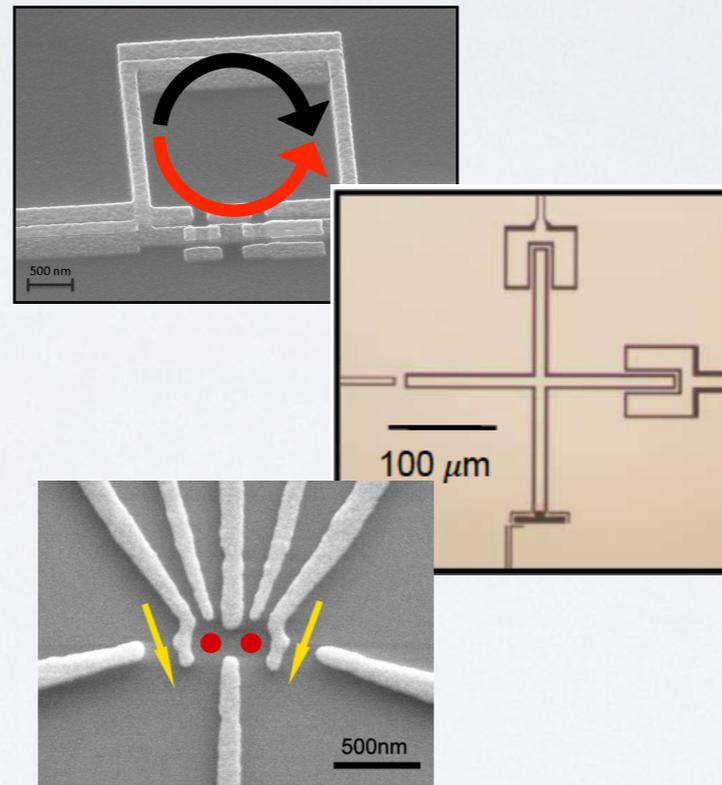
- Quantum computation
- **S**uperconducting qubits
- Qubit state control
- A superconducting quantum computer

# SUPERCONDUCTING QUBITS

Microscopic

Mesoscopic

Macroscopic



$$i\hbar \frac{\partial \psi(\vec{r}, t)}{\partial t} = \mathcal{H}(\vec{r}, t) \psi(\vec{r}, t)$$

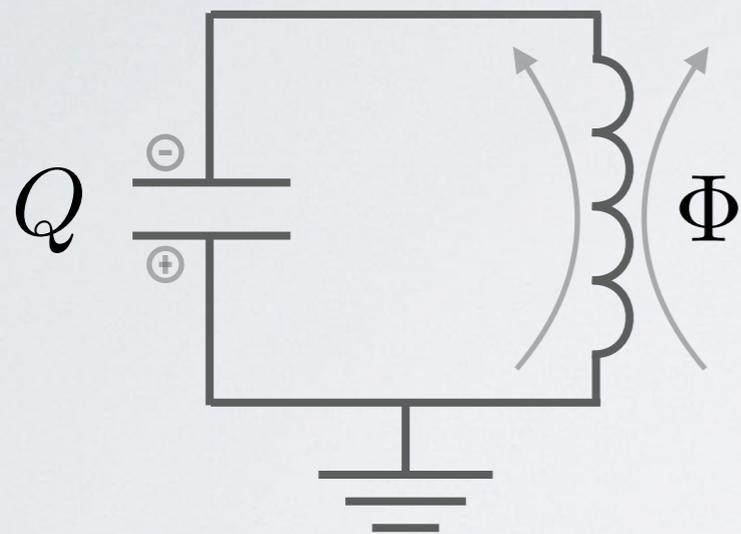
Large number of particles  
Artificial, man-made

Quantum collective degrees of freedom

$$\vec{F} = m\vec{a}$$

# SUPERCONDUCTING QUBITS

What corresponds to these collective degrees of freedom?



$$\mathcal{H} = \frac{Q^2}{2C} + \frac{\Phi^2}{2L}$$

$$\omega_{\text{LC}} = \frac{1}{\sqrt{LC}}$$

Analogous to mechanical oscillator

Quantum regime  $k_B T \ll \hbar \omega_{\text{LC}}$

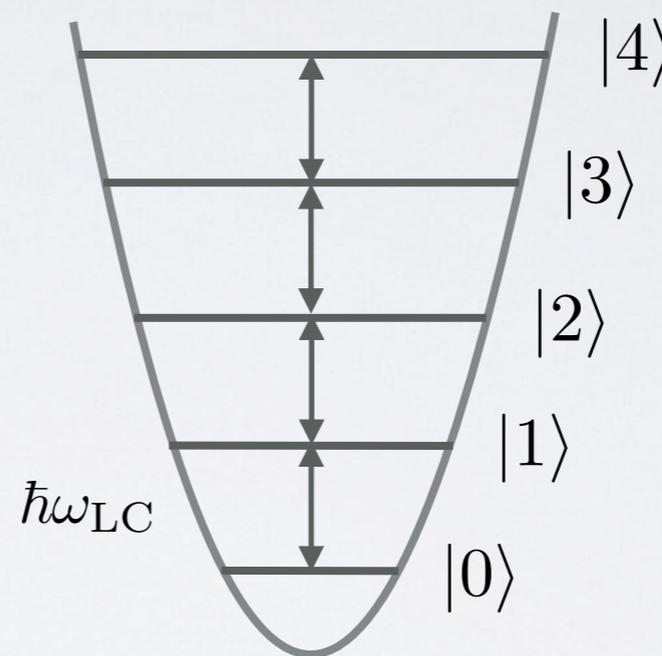
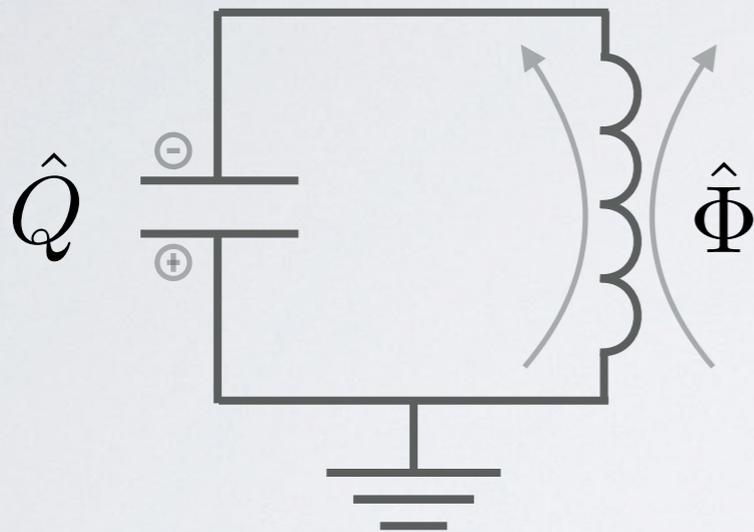
$$\begin{array}{c} \Phi \\ Q \end{array} \rightarrow \begin{array}{c} \hat{\Phi} \\ \hat{Q} \end{array}$$

$$[\hat{\Phi}, \hat{Q}] = i\hbar$$

Quantum fluctuations of collective d.o.f.!

# SUPERCONDUCTING QUBITS

Quantum circuit spectrum and energy levels

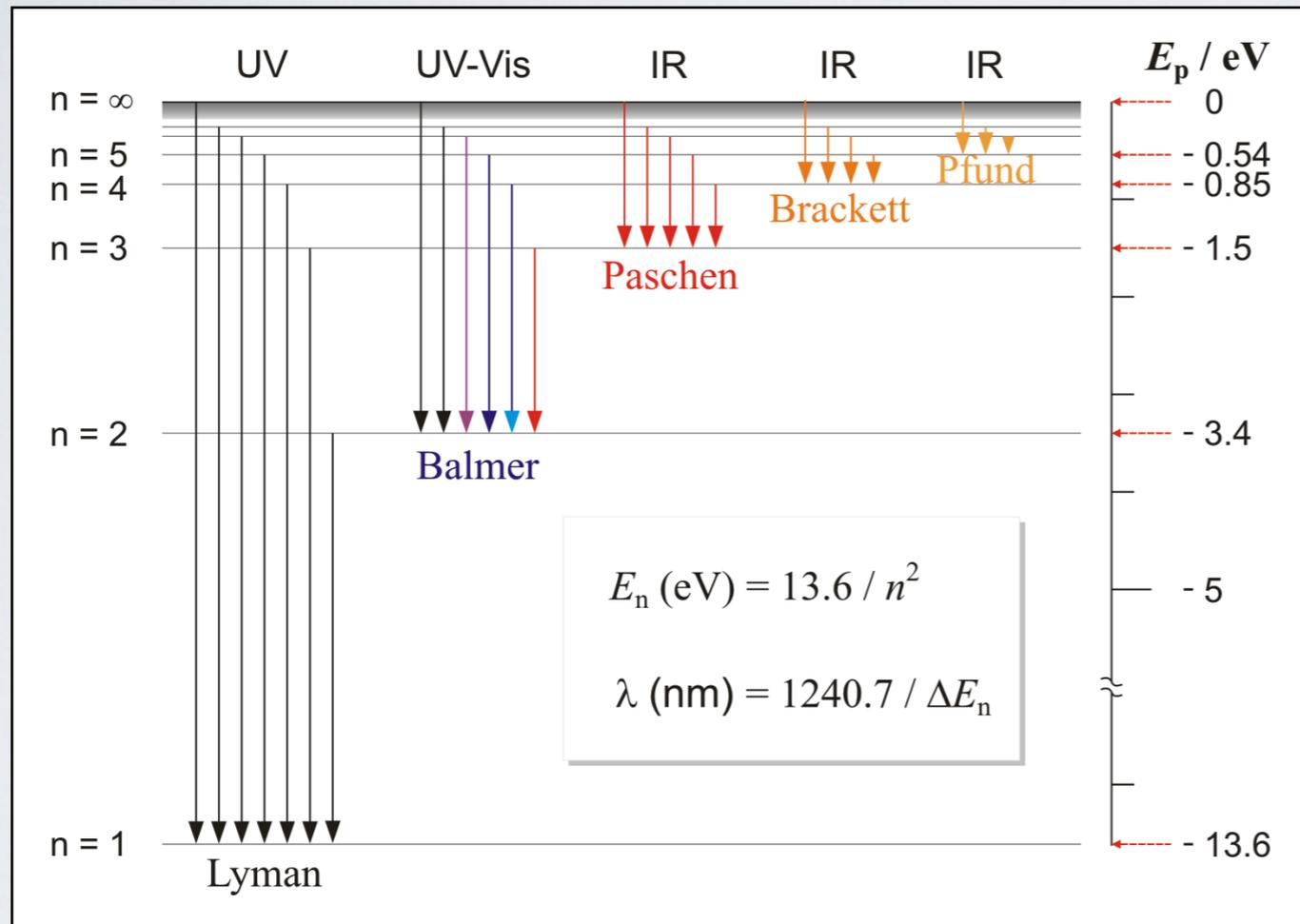


$Q \gg 1$   
Superconducting circuit

- We cannot single out a particular transition
- Not a proper quantum system for quantum information processing

# SUPERCONDUCTING QUBITS

## Hydrogen atom spectrum



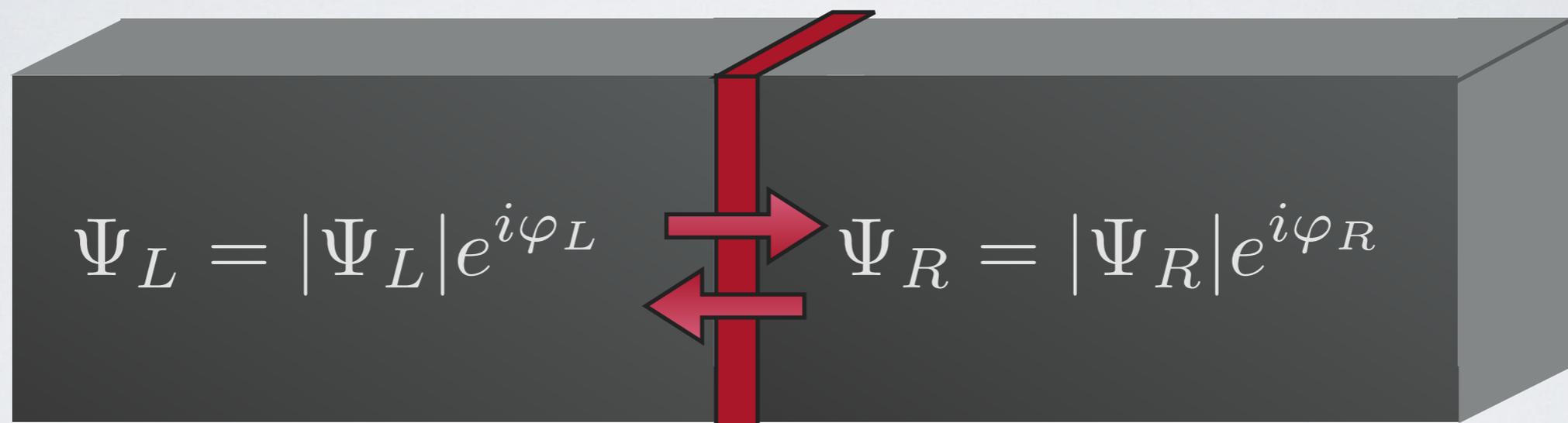
Source: <https://glossary.periodni.com>

Need nonlinear circuit element to alter circuit spectrum...

- Atomic spectra intrinsically anharmonic
- All transitions addressable by external radiation

# SUPERCONDUCTING QUBITS

Josephson junctions: a macroscopic quantum effect



Constituent relation:

$$\frac{dI}{dt} = V \frac{2\pi I_C}{\Phi_0} \sqrt{\frac{I_C^2 - I^2}{I_C^2}}$$

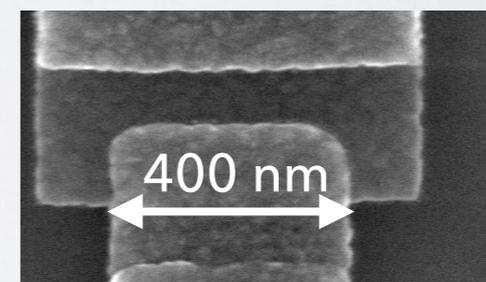
$$\equiv 1/L_J(I)$$

Josephson inductance

Electrical circuits symbol



- ▶ Nonlinear circuit element
- ▶ Lossless

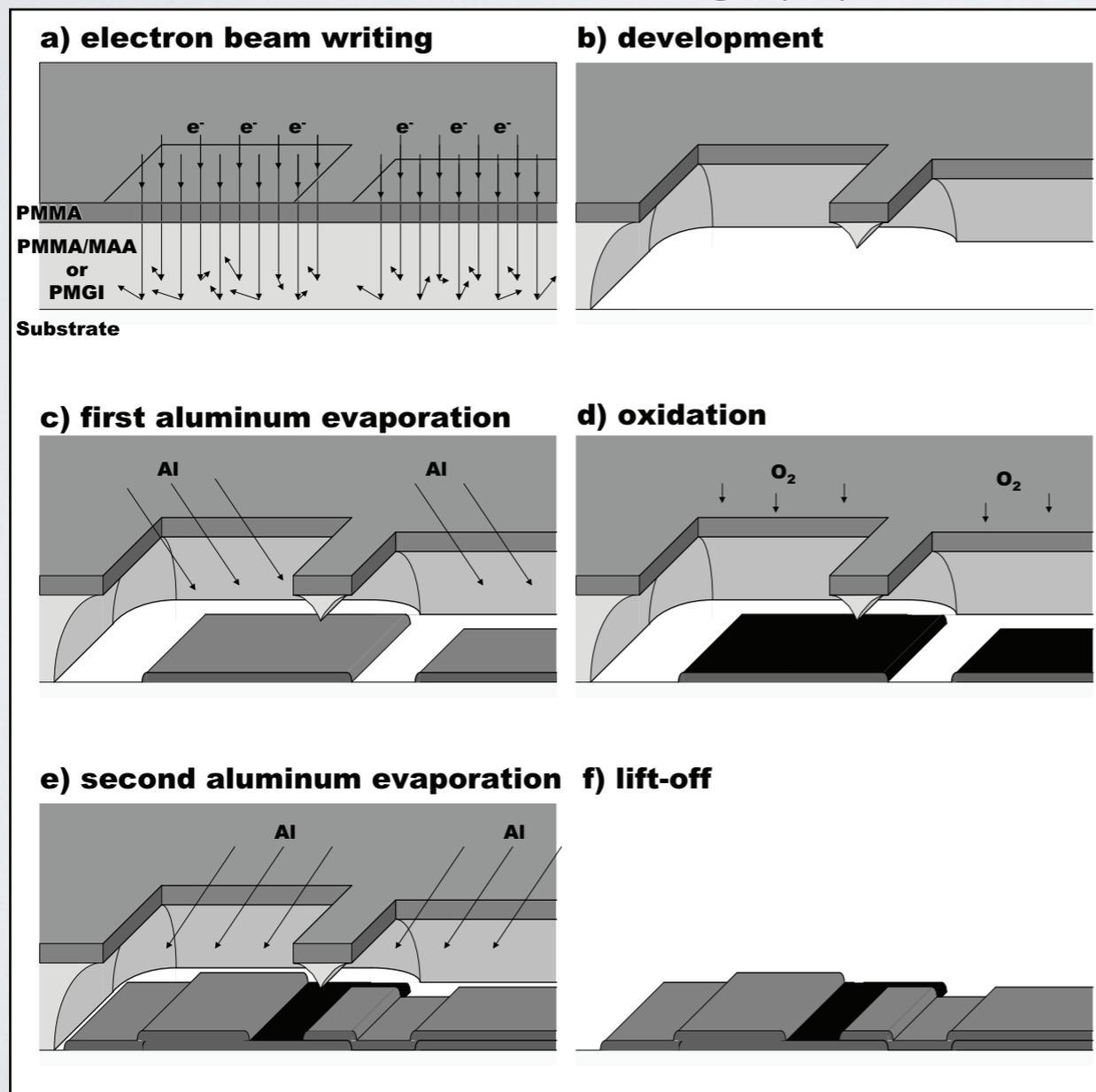


SEM micrograph

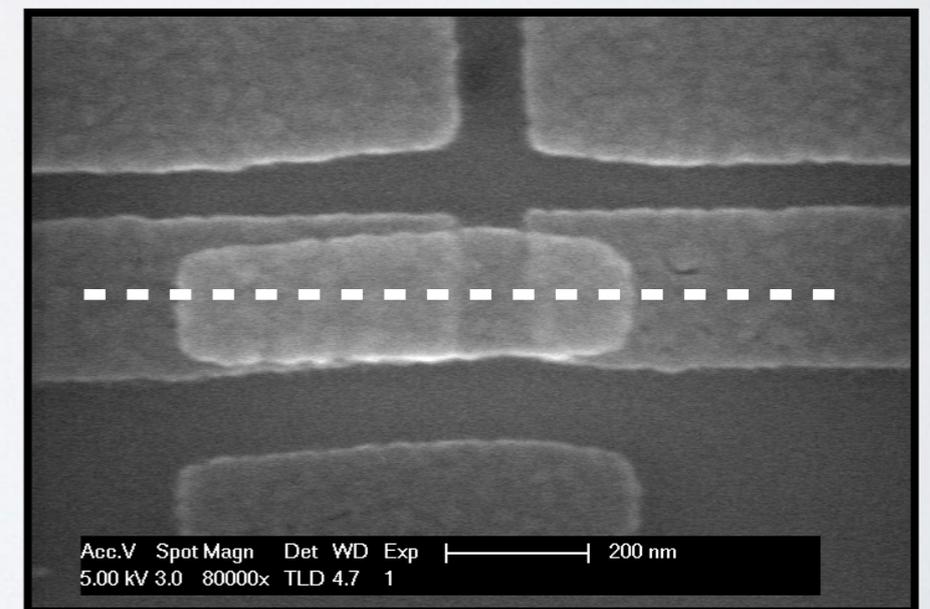
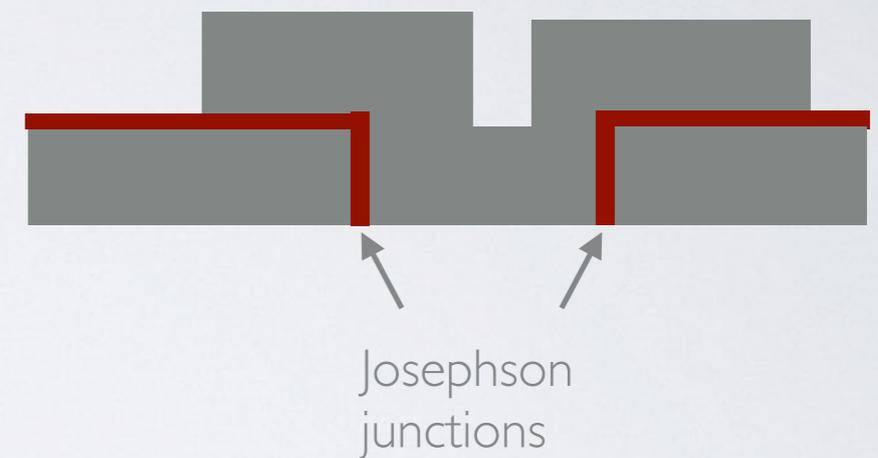
# SUPERCONDUCTING QUBITS

## Junction fabrication

### Electron beam lithography



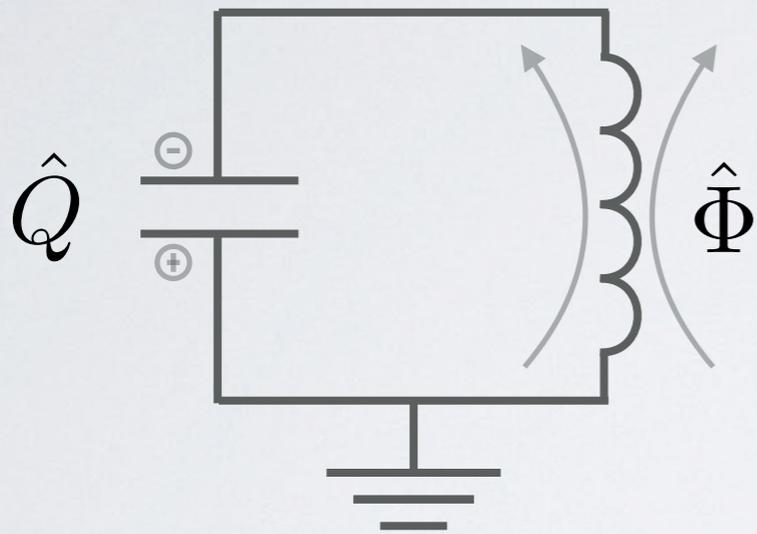
### Shadow angle evaporation



Scanning electron microscope (SEM)

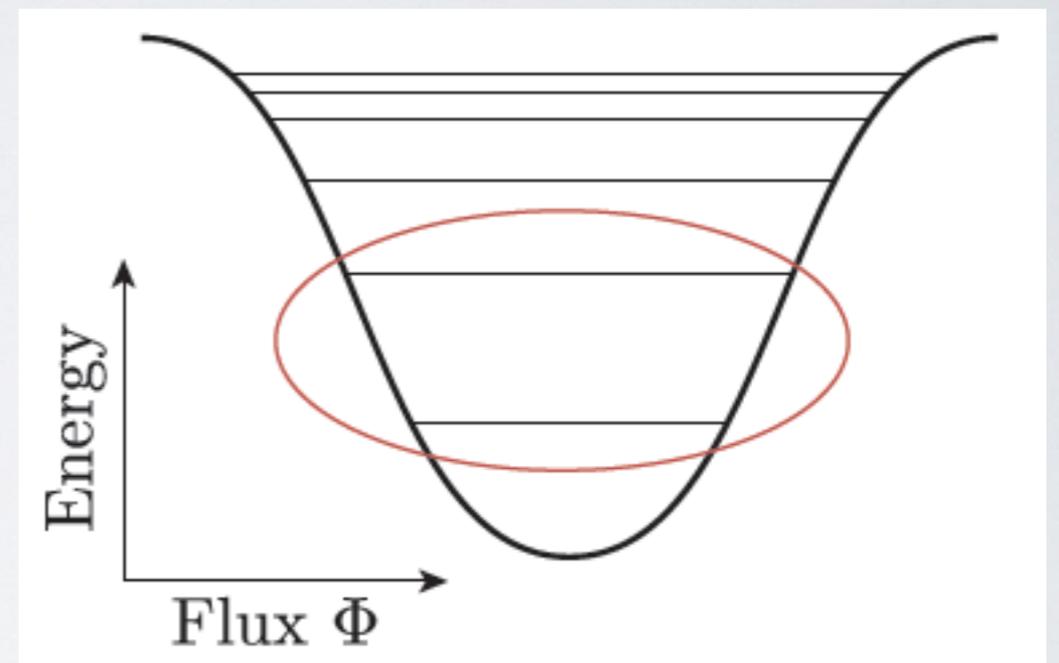
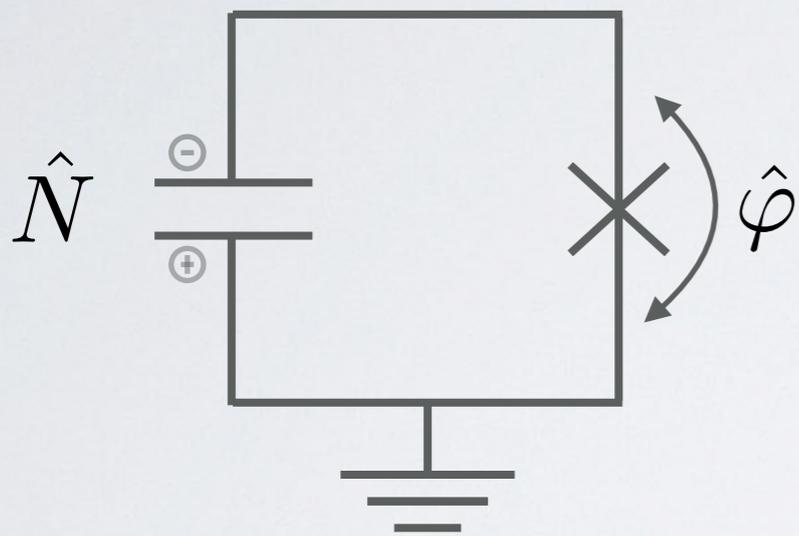
# SUPERCONDUCTING QUBITS

The hydrogen atom of superconducting qubits



# SUPERCONDUCTING QUBITS

The hydrogen atom of superconducting qubits



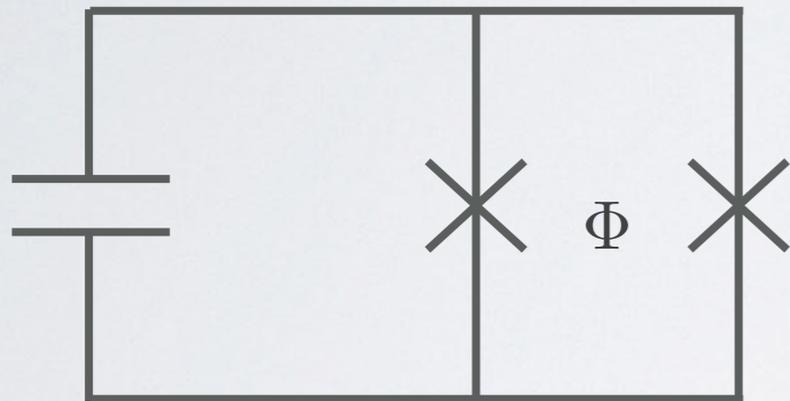
$$\hat{\mathcal{H}} = E_C \hat{N}^2 - E_J \cos(\hat{\varphi})$$

$$\simeq E_C \hat{N}^2 - E_J \left( -\frac{\hat{\varphi}^2}{2} + \frac{\hat{\varphi}^4}{4!} \right) - E_J$$

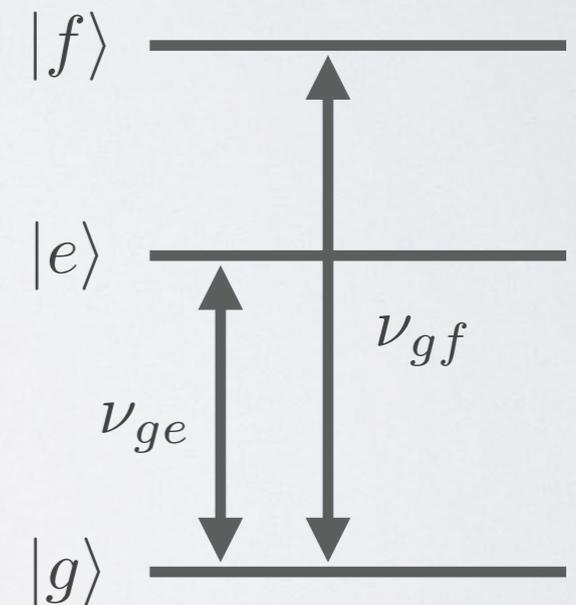
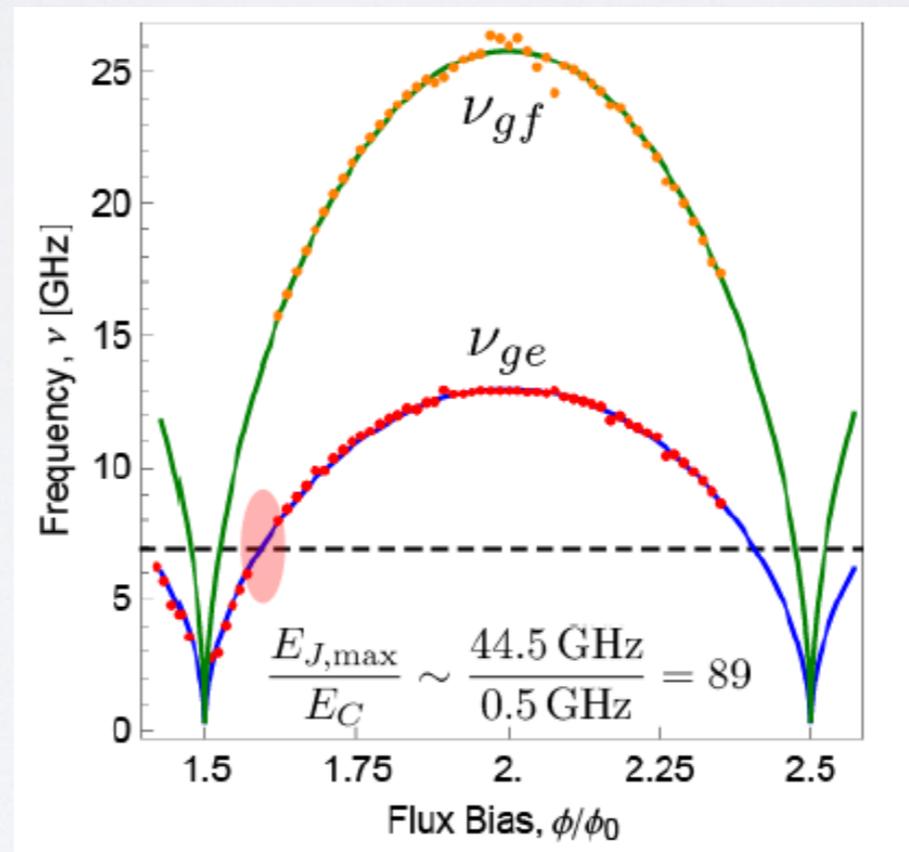
- Anharmonic spectrum
- Energy levels related to charge tunneling
- Lowest two states form a qubit

# SUPERCONDUCTING QUBITS

Transmon qubit



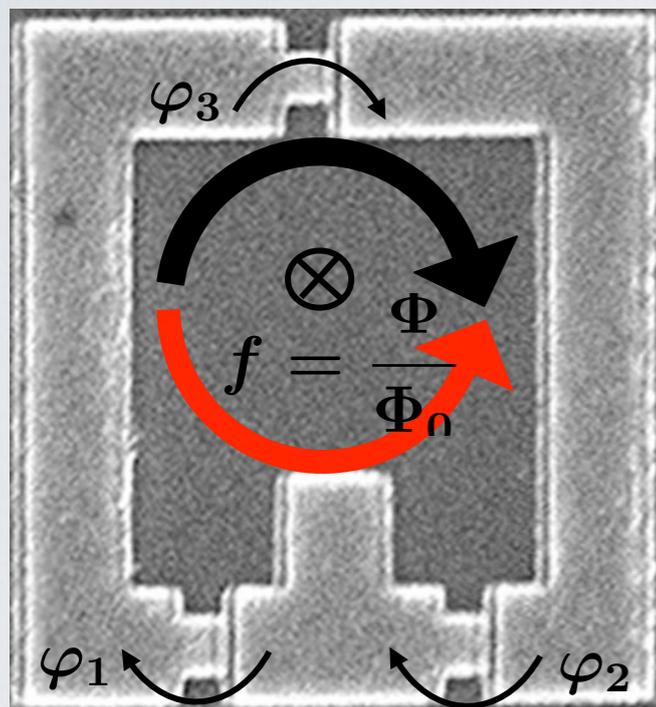
Flux dependence of energy levels



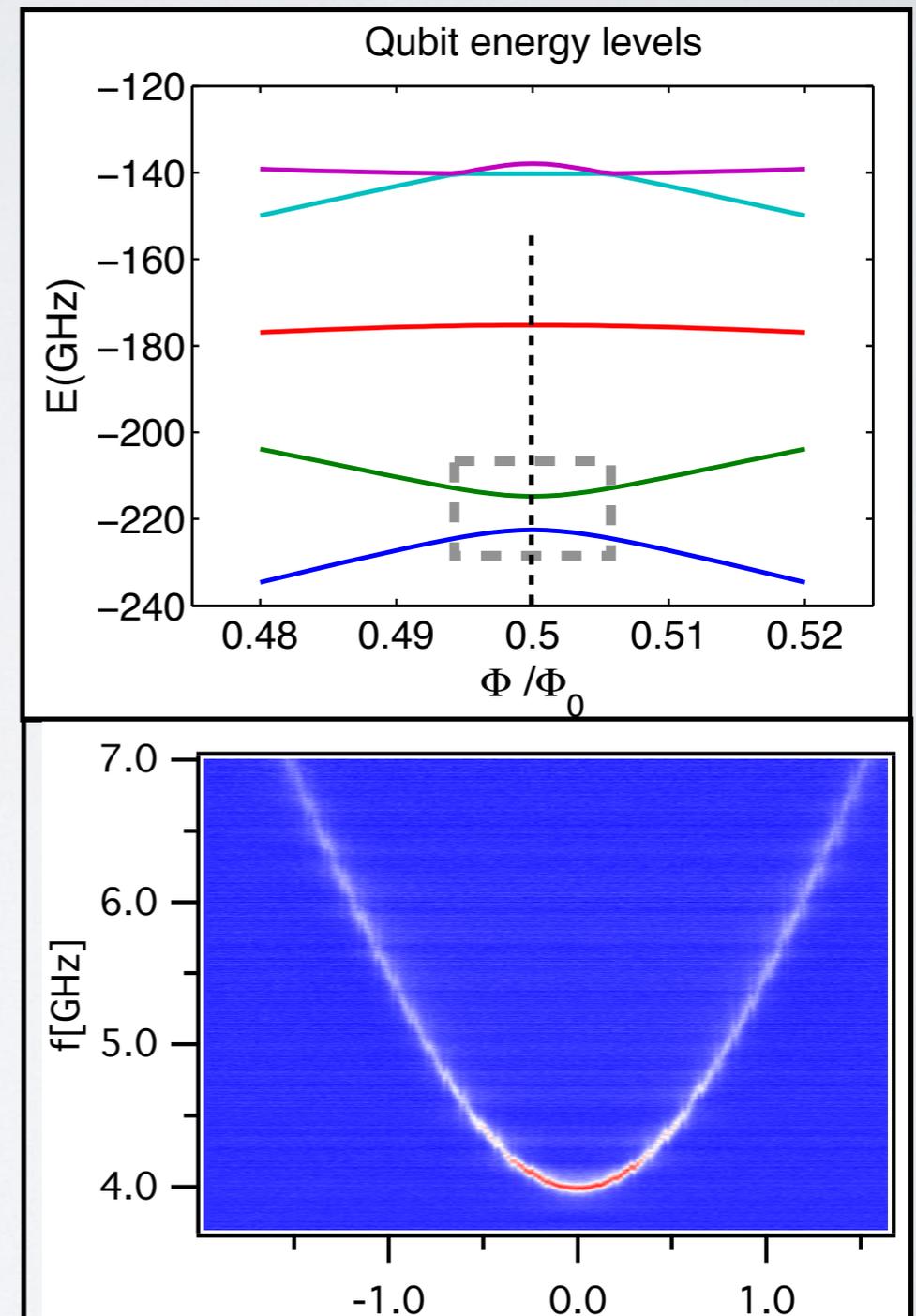
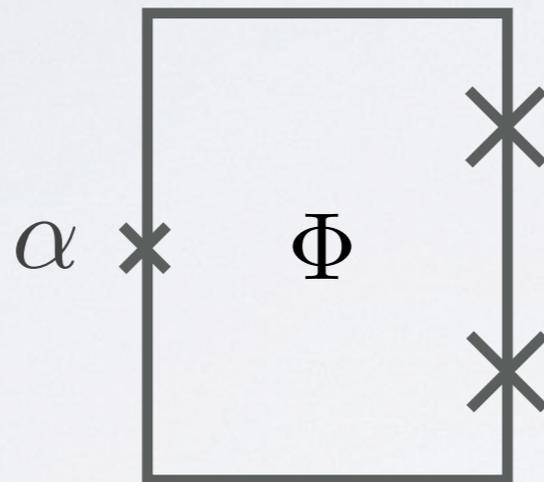
# SUPERCONDUCTING QUBITS

## Persistent current/Flux qubit

Aluminum loop with 3 Josephson junctions



Circuit diagram:



Highly **tuneable**: ideal for quantum annealing

*T. P. Orlando, et al. PRB 60 15398 (1999)*

*J. E. Mooij, et al. Science 285 1036 (1998)*

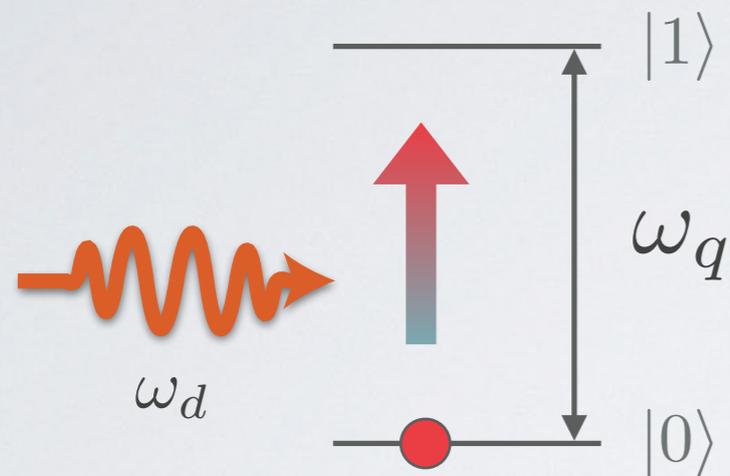
*Forn-Díaz et al., Nature Physics 13, 39 (2017)*

# OUTLINE

- Quantum computation
- Superconducting qubits
- **Q**ubit state control
- A superconducting quantum computer

# QUBIT STATE CONTROL

Single qubit microwave driving



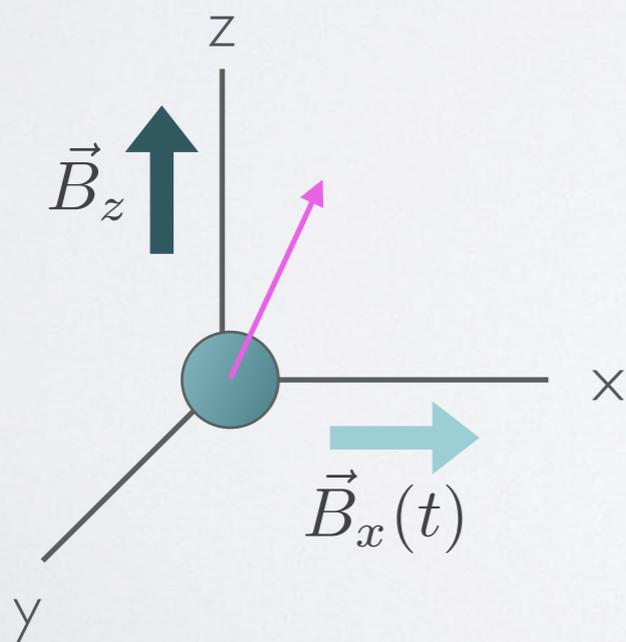
Rabi formula

$$P_{0 \rightarrow 1} = \frac{\Omega_R^2}{\Delta^2 + \Omega_R^2} \sin^2 \left( \sqrt{(\Delta^2 + \Omega_R^2)} t / \hbar \right)$$

$\Omega_R$  Rabi frequency "bare"

$\Delta \equiv \omega_q - \omega_d$  Detuning

Analogy with spin-1/2



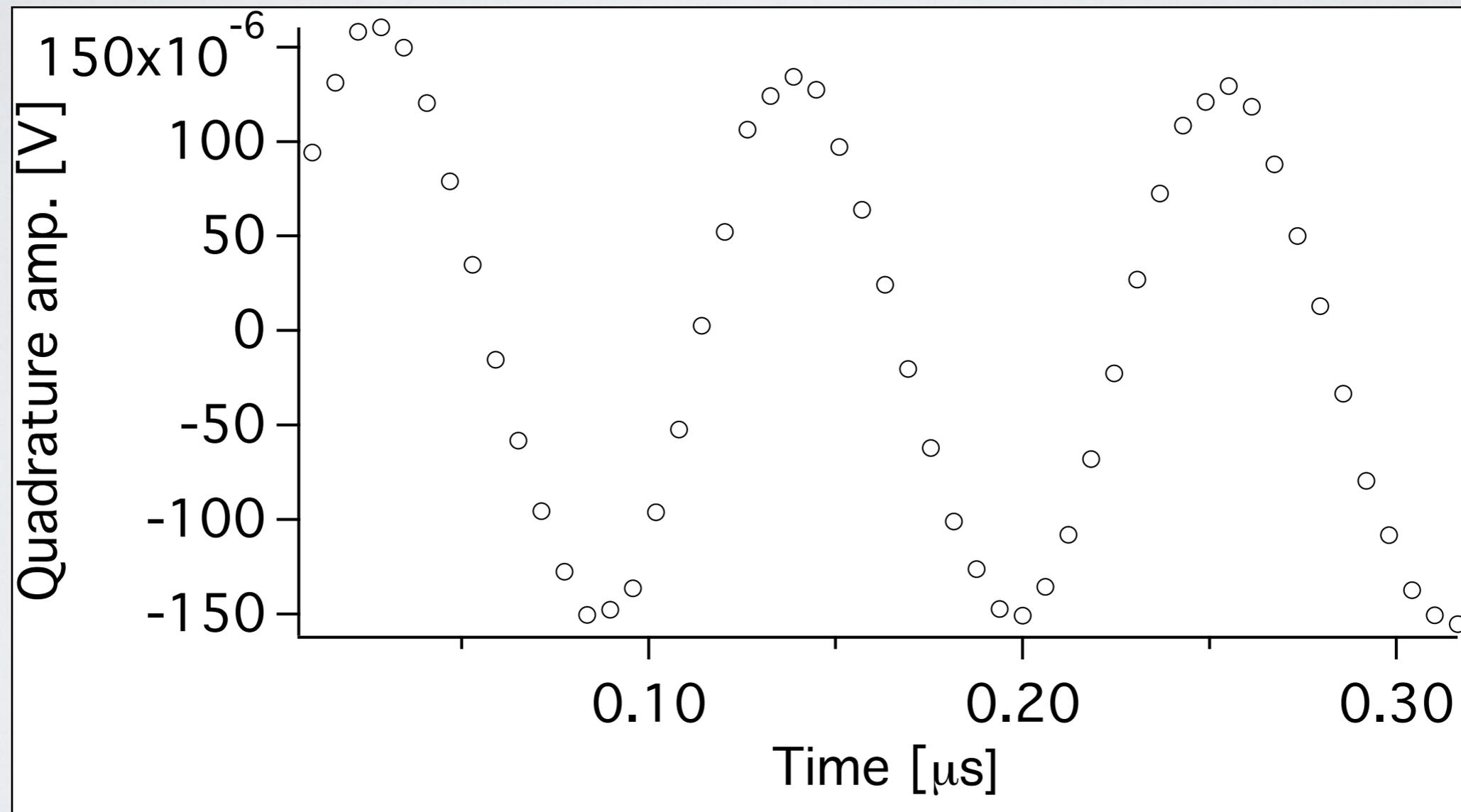
Import all NMR techniques for qubit state control...

*Quantum Mechanics, C. Tannoudji*

*Nielsen and Chuang, Quantum computation and Quantum information*

# QUBIT STATE CONTROL

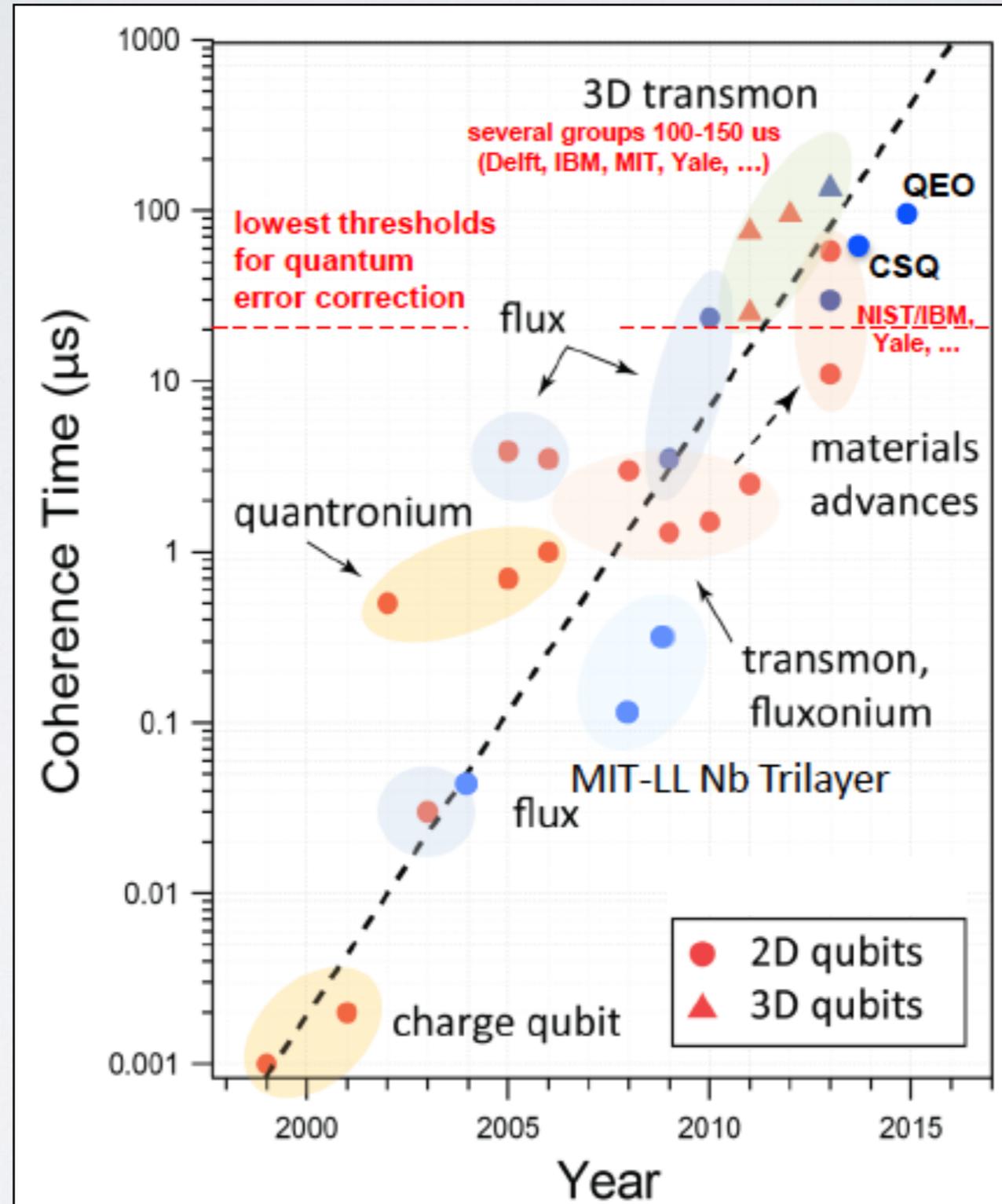
In a real experiment...



...it decays!

# QUBIT STATE CONTROL

A Moore's-like law



# QUBIT STATE CONTROL

## Superconducting qubit setup

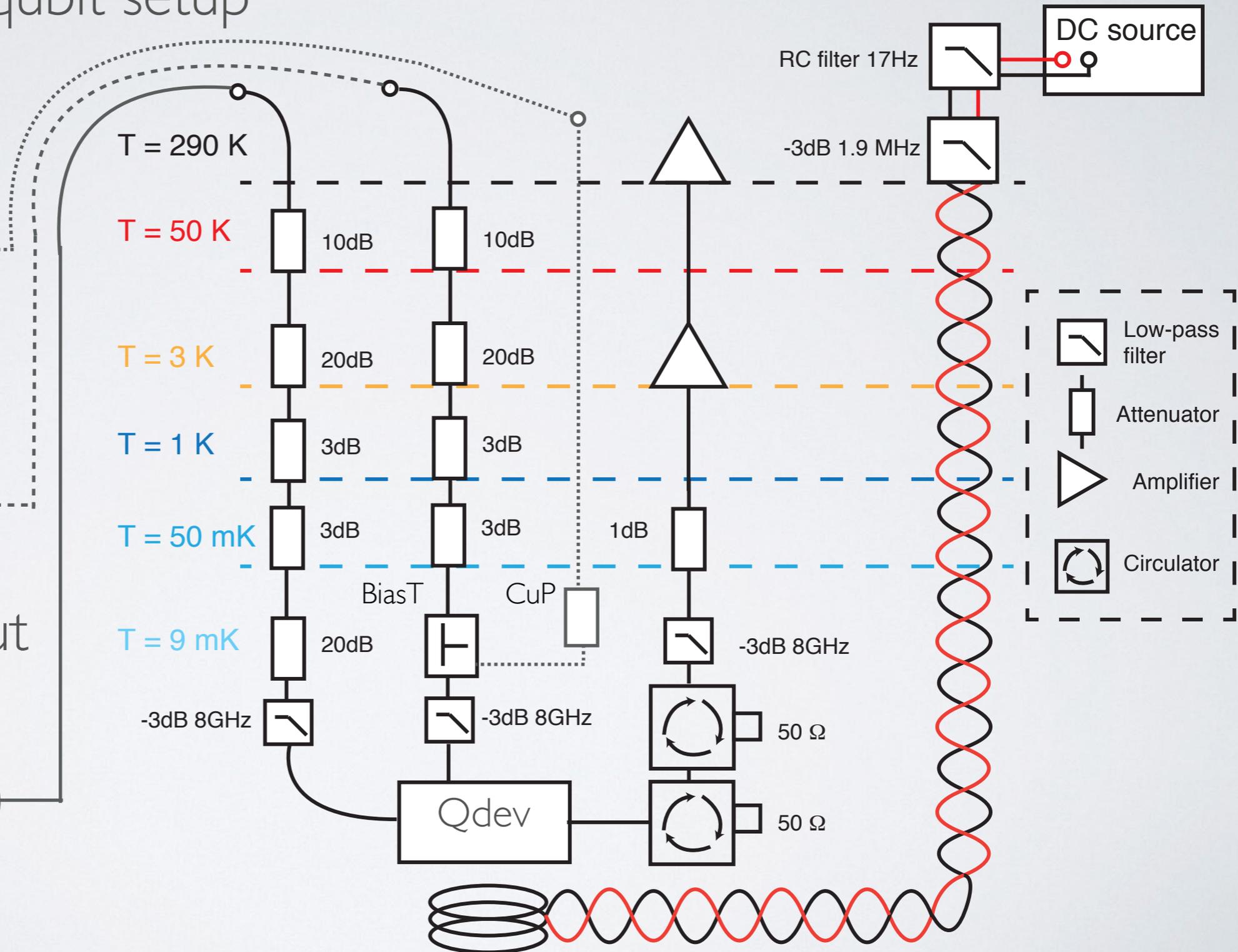
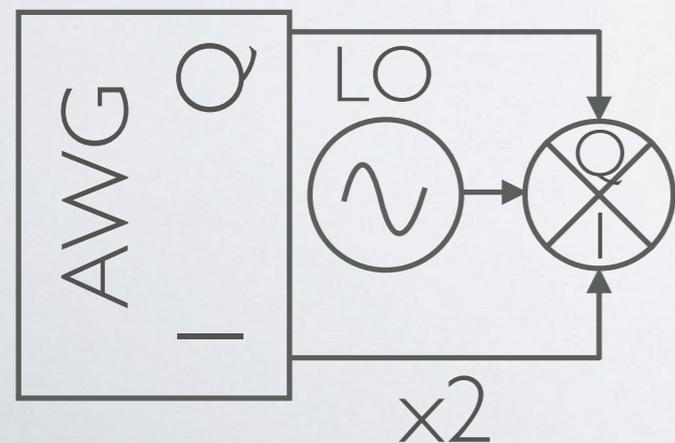
Per qubit:



z control



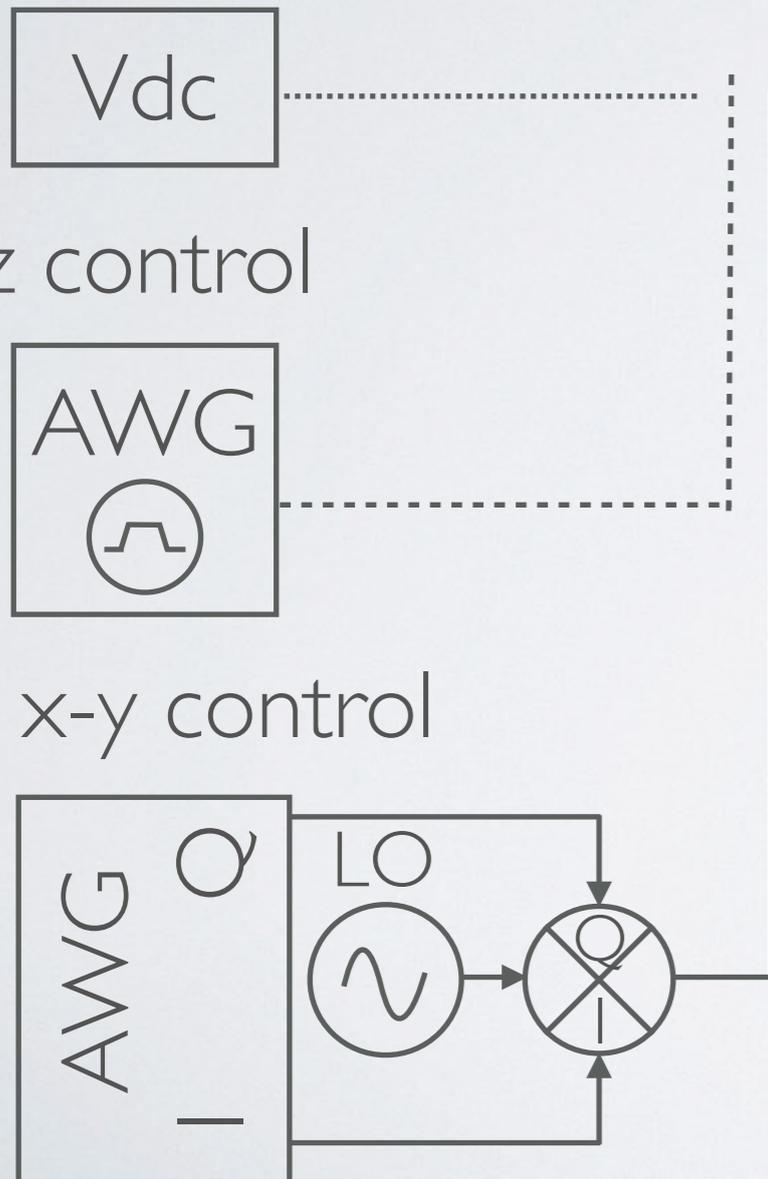
x-y control, readout



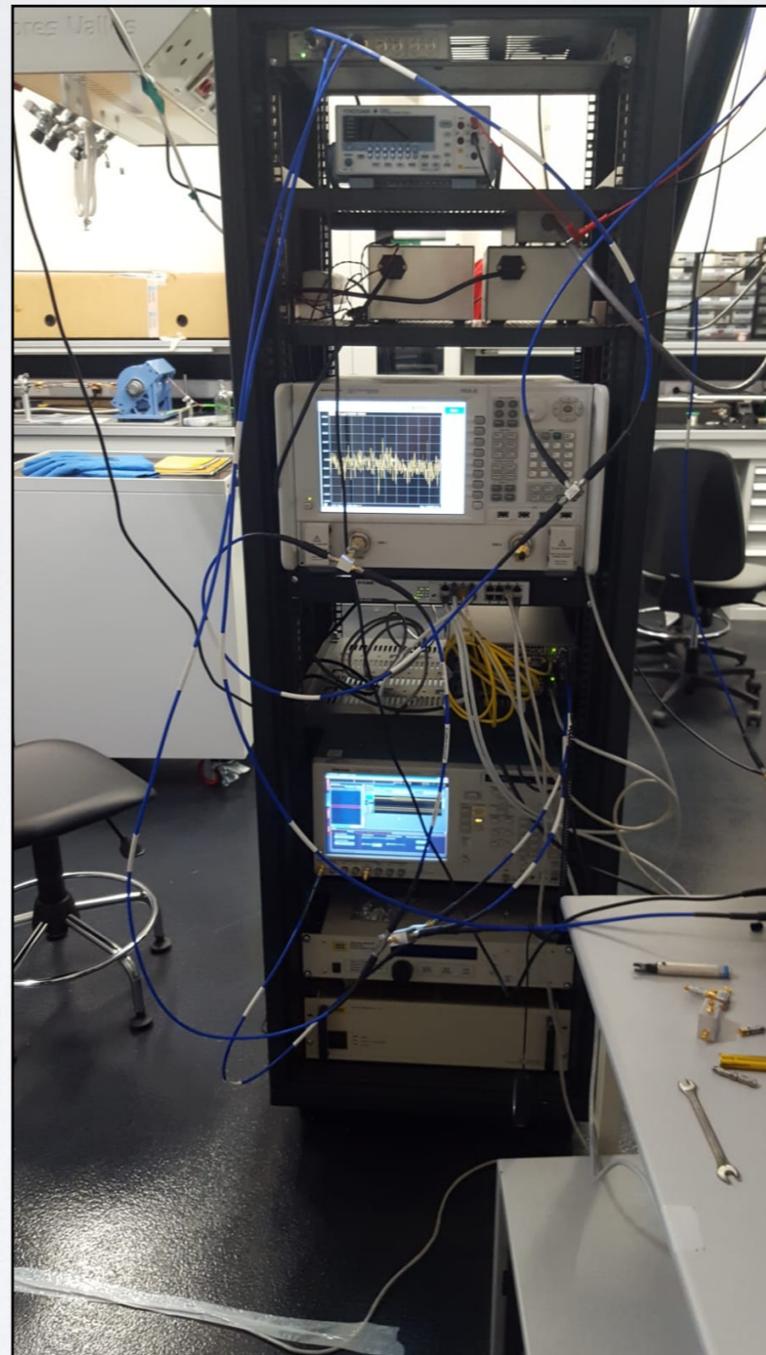
# QUBIT STATE CONTROL

## Setup

Per qubit:

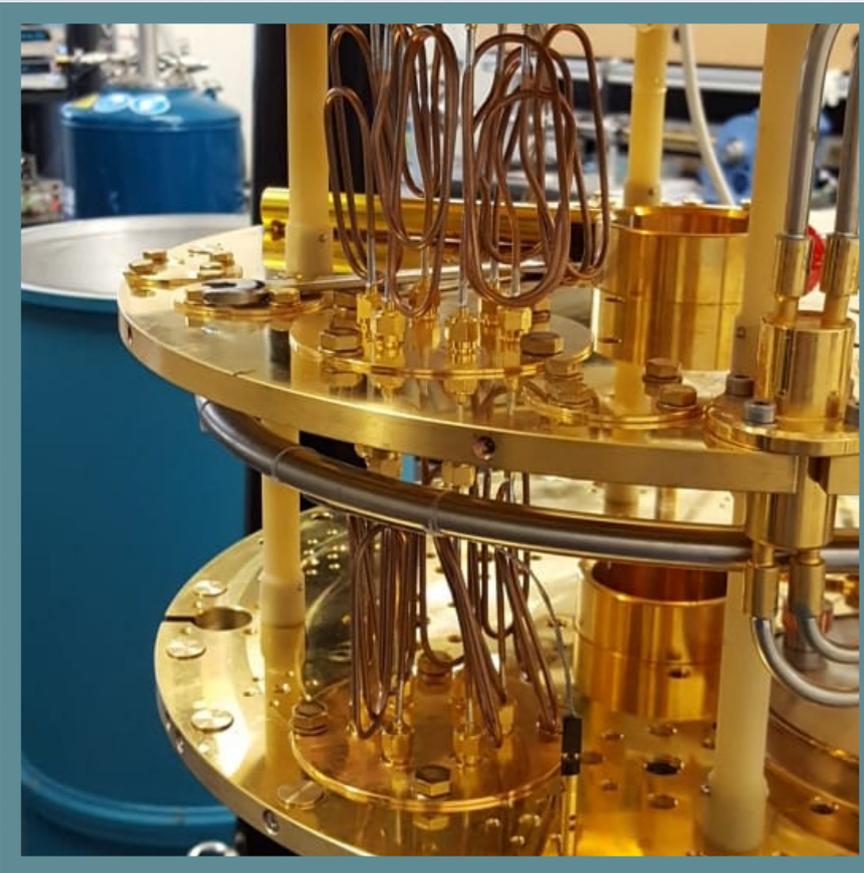


## ICN2 setup

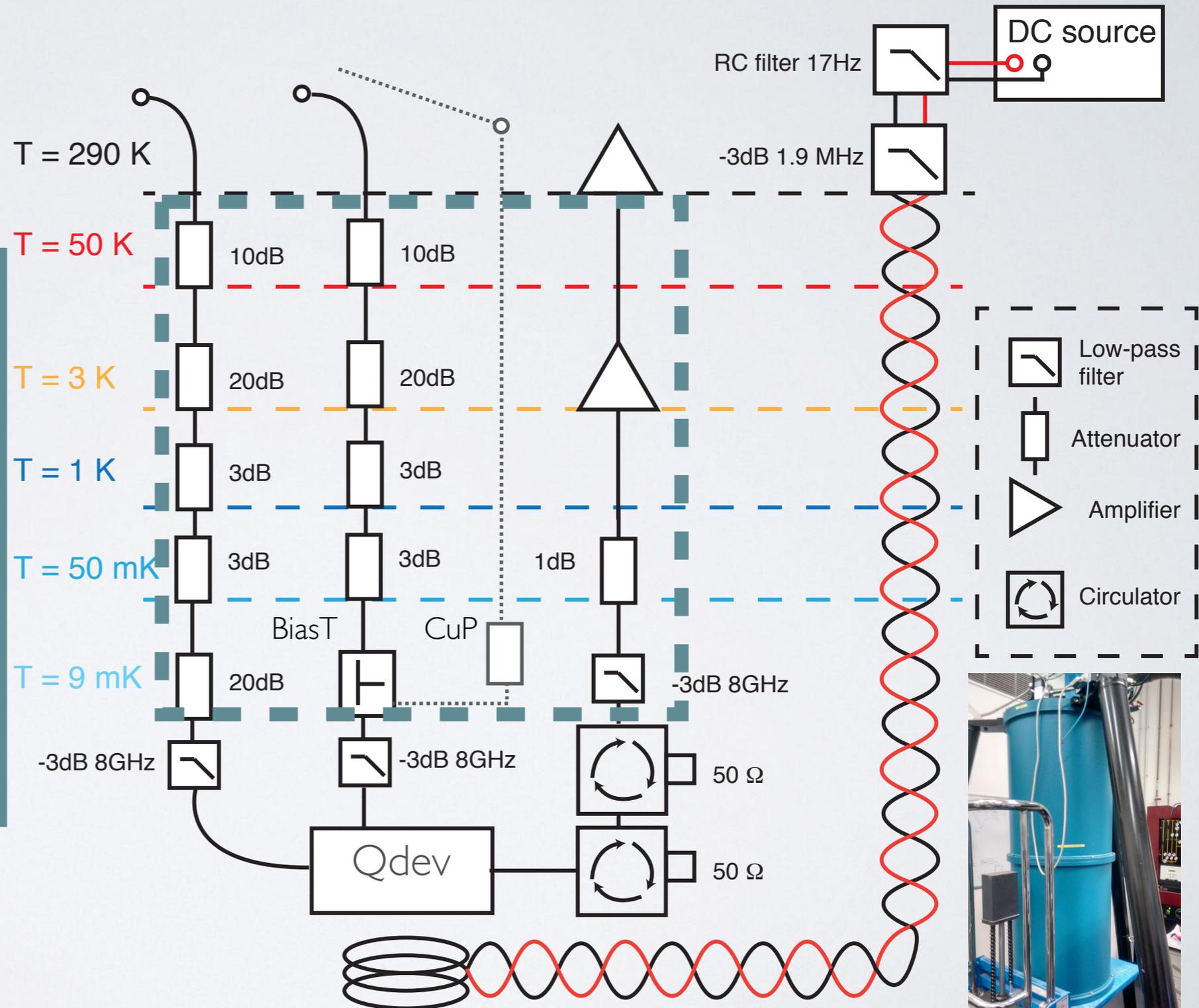


# QUBIT STATE CONTROL

Coaxial wiring  
dilution fridge



$T = 10 \text{ mK}$



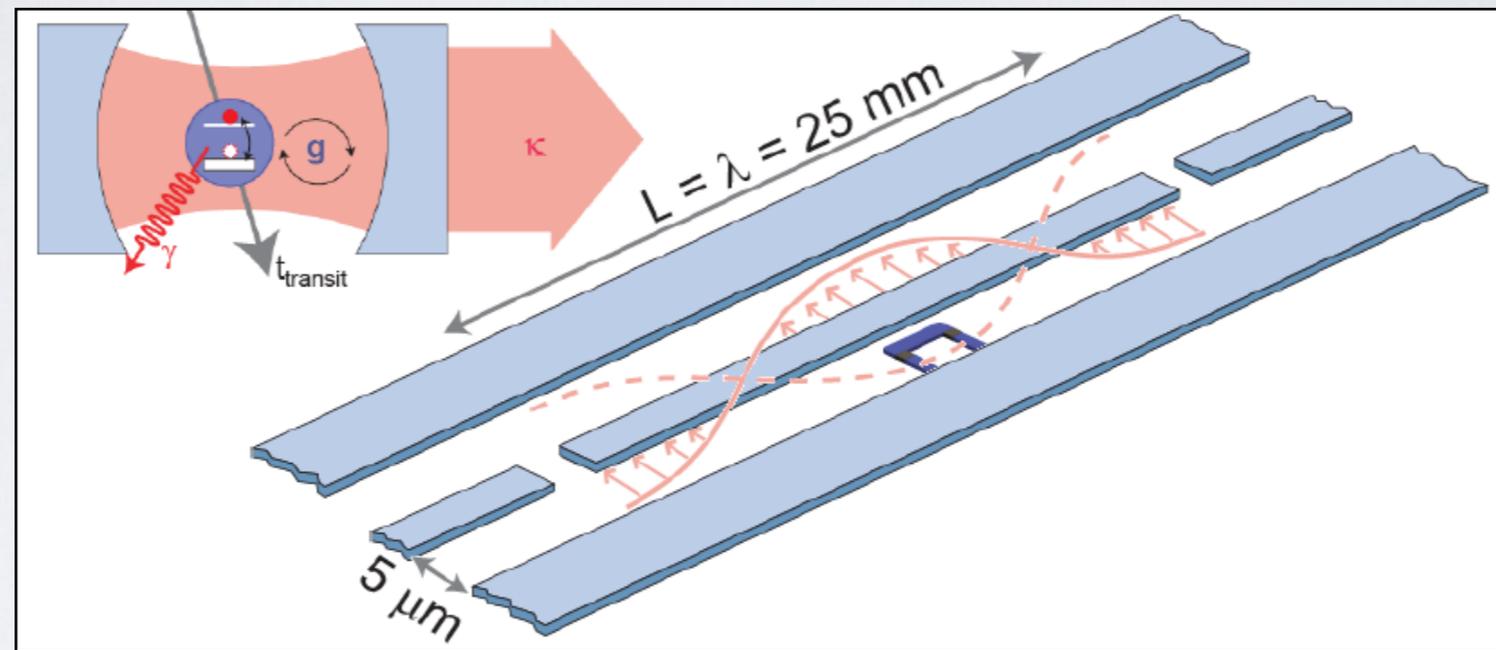


# OUTLINE

- Quantum computation
- Superconducting qubits
- Qubit state control
- **A** superconducting quantum computer

# QUBIT STATE CONTROL

Wiring quantum chips: circuit QED

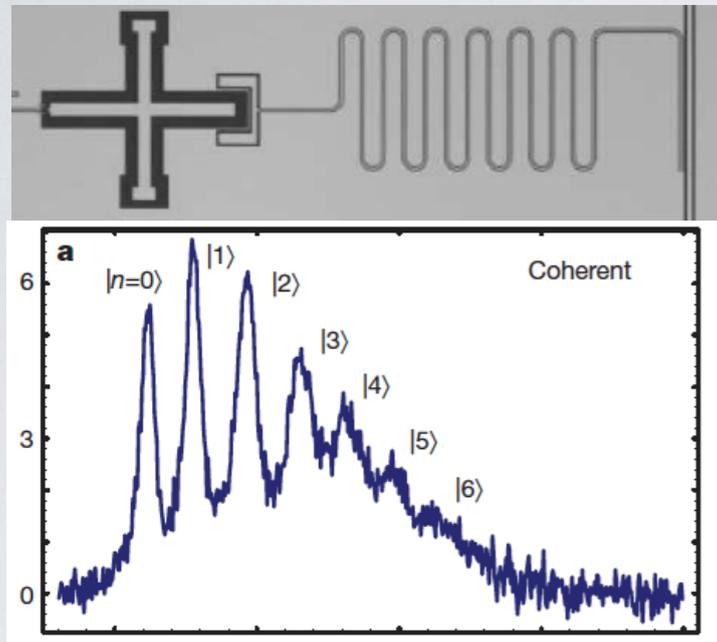


Quantum optics  
on a chip

	Photon propagation	Frequency range (Hz)	Two-level systems	Photon storage	Cavity lifetime	Atom dipole	Coupling strength
Optics	Free space, fibers	$10^{14}$	atoms	cavities	10 ns	1 a.u.	MHz
Microwave	Transmission lines	$10^9$	qubits	resonators	100 us	$10^4$ a.u.	GHz

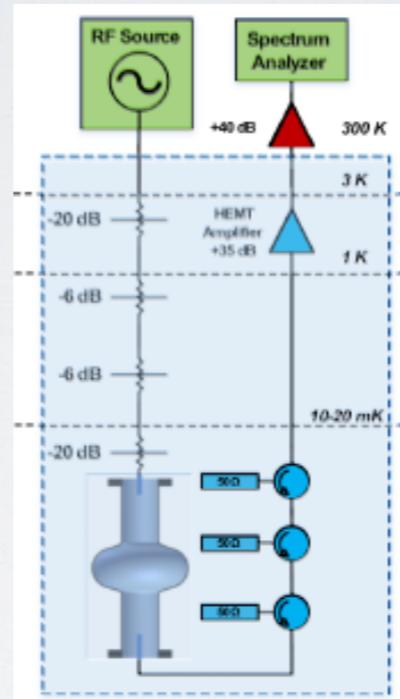
# QUBIT STATE CONTROL

Dispersive qubit/resonator readout



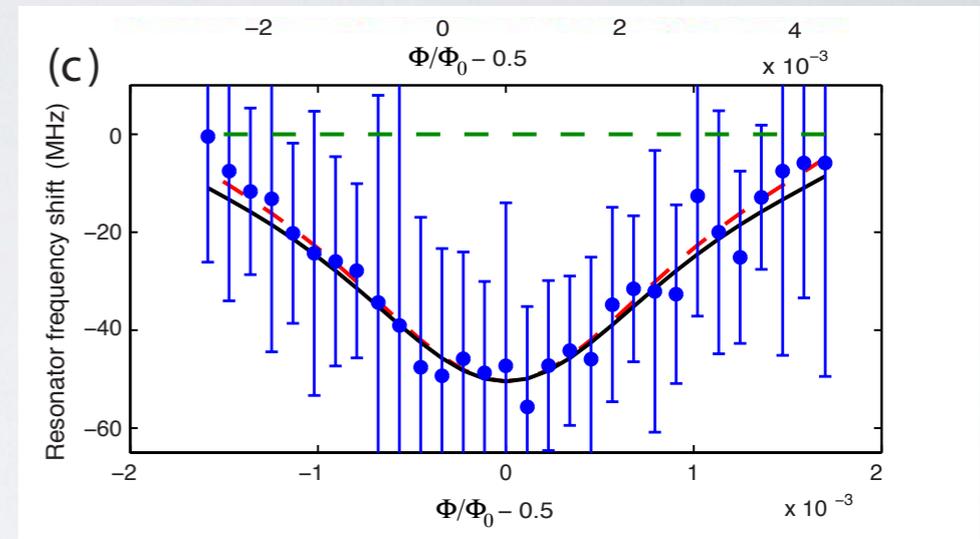
D. Schuster et al., *Nature* 445, 515 (2007)

@Fermilab



arxiv:1810.03703

Beyond QO: Ultrastrong couplings



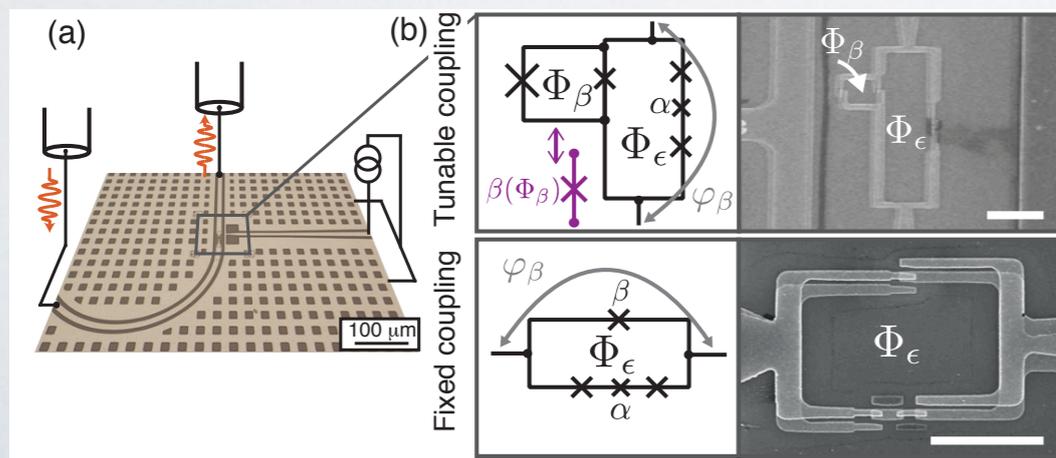
Forn-Díaz et al., *PRL* 105, 237001 (2010)

Quantum simulation of HEP

Garziano et al., *Phys. Rev. A* 90, 043817 (2014)

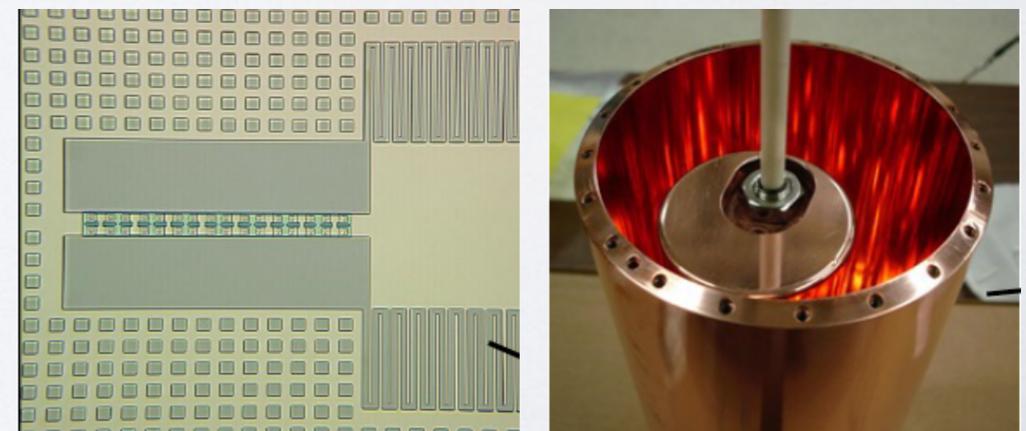
D. Marcos et al., *Phys. Rev. Lett.* 111, 110504 (2013)

Waveguide QED: Propagating photons



Forn-Díaz et al., *Nature Phys.* 13, 39 (2017)

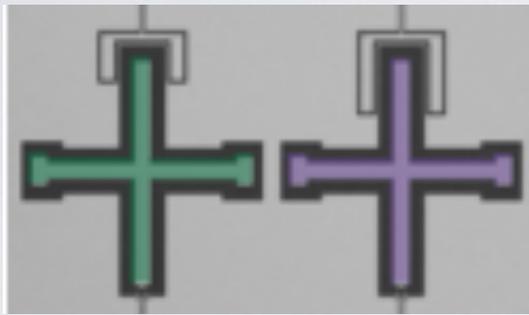
Axion detection with JPAs arxiv:1611.07123



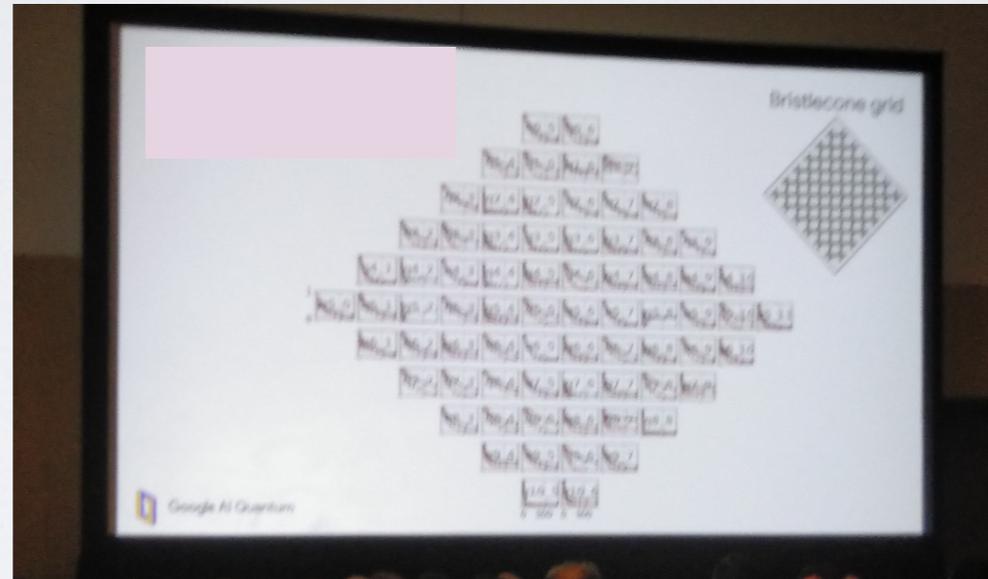
# A SUPERCONDUCTING QUANTUM COMPUTER

72-qubit (2019) *Google/UCSB group*

Direct qubit-qubit coupling

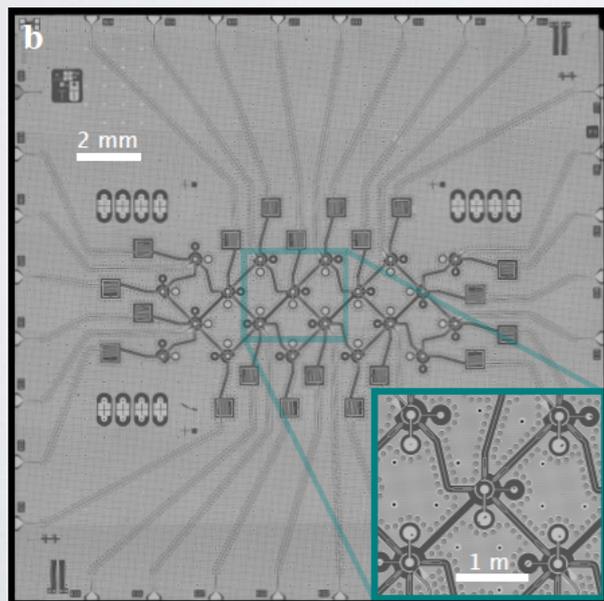


*Nature* 508, 500-503 (2014)



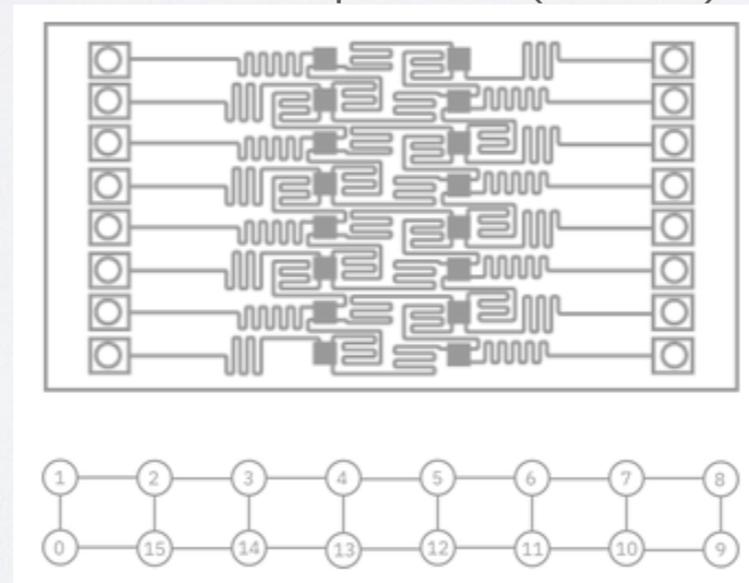
Large enough device to demonstrate quantum supremacy/advantage

Rigetti, 19 qubits (2017)



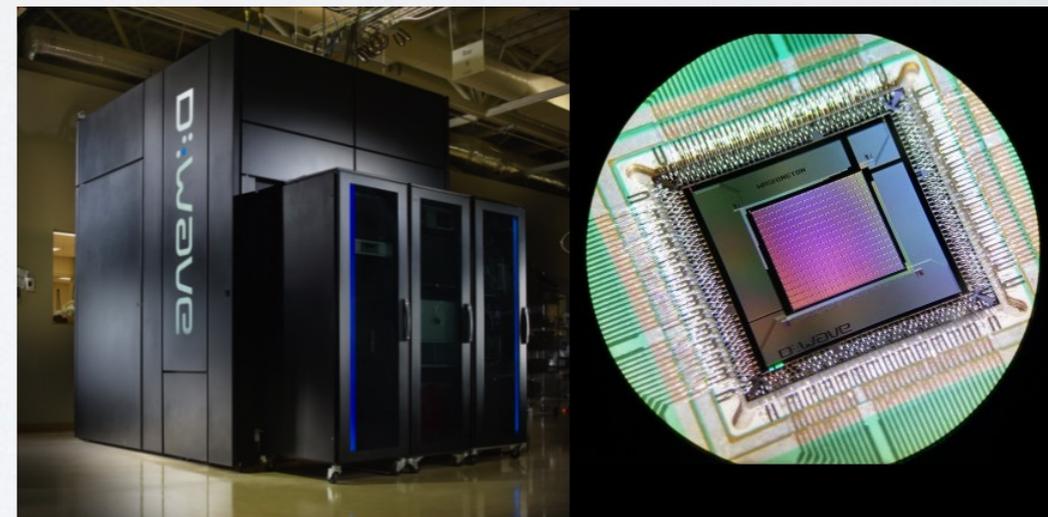
Machine learning

IBM, 20 qubits (2018)



IBM Quantum experience  
Online free access

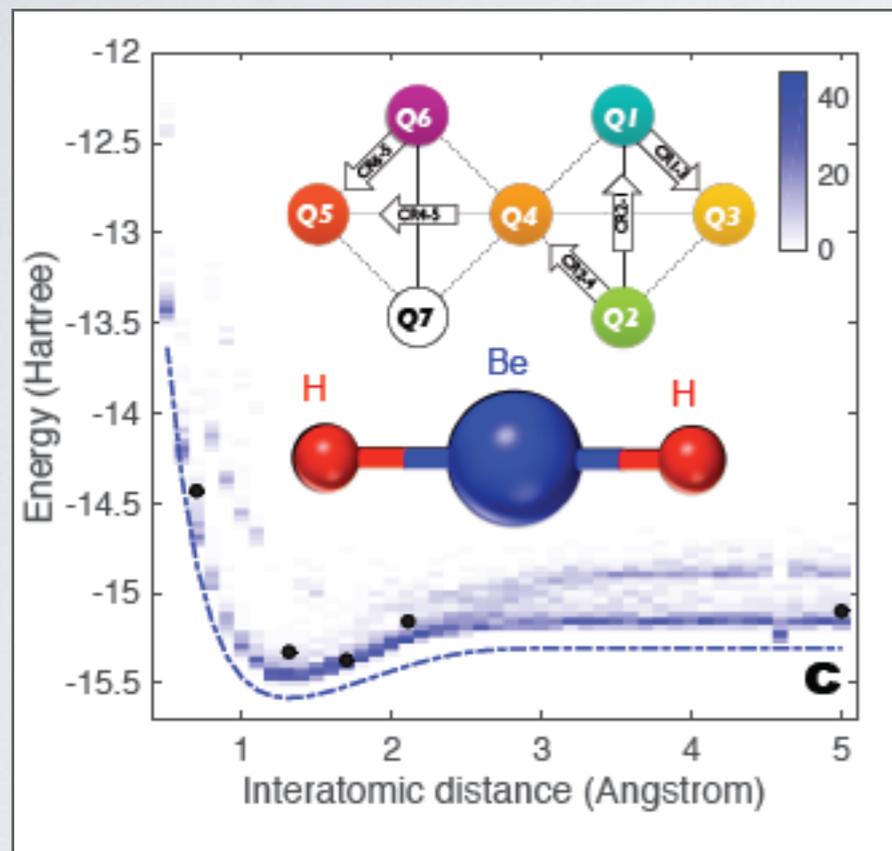
D-Wave, 2000Q (2017)



Quantum annealing, simulators

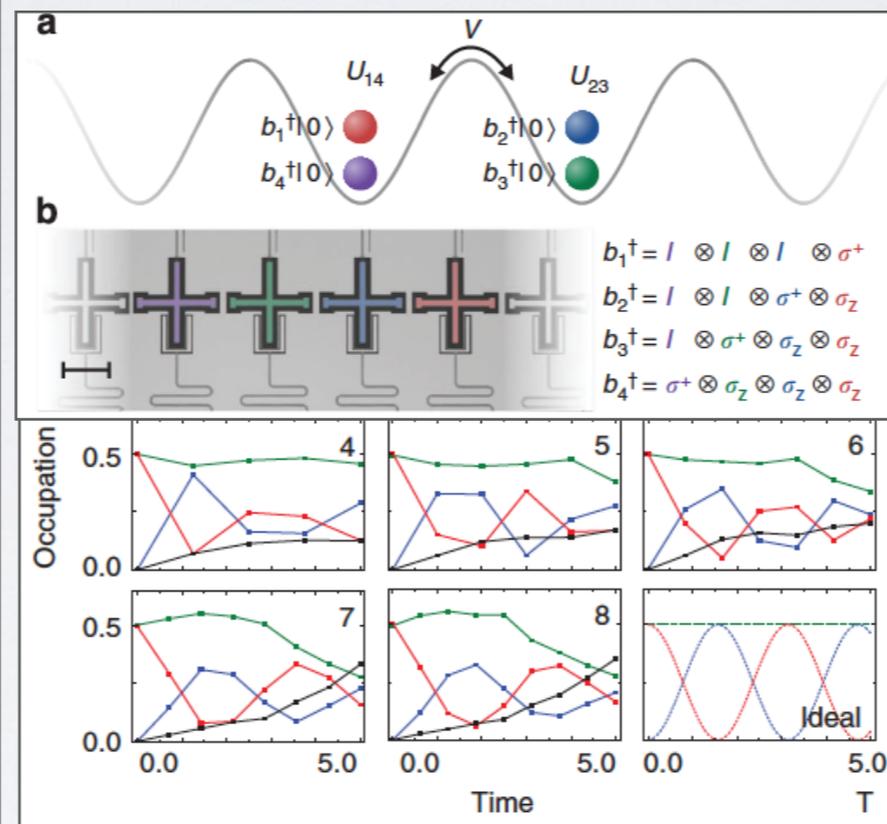
# A SUPERCONDUCTING QUANTUM COMPUTER

Hybrid classical-quantum algorithms:  
Variational quantum eigensolvers



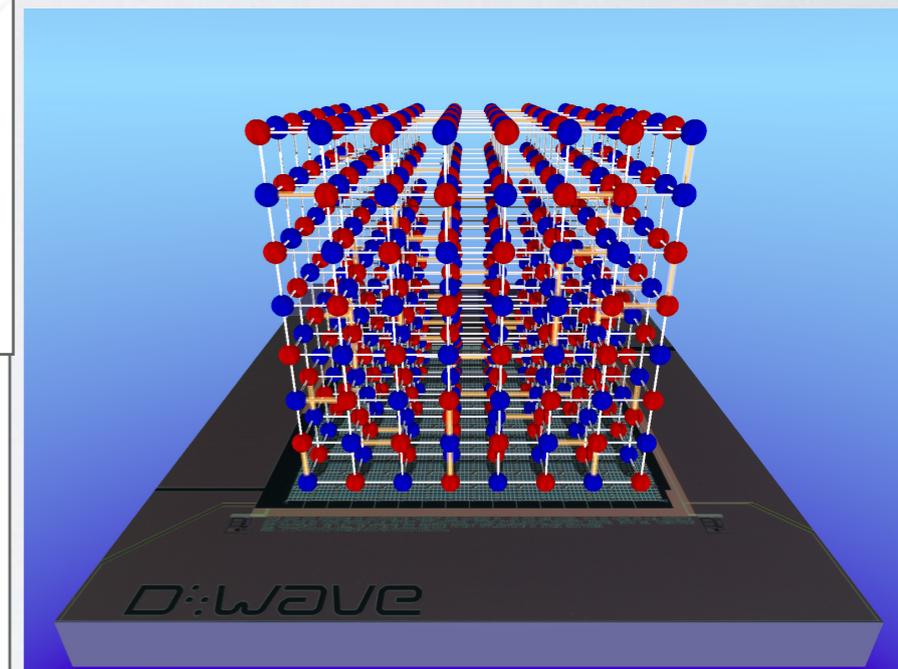
IBM

Digital quantum simulation of  
fermion-fermion scattering



Google

Analog simulator of cubic  
spin lattice



D-Wave

# A SUPERCONDUCTING QUANTUM COMPUTER

BUT...

- Available gate-based algorithms **far** from producing usable applications
- Scalability of qubit number marks **slow** pacing

STILL, ALTERNATIVES EXIST

- Develop quantum algorithms for **small-scale** processors w/o QEC
- Parallel dedicated efforts in **more resilient** quantum technologies with **shorter-term** potential, such as coherent **Quantum Annealing.**

# CONCLUSIONS

- **Q**uantum computers will disrupt our society
- **S**uperconducting qubits are one of the most promising platforms
- **M**ulti-qubit circuits already in operation
- **I**n the next few years, quantum computers will become a reality

Thank you!

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